



海洋生物地球化学
全国重点实验室(厦门大学)
State Key Laboratory of
Marine Environmental Science



廈門大學
Optical
Oceanography
Laboratory

Inherent Optical Properties (IOPs)

Lecture 2: Inversion & Application

Contents:

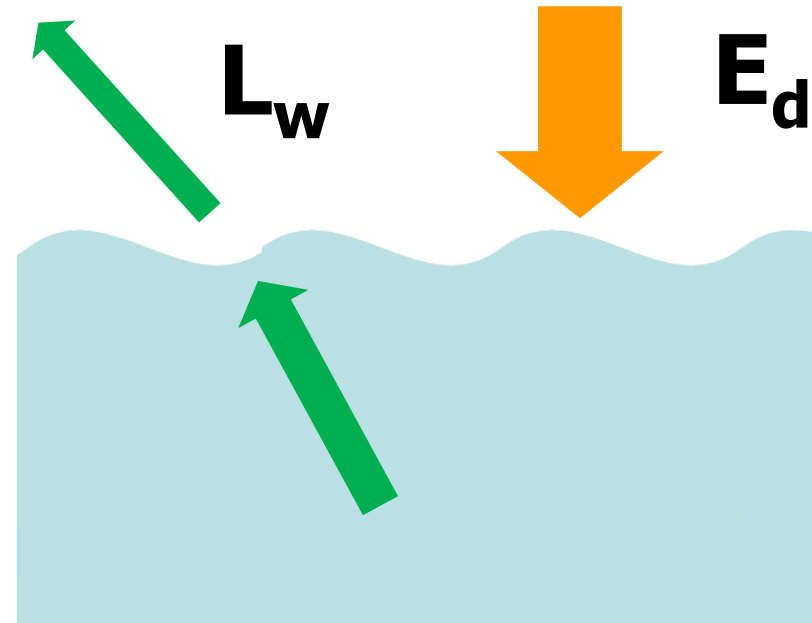
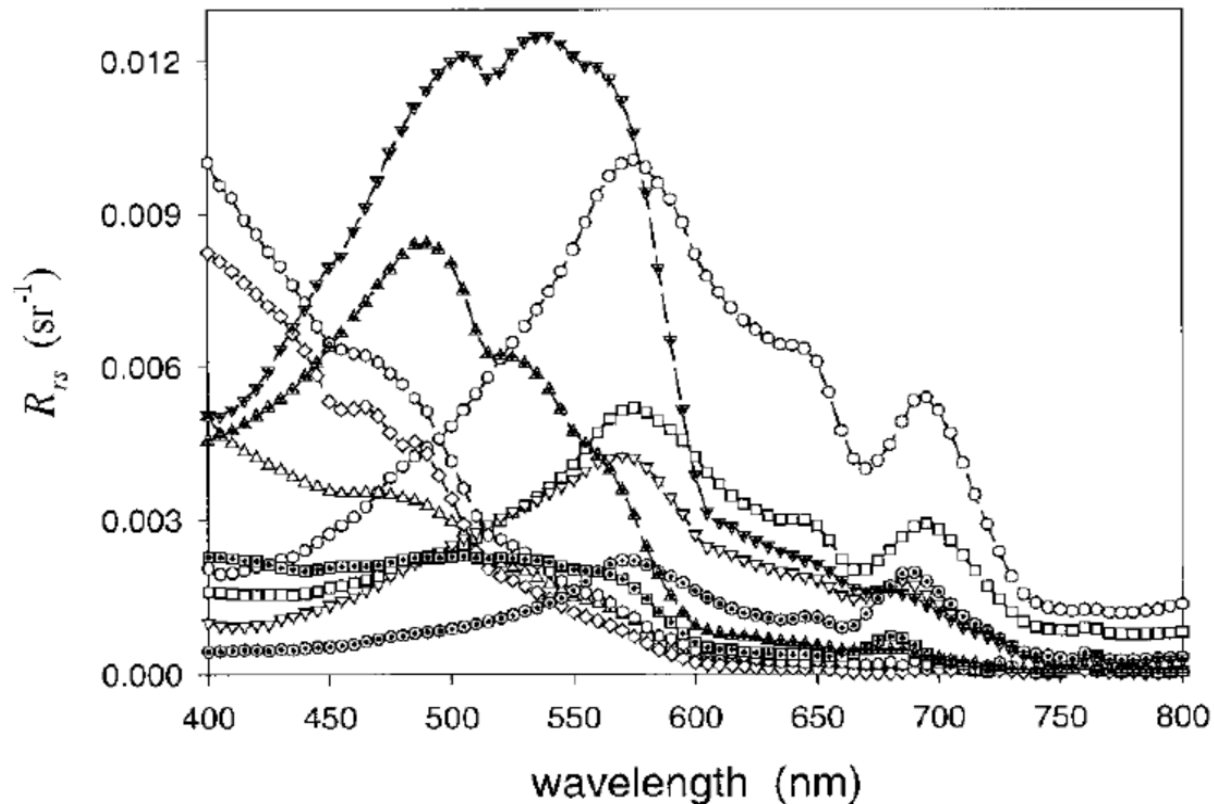
I. Inversion algorithms for IOPs

II. Applications of inverted IOPs

I. Inversion algorithms for IOPs

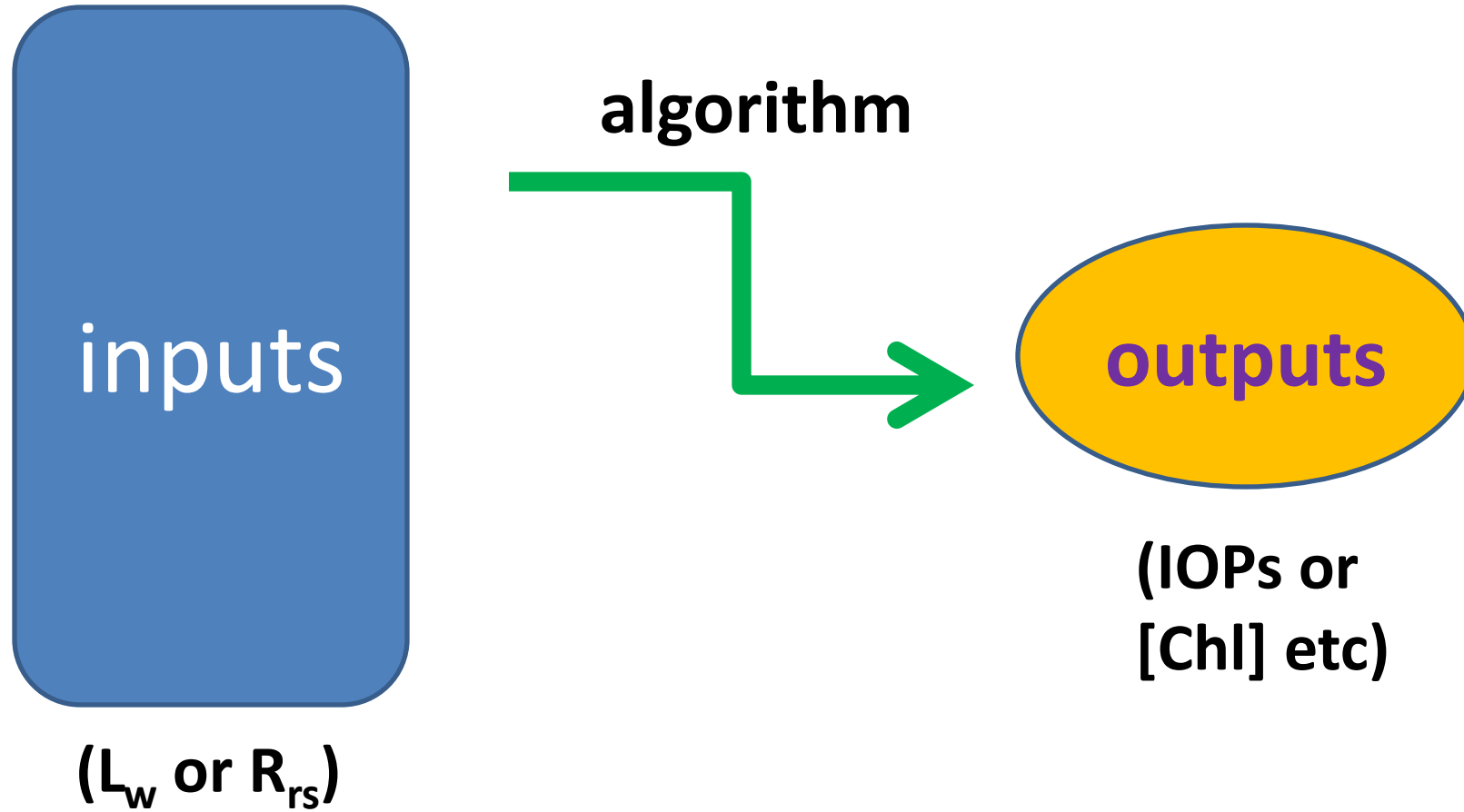
Remote-sensing reflectance (sr^{-1}):

$$R_{rs}(\lambda) = \frac{L_w(\lambda, 0^+)}{E_d(\lambda, 0^+)}$$



The ultimate objective of RS:
Retrieval useful/important
environmental information

How?
algorithm!



Empirical
(explicit or implicit)

Bio-optical models: **No need**

Semi-analytical
(algebraic, LUT, optimization)

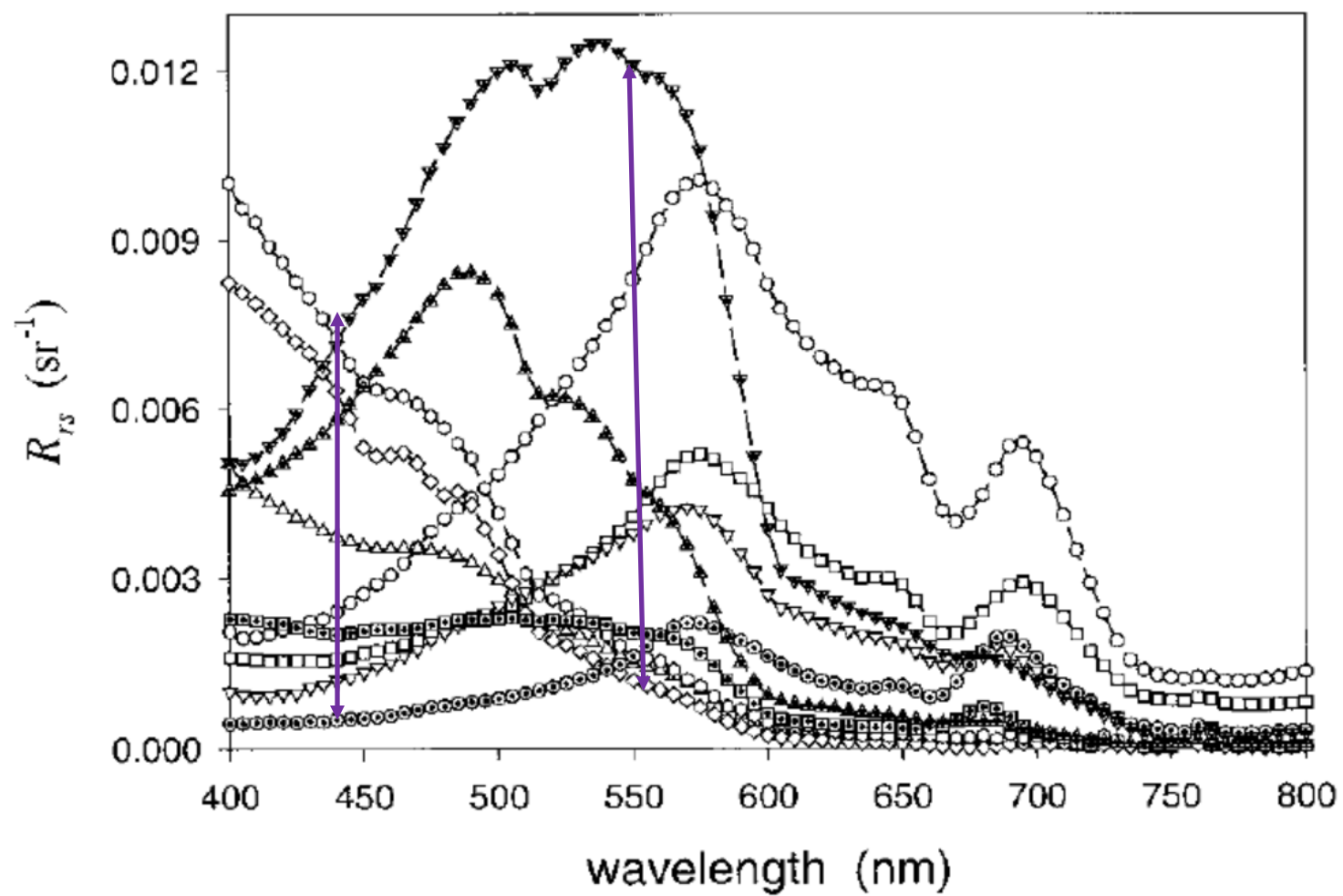
Bio-optical models: **Yes**

 **Bottom Up Strategy (BUS)**
Top Down Strategy (TDS)

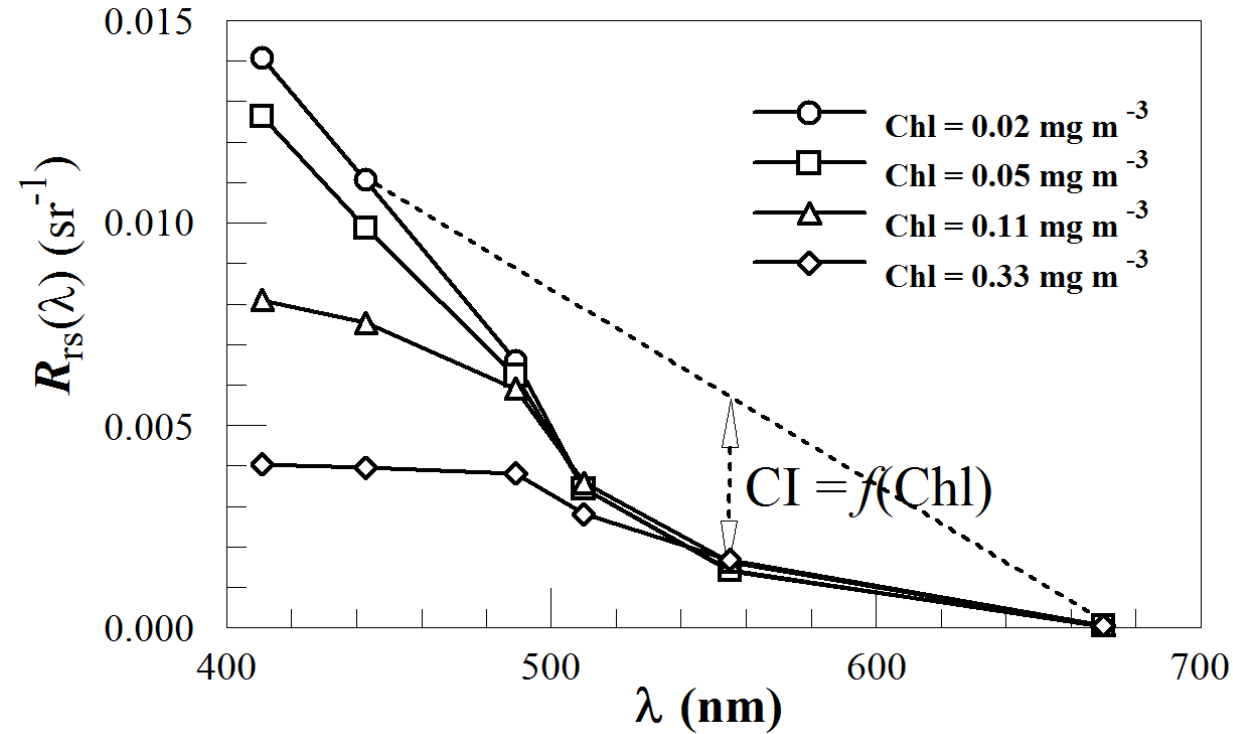
band-ratio algorithms for Chl

Algorithm	Type	Result Equation(s)	Band Ratio (R), Coefficients (a)
Global processing (GPs)	power	$C_{13} = 10^{(a0 + a1 \cdot R1)}$ $C_{23} = 10^{(a2 + a3 \cdot R2)}$ $[C + P] = C_{13}$; if C_{13} and $C_{23} > 1.5 \mu\text{g L}^{-1}$ then $[C + P] = C_{23}$	$R1 = \log(\text{Lwn443}/\text{Lwn550})$ $R2 = \log(\text{Lwn520}/\text{Lwn550})$ $a = [0.053, 1.705, 0.522, 2.440]$
Clark three-band (C3b)	power	$[C + P] = 10^{(a0 + a1 \cdot R)}$	$R = \log((\text{Lwn443} + \text{Lwn520})/\text{Lwn550})$ $a = [0.745, -2.252]$
Aiken-C	hyperbolic + power	$C_{21} = \exp(a0 + a1 \cdot \ln(R))$ $C_{23} = (R + a2)/(a3 + a4 \cdot R)$ $C = C_{21}$; if $C < 2.0 \mu\text{g L}^{-1}$ then $C = C_{23}$	$R = \text{Lwn490}/\text{Lwn555}$ $a = [0.464, -1.989, -5.29, 0.719, -4.23]$
Aiken-P	hyperbolic + power	$C_{22} = \exp(a0 + a1 \cdot \ln(R))$ $C_{24} = (R + a2)/(a3 + a4 \cdot R)$ $[C + P] = C_{22}$; if $[C + P] < 2.0 \mu\text{g L}^{-1}$ then $[C + P] = C_{24}$	$R = \text{Lwn490}/\text{Lwn555}$ $a = [0.696, -2.085, -5.29, 0.592, -3.48]$
OCTS-C	power	$C = 10^{(a0 + a1 \cdot R)}$	$R = \log((\text{Lwn520} + \text{Lwn565})/\text{Lwn490})$ $a = [0.55006, 3.497]$
OCTS-P	multiple regression	$[C + P] = 10^{(a0 + a1 \cdot R1 + a2 \cdot R2)}$	$R1 = \log(\text{Lwn443}/\text{Lwn520})$ $R2 = \log(\text{Lwn490}/\text{Lwn520})$ $a = [0.19535, -2.079, -3.497]$
POLDER	cubic	$C = 10^{(a0 + a1 \cdot R + a2 \cdot R^2 + a3 \cdot R^3)}$	$R = \log(\text{Rrs443}/\text{Rrs565})$ $a = [0.438, -2.114, 0.916, -0.851]$
CalCOFI two-band linear	power	$C = 10^{(a0 + a1 \cdot R)}$	$R = \log(\text{Rrs490}/\text{Rrs555})$ $a = [0.444, -2.431]$
CalCOFI two-band cubic	cubic	$C = 10^{(a0 + a1 \cdot R + a2 \cdot R^2 + a3 \cdot R^3)}$	$R = \log(\text{Rrs490}/\text{Rrs555})$ $a = [0.450, -2.860, 0.996, -0.3674]$
CalCOFI three-band	multiple regression	$C = \exp(a0 + a1 \cdot R1 + a2 \cdot R2)$	$R1 = \ln(\text{Rrs490}/\text{Rrs555})$ $R2 = \ln(\text{Rrs510}/\text{Rrs555})$ $a = [1.025, -1.622, 1.238]$
CalCOFI four-band	multiple regression	$C = \exp(a0 + a1 \cdot R1 + a2 \cdot R2)$	$R1 = \ln(\text{Rrs443}/\text{Rrs555})$ $R2 = \ln(\text{Rrs412}/\text{Rrs510})$ $a = [0.753, -2.583, 1.389]$
Morel-1	power	$C = 10^{(a0 + a1 \cdot R)}$	$R = \log(\text{Rrs443}/\text{Rrs555})$ $a = [0.2492, -1.768]$
Morel-2	power	$C = \exp(a0 + a1 \cdot R)$	$R = \ln(\text{Rrs490}/\text{Rrs555})$ $a = [1.077835, -2.542605]$
Morel-3	cubic	$C = 10^{(a0 + a1 \cdot R + a2 \cdot R^2 + a3 \cdot R^3)}$	$R = \log(\text{Rrs443}/\text{Rrs555})$ $a = [0.20766, -1.82878, 0.75885, -0.73979]$
Morel-4	cubic	$C = 10^{(a0 + a1 \cdot R + a2 \cdot R^2 + a3 \cdot R^3)}$	$R = \log(\text{Rrs490}/\text{Rrs555})$ $a = [1.03117, -2.40134, 0.3219897, -0.291066]$

(O'Reilly et al. 1998)

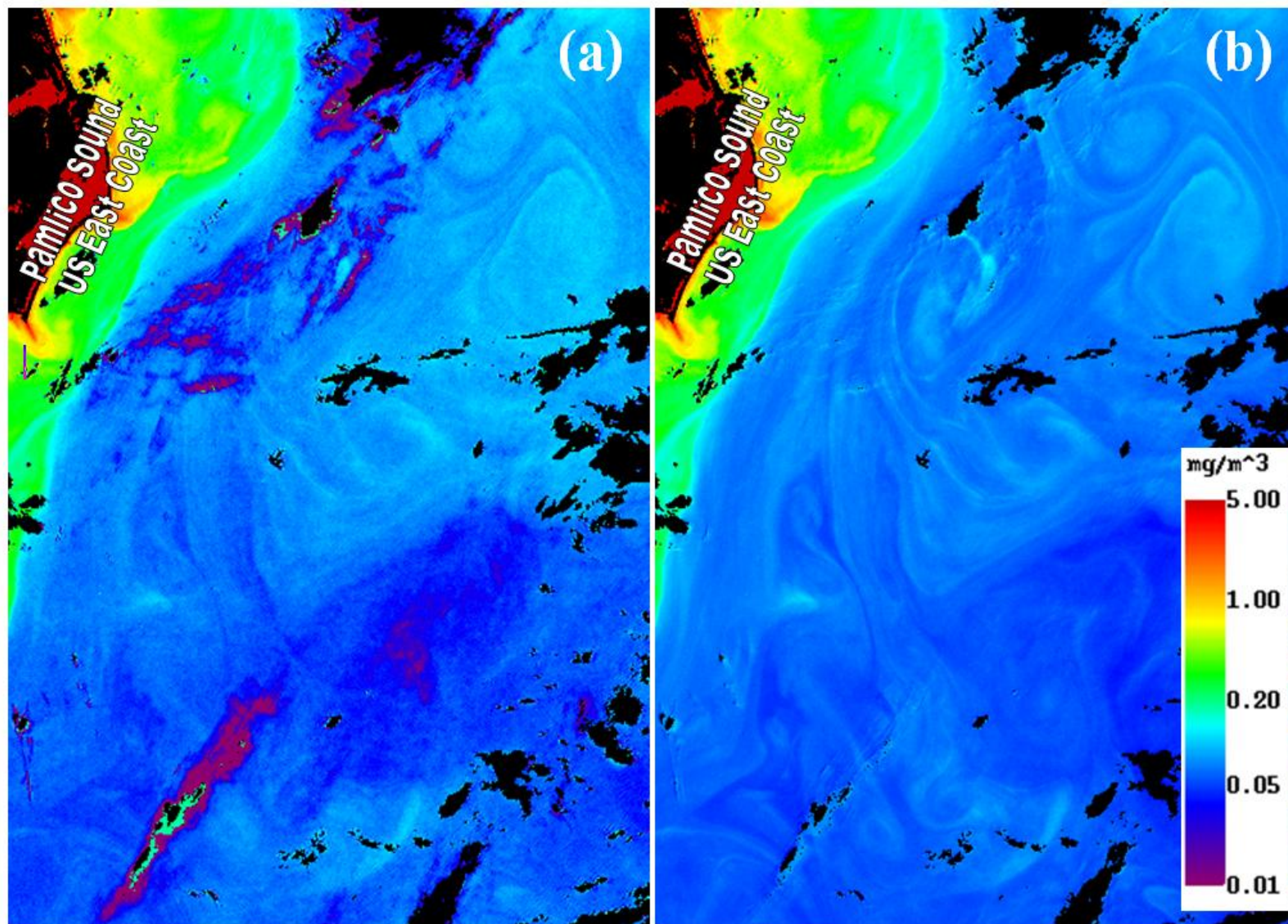


Chl based on band difference



$$CI = R_{rs}(555) - \left\{ R_{rs}(443) + \frac{555 - 443}{670 - 443} \times [R_{rs}(670) - R_{rs}(443)] \right\}$$

$$\text{Chl} = 10^{-0.49 + 191.66 \text{ CI}}; \quad CI \leq -0.0005 \text{ sr}^{-1}$$



$$R_{rs}^{Sat}(\lambda) = R_{rs}(\lambda) + \delta(\lambda) = R_{rs}(\lambda) + y \lambda + x$$

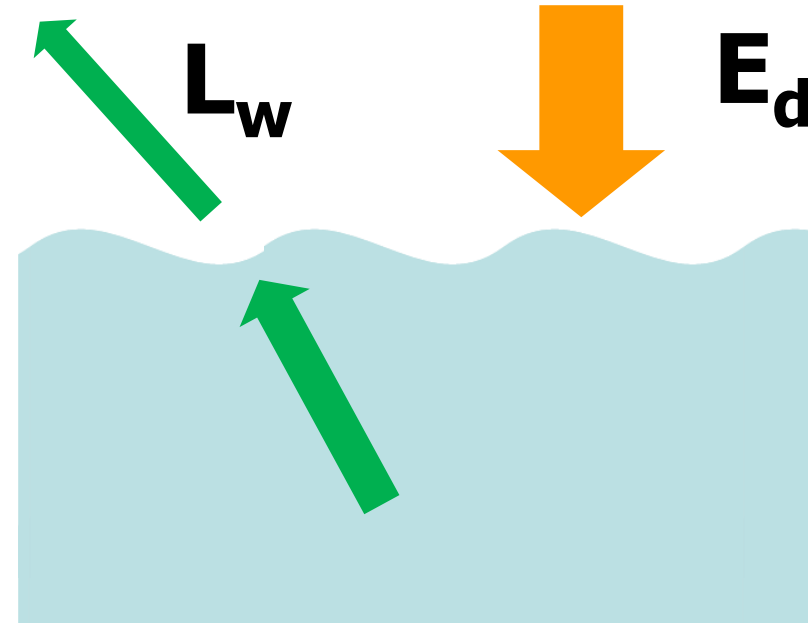
$$MBD_{Rrs440} = R_{rs}(555) - \left[R_{rs}(443) + \frac{555 - 443}{670 - 443} (R_{rs}(670) - R_{rs}(443)) \right]$$

$$MBD(R_{rs}^{Sat}) = MBD_{Rrs}$$

Physics-based algorithms (mechanistic)

Remote-sensing reflectance (sr^{-1}):

$$R_{rs}(\lambda) = \frac{L_w(\lambda, 0^+)}{E_d(\lambda, 0^+)}$$



How is R_{rs} related to water's optical (biogeochemical) properties?

Physics-based algorithms (mechanistic)

$$r_{rs}(\lambda, \pi) = \sum_{i=1}^2 g_i \left(\frac{b_b(\lambda)}{a(\lambda) + b_b(\lambda)} \right)^i;$$

$$g_1 = 0.0949, g_2 = 0.0794$$

(Gordon et al, 1988)

$$r_{rs} \Rightarrow R_{rs} ?$$

$$R_{rs} = \frac{L_w}{E_d(0^+)}$$

$$E_d(0^-) = t_E E_d(0^+) + \gamma E_u(0^-)$$

$$L_w = \frac{t_L}{n_w^2} L_u(0^-)$$

$$R_{rs} = \frac{t_E t_L}{n_w^2} \frac{r_{rs}}{1 - \gamma R} \doteq \frac{0.52 r_{rs}}{1 - 1.7 r_{rs}}$$

Solve Rrs for IOPs or in-water constituents?

Two common strategies:

1. Bottom-up strategy (BUS):

Assume we know the spectral shapes of the optically active components

2. Top-down strategy (TDS):

Only need the spectral shape information when it is necessary

What are we facing in RS inversion?

$$R_{rs}(\lambda) = F(a(\lambda), b_b(\lambda))$$



$$R_{rs}(\lambda) = F(a_w(\lambda), a_{ph}(\lambda), a_{dg}(\lambda), b_{bw}(\lambda), b_{bp}(\lambda))$$



$$\begin{cases} R_{rs}(\lambda_1) = F(a_w(\lambda_1), a_{ph}(\lambda_1), a_{dg}(\lambda_1), b_{bw}(\lambda_1), b_{bp}(\lambda_1)) \\ R_{rs}(\lambda_2) = F(a_w(\lambda_2), a_{ph}(\lambda_2), a_{dg}(\lambda_2), b_{bw}(\lambda_2), b_{bp}(\lambda_2)) \\ \vdots \\ R_{rs}(\lambda_n) = F(a_w(\lambda_n), a_{ph}(\lambda_n), a_{dg}(\lambda_n), b_{bw}(\lambda_n), b_{bp}(\lambda_n)) \end{cases}$$

of unknowns > # of equations!

An ill formulated math problem!

Have to increase # of equations or decrease # of unknowns!

1. Bottom-up strategy (BUS):

Build-up an Rrs spectrum block-by-block:

$$a(\lambda) = a_w(\lambda) + \sum a_{xi}(\lambda) \qquad b_b(\lambda) = b_{bw}(\lambda) + \sum b_{bxi}(\lambda)$$

$$a(\lambda) = a_w(\lambda) + a_{ph}(\lambda) + a_d(\lambda) + a_g(\lambda)$$

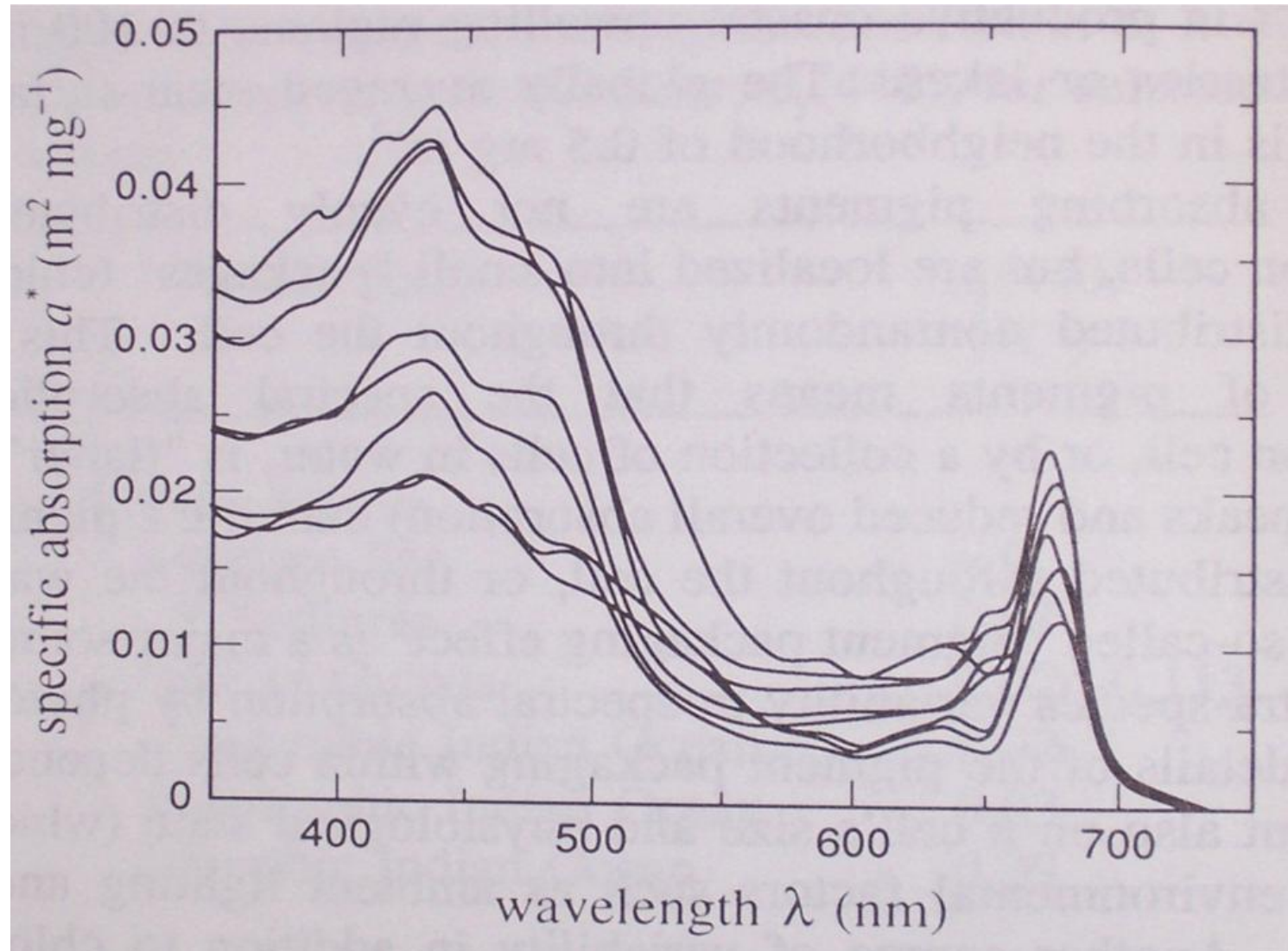
$$a(\lambda) = a_w(\lambda) + a_{ph}(\lambda) + a_{dg}(\lambda)$$

$$a(\lambda) = a_w(\lambda) + M_1 \langle a_{ph}(\lambda) \rangle + M_2 \langle a_{dg}(\lambda) \rangle$$

$$b_b(\lambda) = b_{bw}(\lambda) + b_{bp}(\lambda)$$

$$b_b(\lambda) = b_{bw}(\lambda) + M_3 \langle b_{bp}(\lambda) \rangle$$

➡ Bio-optical models (forward model)



Modeling a_{ph} spectrum

Example of **one** parameter hyperspectral $a_{ph}(\lambda)$ model:

Lee (1994); Lee et al (1998):

$$a_{ph}(\lambda) = (a_0(\lambda) + a_1(\lambda) \ln(P)) P$$

$$P = a_{ph}(440)$$

Bricaud et al (1995):

$$a_{ph}(\lambda) = A_{ph}(\lambda) Chl^{1-B_{ph}(\lambda)}$$

Table 2. Spectral Values of the Constants Obtained When Fitting the Variations of $a_{ph}^*(\lambda)$ Versus the (chl $a + div$) Concentration (Chl) to Power Laws of the Form $a_{ph}^*(\lambda) = A(\lambda) (Chl)^{-B(\lambda)}$ and Determination Coefficients on the Log-Transformed Data r^2

λ , nm	A	B	r^2	λ , nm	A	B
400	0.0263	0.282	0.702	402	0.0271	0.281
404	0.0280	0.282	0.706	406	0.0290	0.281
408	0.0301	0.282	0.710	410	0.0313	0.283
412	0.0323	0.286	0.718	414	0.0333	0.291
416	0.0342	0.293	0.725	418	0.0349	0.296
420	0.0356	0.299	0.733	422	0.0359	0.306
424	0.0362	0.313	0.746	426	0.0369	0.316
428	0.0376	0.317	0.749	430	0.0386	0.314
432	0.0391	0.318	0.750	434	0.0395	0.324
436	0.0399	0.328	0.757	438	0.0401	0.332
440	0.0403	0.332	0.762	442	0.0398	0.339
444	0.0390	0.348	0.774	446	0.0383	0.355
448	0.0375	0.360	0.783	450	0.0371	0.359
452	0.0365	0.362	0.783	454	0.0358	0.366
456	0.0354	0.367	0.789	458	0.0351	0.368
460	0.0350	0.365	0.789	462	0.0347	0.366
464	0.0343	0.368	0.792	466	0.0339	0.369
468	0.0335	0.369	0.793	470	0.0332	0.368
472	0.0325	0.371	0.792	474	0.0318	0.375
476	0.0312	0.378	0.793	478	0.0306	0.379
480	0.0301	0.377	0.791	482	0.0296	0.377
484	0.0290	0.376	0.788	486	0.0285	0.373
488	0.0279	0.369	0.783	490	0.0274	0.361
492	0.0267	0.356	0.774	494	0.0258	0.349
496	0.0249	0.341	0.763	498	0.0240	0.332
500	0.0230	0.321	0.747	502	0.0220	0.311
504	0.0209	0.300	0.722	506	0.0199	0.288
508	0.0189	0.275	0.686	510	0.0180	0.260
512	0.0171	0.249	0.641	514	0.0163	0.237
516	0.0156	0.224	0.578	518	0.0149	0.211
520	0.0143	0.196	0.498	522	0.0137	0.184
524	0.0131	0.173	0.417	526	0.0126	0.162
528	0.0121	0.151	0.332	530	0.0117	0.139
532	0.0113	0.129	0.248	534	0.0108	0.119
536	0.0104	0.109	0.176	538	0.0100	0.100
540	0.0097	0.090	0.116	542	0.0093	0.081

Table 2. Parameters for the Empirical $a_{ph}(\lambda)$ Simulation by Eq. (12)^a

Wavelength	$a_0(\lambda)$	$a_1(\lambda)$
390	0.5813	0.0235
400	0.6843	0.0205
410	0.7782	0.0129
420	0.8637	0.006
430	0.9603	0.002
440	1.0	0
450	0.9634	0.006
460	0.9311	0.0109
470	0.8697	0.0157
480	0.789	0.0152
490	0.7558	0.0256
500	0.7333	0.0559
510	0.6911	0.0865
520	0.6327	0.0981
530	0.5681	0.0969
540	0.5046	0.09
550	0.4262	0.0781
560	0.3433	0.0659
570	0.295	0.06
580	0.2784	0.0581

Example of two-parameters model:

(Ciotti et al 2002)

$$a_{\phi}(\lambda) = a_{\phi}(505) \{ [S_f \cdot \bar{a}_{<pico>}(\lambda)] + [(1 - S_f) \cdot \bar{a}_{<micro>}(\lambda)] \}$$

Table 3. Basis vectors representing the normalized absorption for the smallest ($\bar{a}_{(pico)}(\lambda)$, *Prochlorococcus*) and biggest ($\bar{a}_{(micro)}(\lambda)$, average microplankton) cell sizes in our data set. Wavelength (λ) in nm. Basis vectors for $\bar{a}_{ph}(\lambda)$ can be constructed by setting $\bar{a}_{(pico)}(676)$ to 0.023 m² mg⁻¹, $\bar{a}_{(micro)}(674)$ to 0.0086 m² mg⁻¹, and scaling for the other wavelengths accordingly.

λ	Pico	Micro	λ	Pico	Micro	λ	Pico	Micro	λ	Pico	Micro	λ	Pico	Micro
400	1.682	1.574												
402	1.734	1.584	462	2.526	1.623	522	0.544	1.013	582	0.111	0.459	642	0.191	0.528
404	1.800	1.600	464	2.455	1.616	524	0.522	0.992	584	0.072	0.452	644	0.174	0.526
406	1.890	1.617	466	2.402	1.606	526	0.486	0.977	586	0.073	0.452	646	0.197	0.528
408	1.978	1.633	468	2.331	1.592	528	0.448	0.959	588	0.073	0.449	648	0.176	0.538
410	2.057	1.654	470	2.281	1.568	530	0.391	0.944	590	0.099	0.443	650	0.168	0.549
412	2.162	1.669	472	2.205	1.542	532	0.375	0.927	592	0.070	0.433	652	0.160	0.574
414	2.269	1.674	474	2.136	1.509	534	0.336	0.909	594	0.095	0.424	654	0.217	0.605
416	2.327	1.684	476	2.063	1.481	536	0.305	0.888	596	0.085	0.416	656	0.244	0.655
418	2.398	1.697	478	2.049	1.459	538	0.292	0.868	598	0.090	0.406	658	0.286	0.720
420	2.457	1.708	480	1.998	1.437	540	0.288	0.847	600	0.086	0.401	660	0.381	0.798
422	2.533	1.710	482	1.930	1.415	542	0.261	0.826	602	0.068	0.400	662	0.437	0.889
424	2.614	1.716	484	1.918	1.399	544	0.245	0.806	604	0.078	0.403	664	0.520	0.979
426	2.663	1.737	486	1.897	1.387	546	0.214	0.785	606	0.069	0.408	666	0.660	1.068
428	2.749	1.763	488	1.867	1.377	548	0.194	0.764	608	0.090	0.416	668	0.716	1.147
430	2.804	1.793	490	1.812	1.367	550	0.187	0.737	610	0.096	0.429	670	0.824	1.207
432	2.840	1.812	492	1.776	1.349	552	0.138	0.711	612	0.094	0.443	672	0.846	1.243
434	2.915	1.827	494	1.701	1.338	554	0.137	0.682	614	0.084	0.458	674	0.816	1.249
436	2.947	1.830	496	1.648	1.319	556	0.111	0.653	616	0.105	0.473	676	0.891	1.227
438	2.978	1.834	498	1.522	1.301	558	0.094	0.626	618	0.128	0.487	678	0.869	1.174
440	3.014	1.824	500	1.439	1.271	560	0.095	0.604	620	0.119	0.495	680	0.812	1.096
442	3.032	1.800	502	1.373	1.242	562	0.070	0.580	622	0.126	0.499	682	0.741	1.004
444	3.011	1.771	504	1.270	1.222	564	0.053	0.555	624	0.138	0.504	684	0.605	0.893

Multiple-parameters model:

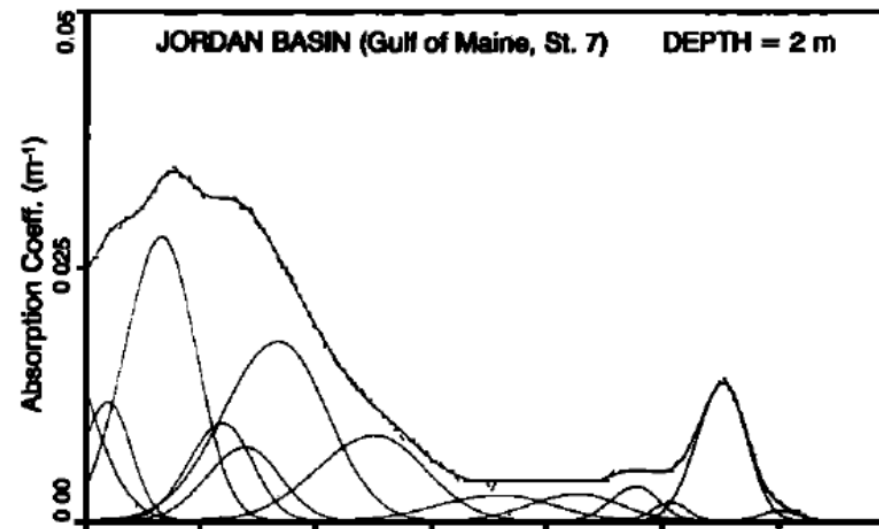
$$a_{ph}(\lambda) = \sum_{j=1}^l C_j a_j^*(\lambda_{mj}) \exp \left[\frac{(\lambda - \lambda_{mj})^2}{2\sigma_j^2} \right] \quad (7)$$

TABLE 2. Input Values and Mean Characteristics of Gaussian Bands Reflecting Absorption by Chlorophylls and Carotenoids

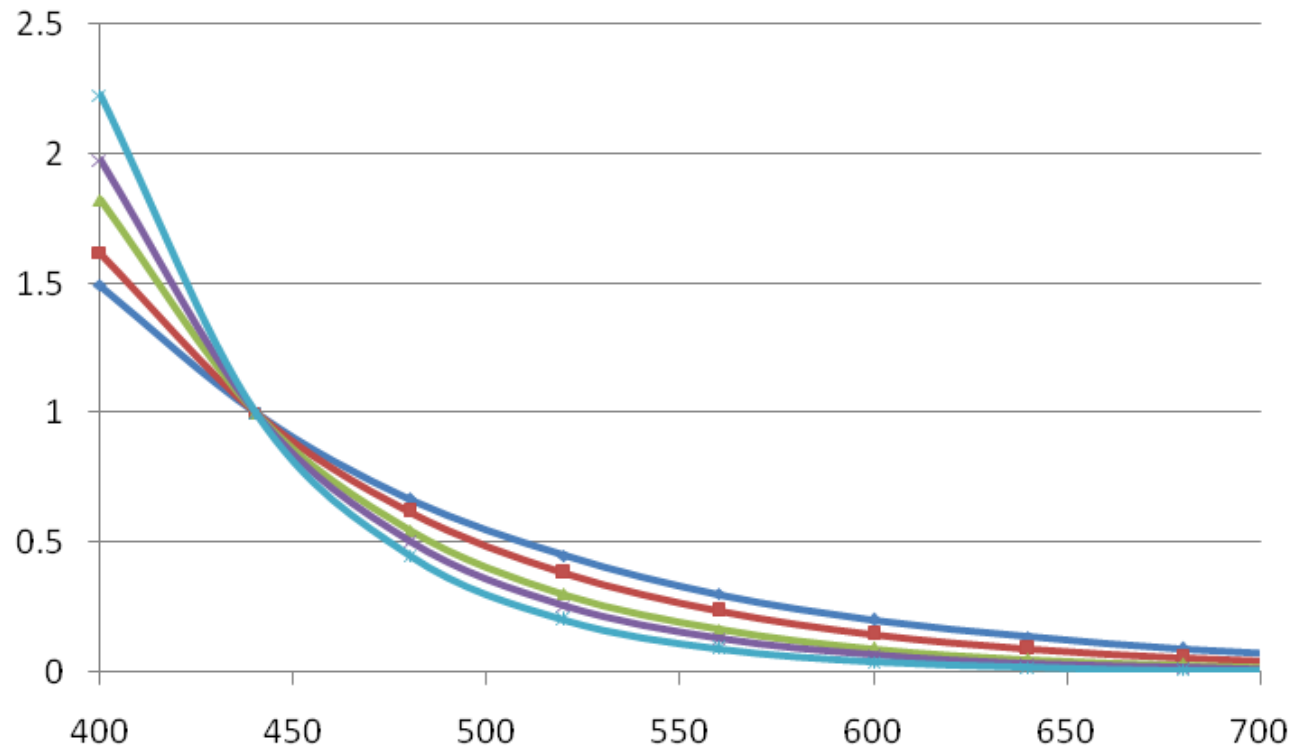
Characteristic	Gaussian Band Number and Associated Pigment Species												
	1 chl a	2 chl a	3 chl a	4 chl c	5 chl b	6 carot.	7 carot.	8 chl c	9 chl a	10 chl c	11 chl b	12 chl a	13 chl a
Input parameters													
Half width, nm	53.8	21.3	32.1	27.2	45.0	45.4	45.9	46.3	35.0	28.9	24.4	21.6	33.5
Center, nm	384	413	435	461	464	490	532	583	623	644	655	676	700
Output parameters													
Half width, nm	43.2	22.7	34.5	29.3	36.0	46.8	49.6	46.8	38.0	24.9	25.4	24.7	29.0
Center, nm	381.5	410.8	433.5	459.2	466.6	487.8	532.0	585.6	620.6	640.7	652.9	675.6	699.8
Specific absorption coefficient, m ² (mg pigment) ⁻¹	0.042	0.019	0.047	0.110	0.115	0.035	0.019	0.044	0.005	0.044	0.029	0.021	0.002

Specific absorption coefficients of each pigment are ratios of Gaussian band absorptions (in reciprocal meters) to high-performance liquid chromatography concentrations (in milligrams per cubic meter) of that pigment. Chl, chlorophyll; Carot., carotenoid.

(Hoepffner and Sathyendranath, 1993)



Absorption components: a_{dg} spectrum shapes



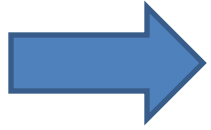
$$\langle a_{dg}(\lambda) \rangle = e^{-S(\lambda-440)}$$

S: 0.01 – 0.02 nm⁻¹

(Bricaud et al 1981)

$$\langle b_{bp}(\lambda) \rangle = \left(\frac{440}{\lambda} \right)^\eta$$

$$R_{rs}(\lambda) = G \frac{b_b(\lambda)}{a(\lambda) + b_b(\lambda)}$$



$$R_{rs}(\lambda) = G \frac{b_{bw}(\lambda) + M_3 \langle b_{bp}(\lambda) \rangle}{a_w(\lambda) + M_1 \langle a_{ph}(\lambda) \rangle + M_2 \langle a_{dg}(\lambda) \rangle + b_{bw}(\lambda) + M_3 \langle b_{bp}(\lambda) \rangle}$$

3-variable model to describe an Rrs spectrum

(Sathyendranath et al 1989)

M_{1-3} are wavelength independent variables.

Then they could be derived by comparing the modeled Rrs spectrum with the measured Rrs spectrum.

Spectral ranges used for solutions (e.g. examples of BUS):

The **blue-green** domain: e.g., Hoge and Lyon (1996), Carder et al (1999)

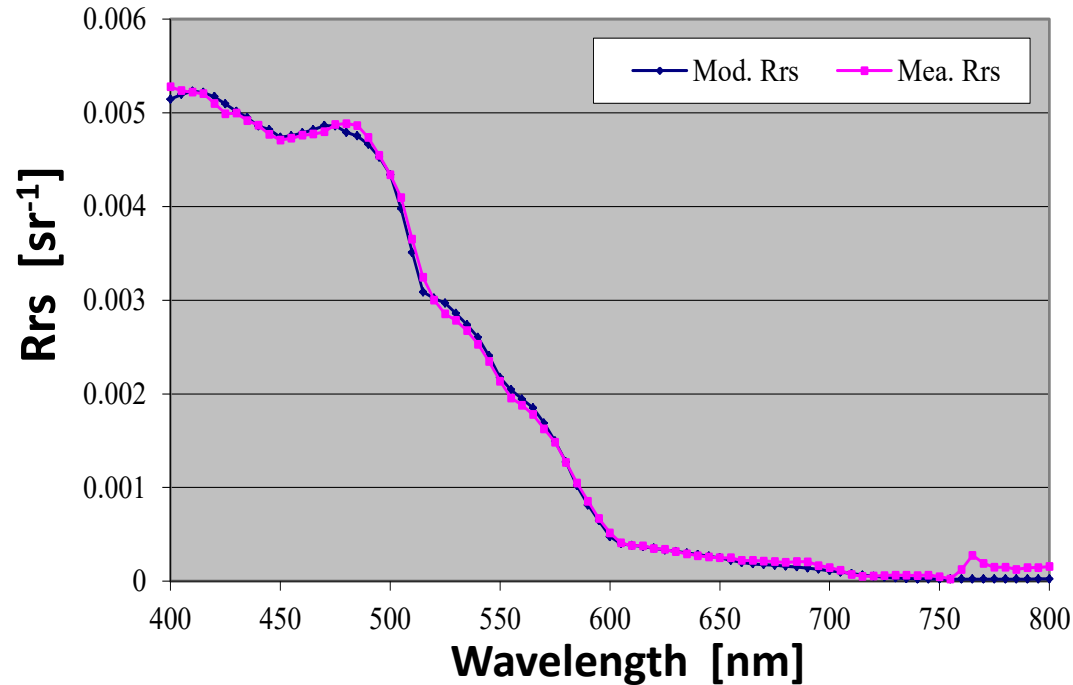
The **red-infrared** domain: e.g., Binding et al (2012)

The **entire spectrum (spectral optimization)**: e.g., Bukata et al (1995), Lee et al (1994,1996,1999), Maritorena et al (2002), Boss and Roesler (2006), Brando et al (2012), Werdell et al (2013)

Look-Up-Tables (LUT): e.g., Carder et al (1991); Mobley et al (2005)

Spectral Optimization

Matching between measured and modeled R_{rs} spectra



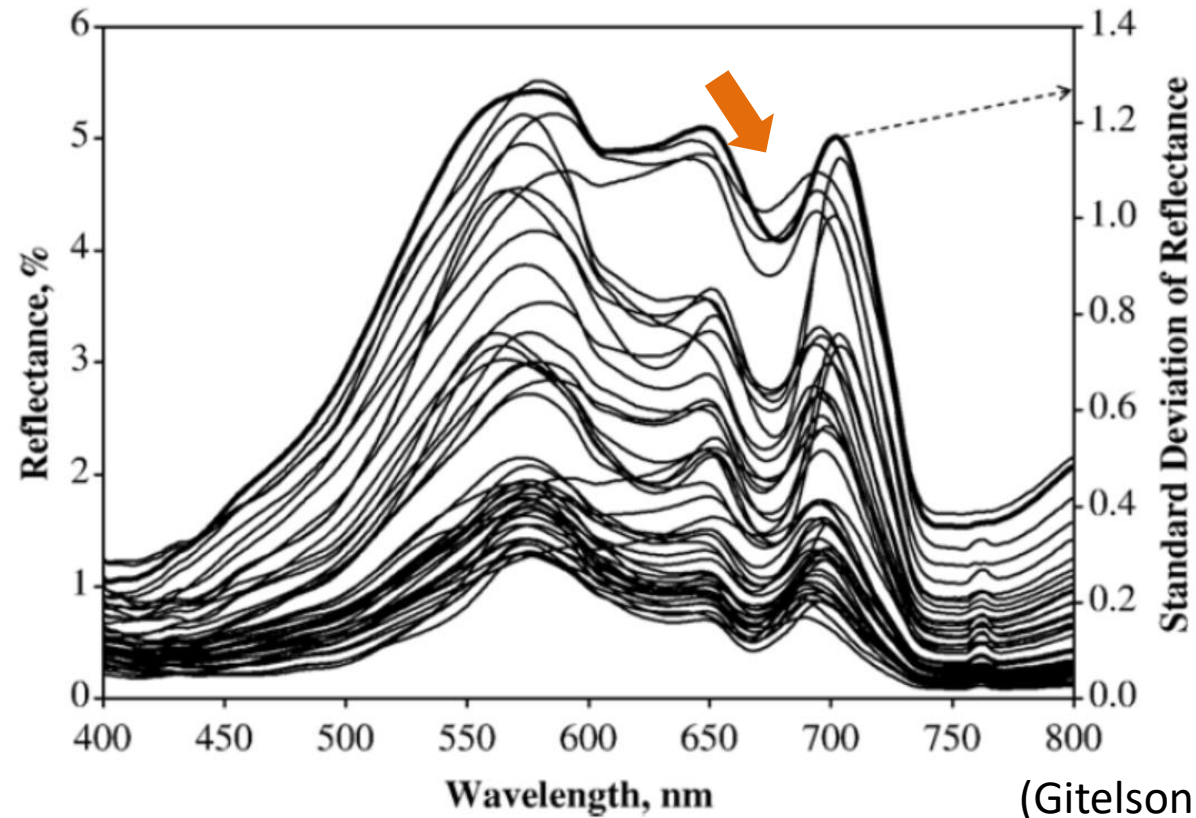
Quantitative measure of the closure (**error function**):

$$\delta_{R_{rs}} = \frac{\sqrt{\Lambda_{\lambda 1}^{\lambda 2} (\tilde{R}_{rs}(\lambda) - R_{rs}(\lambda))^2}}{\Lambda_{\lambda 1}^{\lambda 2} R_{rs}(\lambda)} = \sqrt{n} \frac{\sqrt{\sum_{\lambda 1}^{\lambda 2} (\tilde{R}_{rs}(\lambda) - R_{rs}(\lambda))^2}}{\sum_{\lambda 1}^{\lambda 2} R_{rs}(\lambda)}$$

Logic (assumption) behind SOA:

A unique set of bio-optical properties for each R_{rs} spectrum.

Algorithms using information in the red-infrared bands



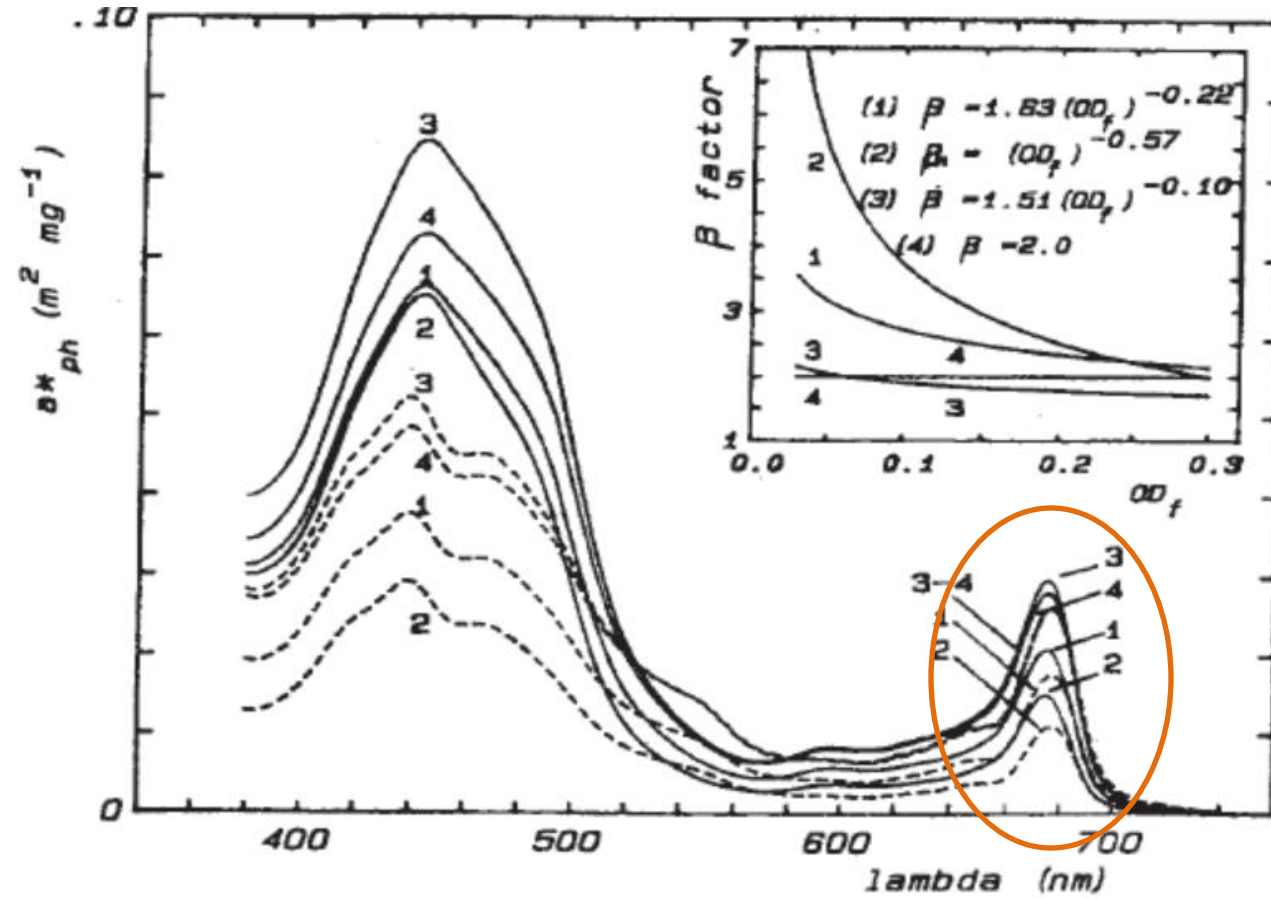
Two bands

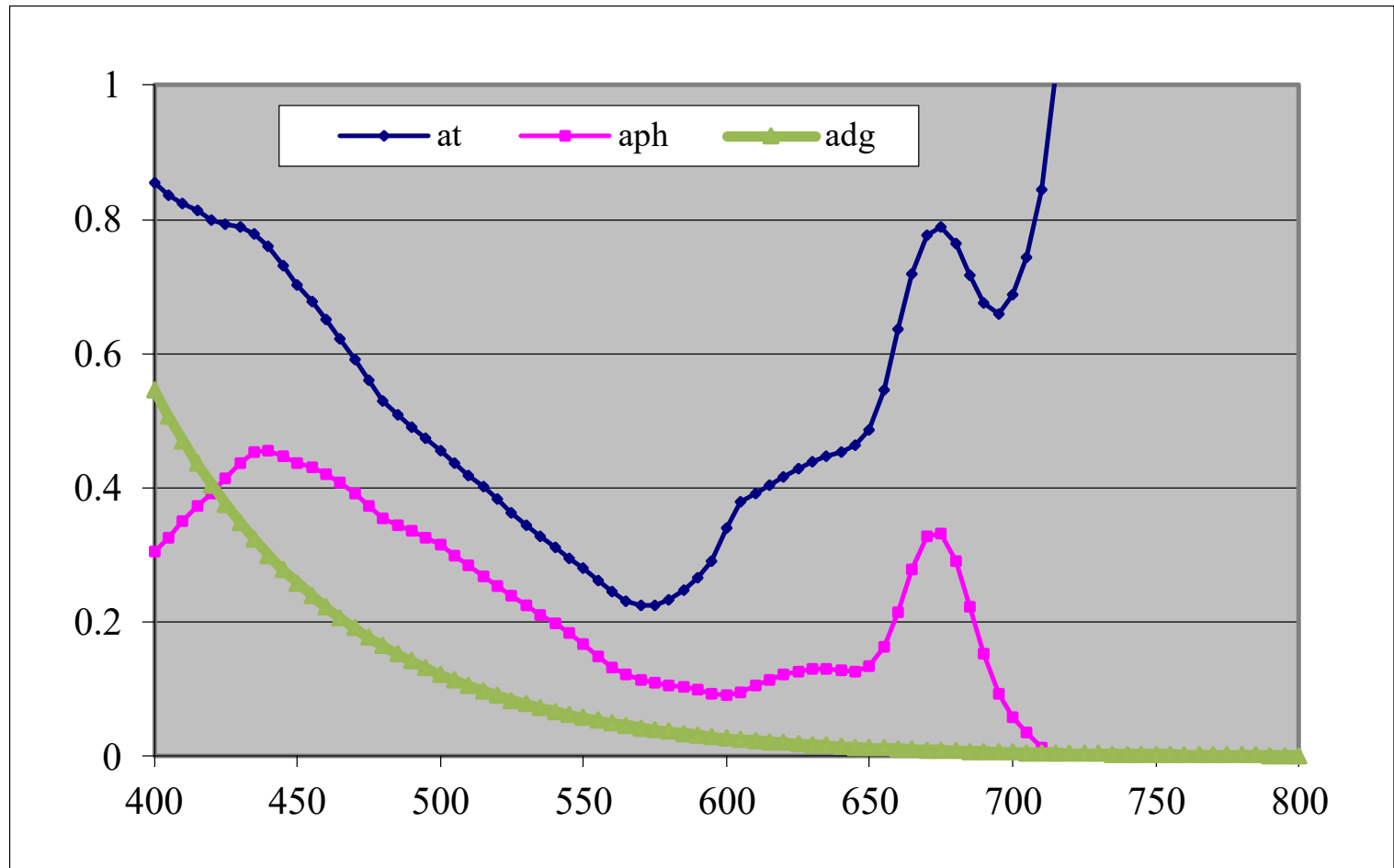
$$Chl = f\left(\frac{Rrs(75x)}{Rrs(67x)}\right)$$

Three bands

$$Chl = f\left(\frac{Rrs(75x)}{Rrs(67x)} - \frac{Rrs(75x)}{Rrs(70x)}\right)$$

a_{ph}





$$R_{rs}(\lambda) = G \frac{b_{bw}(\lambda) + M_3 \langle b_{bp}(\lambda) \rangle}{a_w(\lambda) + M_1 \langle a_{ph}(\lambda) \rangle + M_2 \langle a_{dg}(\lambda) \rangle + b_{bw}(\lambda) + M_3 \langle b_{bp}(\lambda) \rangle}$$

$$R_{rs}(\lambda) \approx G \frac{M_3 \langle b_{bp}(\lambda) \rangle}{a_w(\lambda) + M_1 \langle a_{ph}(\lambda) \rangle}$$

$$\frac{R_{rs}(\lambda_{red1})}{R_{rs}(\lambda_{red2})} = \frac{\langle b_{bp}(\lambda_{red1}) \rangle}{\langle b_{bp}(\lambda_{red2}) \rangle} \frac{a_w(\lambda_{red2}) + M_1 \langle a_{ph}(\lambda_{red2}) \rangle}{a_w(\lambda_{red1}) + M_1 \langle a_{ph}(\lambda_{red1}) \rangle}$$

Proper contrast of Rrs at λ_1 and λ_2 then leads to M_1 .

2. Top-down strategy (TDS):

$$R_{rs} = G \frac{b_b}{a + b_b}$$

$$R_{rs} \rightarrow b_b \& a \rightarrow a_x$$



Clarity (Secchi depth, light depth, SPM, etc)

Remote sensing measures the *total* effect:

Water clarity (or turbidity) is also a measure of total effect.

Examples of TDS:

Loisel & Stramski (2000), QAA (Lee et al, 2002); Smyth et al (2006); Doran et al (2007).

The Quasi-Analytical Algorithm (QAA)

Forward modeling:

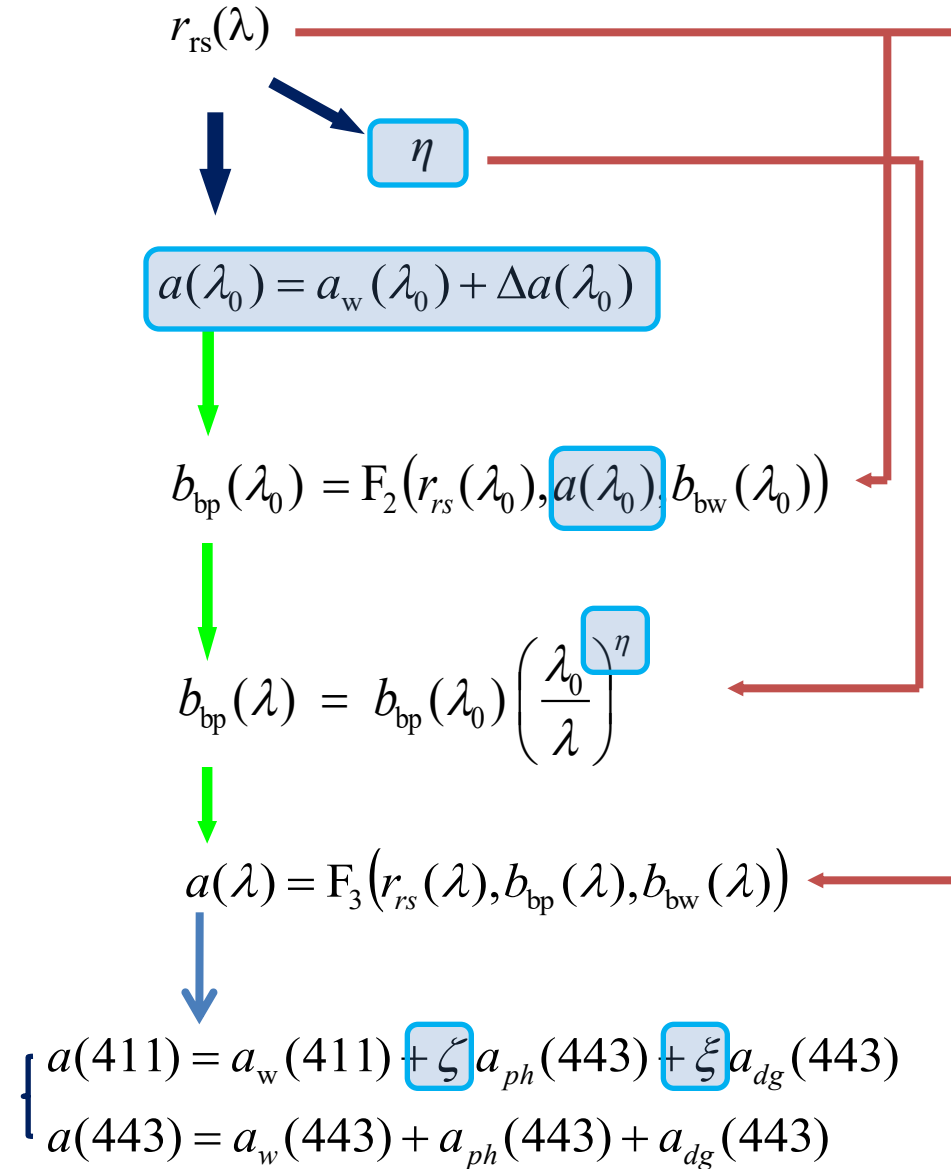
$(a, b_b, \text{etc}) \longrightarrow R_{rs}$

$$R_{rs} \approx 0.05 \frac{b_b}{a + b_b}$$

QAA:

$(a, b_b) \longleftarrow R_{rs}$

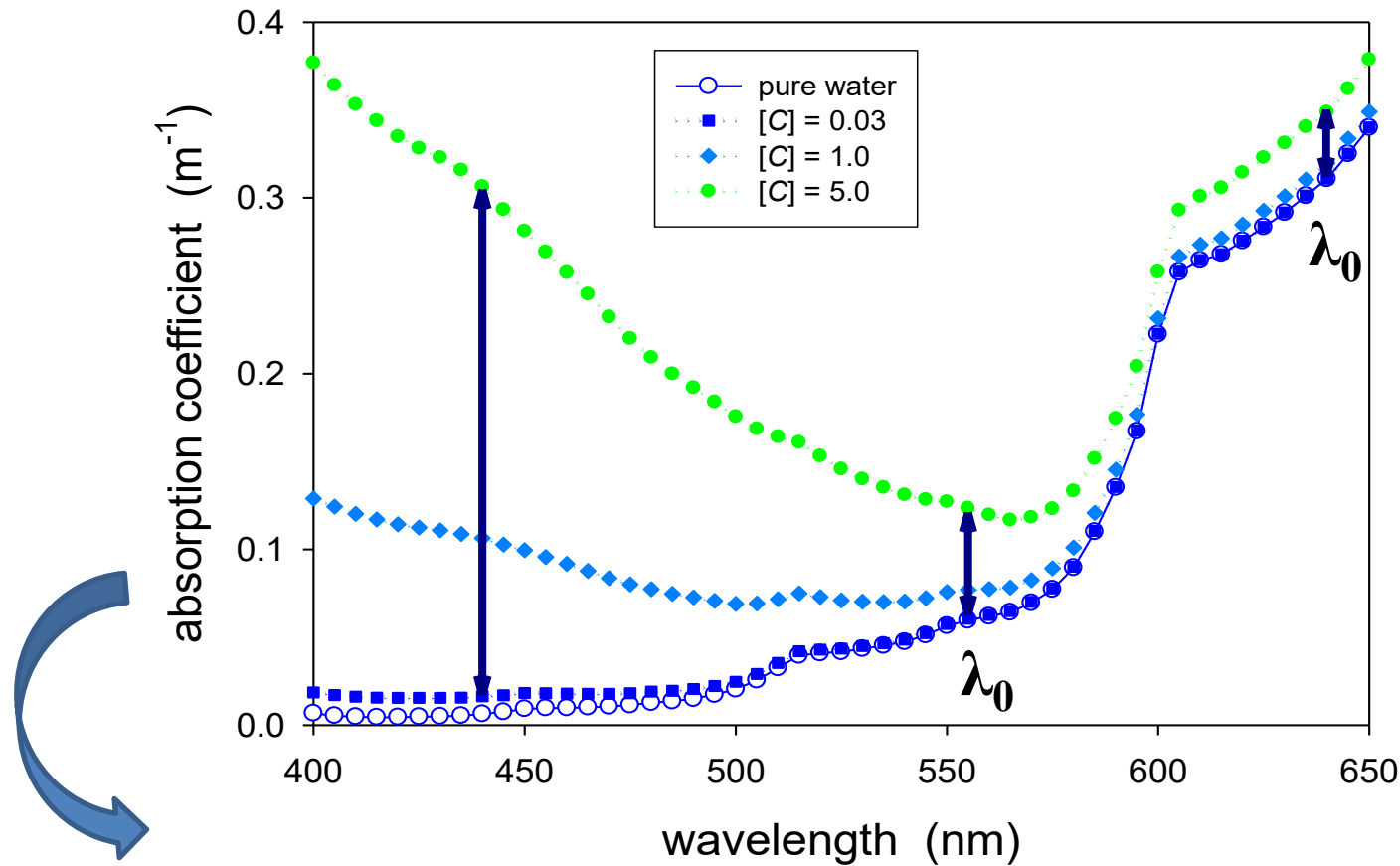
The data flow of QAA:



$$\zeta = \frac{a_{ph}(411)}{a_{ph}(443)}$$

$$\xi = \frac{a_{dg}(411)}{a_{dg}(443)}$$

Logic behind QAA (and its updated versions):



For a reference wavelength, λ_0 , variation of $a(\lambda_0)$ is limited.

Known $a(\lambda_0)$, enables calculation of $b_b(\lambda_0)$ from $R_{rs}(\lambda_0)$; propagate $b_b(\lambda_0)$ to $b_b(\lambda)$, then enables calculation of $a(\lambda)$ from $R_{rs}(\lambda)$.

No need of spectral model of $a_x(\lambda)$ in this process!

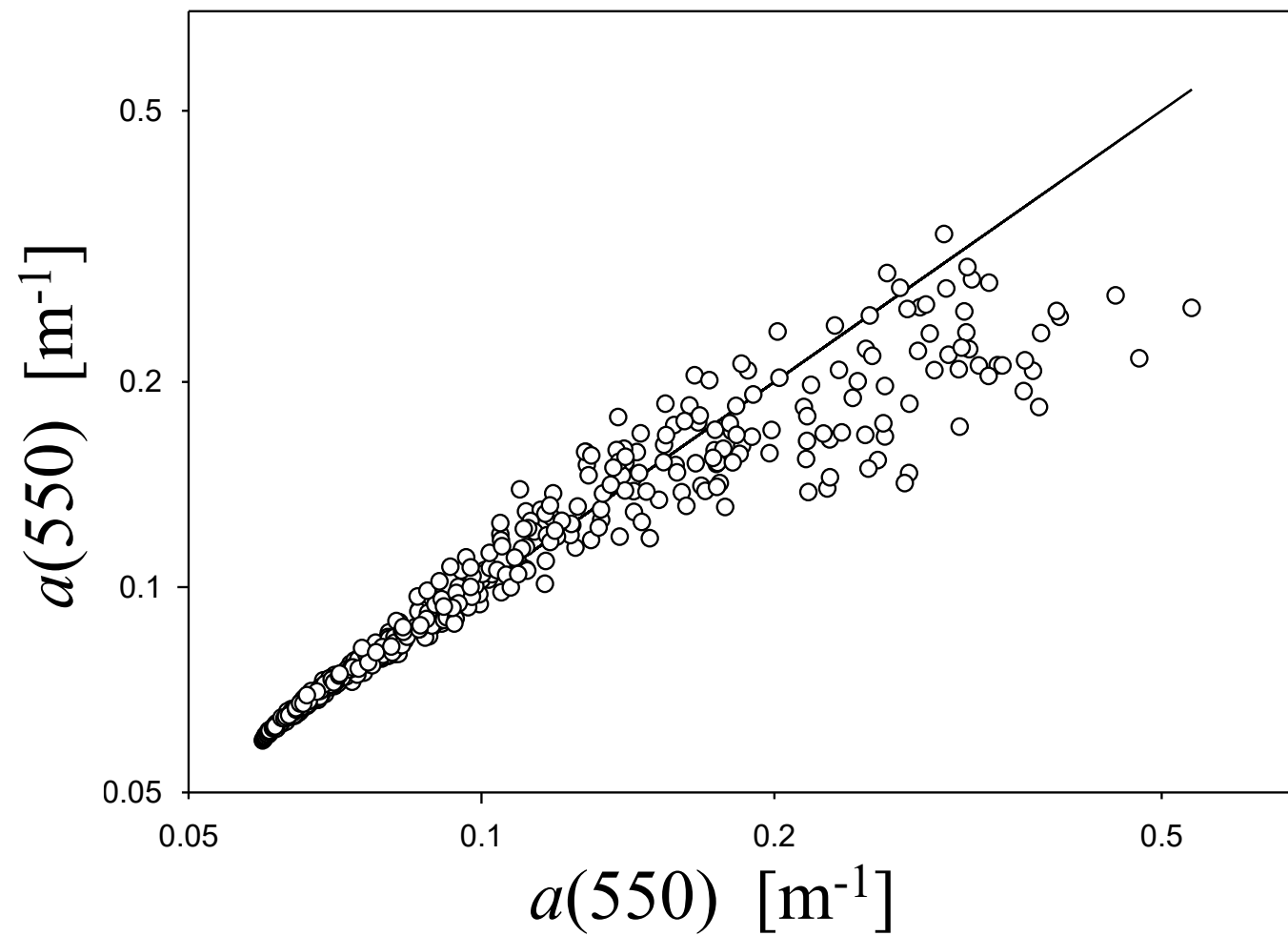
When 550 nm as the reference wavelength (λ_0)

$$a(550) = a_w(550) + 10^{-1.146 - 1.366\chi - 0.469\chi^2}$$

$$\chi = \log \left(\frac{r_{rs}(443) + r_{rs}(490)}{r_{rs}(\lambda_0) + 5 \frac{r_{rs}(667)}{r_{rs}(490)} r_{rs}(667)} \right)$$

$$a_w(550) = 0.0565 \text{ m}^{-1}$$

Empirical!



Invert Rrs:

$$R_{rs} \longrightarrow r_{rs} \longrightarrow \{a \& b_b\}$$

$$r_{rs}(\lambda) = R_{rs}(\lambda) / (0.52 + 1.7 R_{rs}(\lambda))$$

$$r_{rs} = g_0 \left(\frac{b_b}{a + b_b} \right) + g_1 \left(\frac{b_b}{a + b_b} \right)^2 \quad g_0=0.089, g_1=0.125$$

$$u(\lambda) = \frac{b_b(\lambda)}{a(\lambda) + b_b(\lambda)} = \frac{-g_0 + \sqrt{(g_0)^2 + 4 g_1 * r_{rs}(\lambda)}}{2 g_1}$$

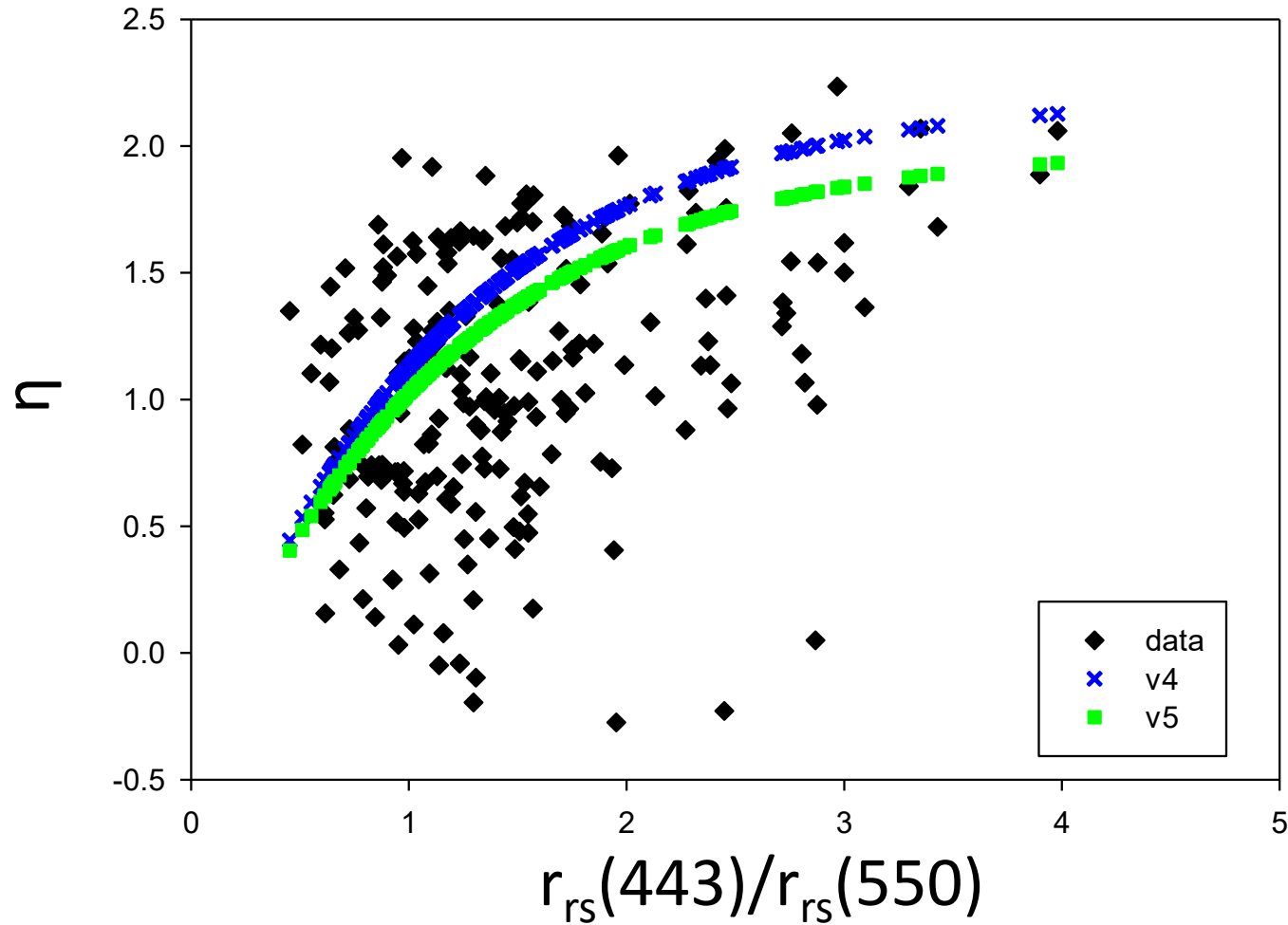
$$a(550) = a_w(550) + 10^{-1.146 - 1.366 \chi - 0.469 \chi^2}$$

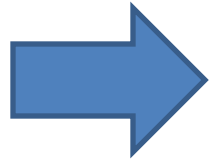
$$\Rightarrow b_{bp}(550) = \frac{u(550) a(550)}{1 - u(550)} - b_{bw}(550)$$

$$b_{bp}(\lambda) = b_{bp}(550) \left(\frac{550}{\lambda} \right)^{\eta}$$

Empirical:

$$\eta = 2.0 \left(1 - 1.2 \exp \left(-0.9 \frac{r_{rs}(443)}{r_{rs}(550)} \right) \right)$$





$$b_b(\lambda) = b_{bw}(\lambda) + b_{bp}(\lambda)$$



$$a(\lambda) = \frac{(1 - u(\lambda)) b_b(\lambda)}{u(\lambda)}$$

$$a(\lambda) = a_w(\lambda) + a_{ph}(\lambda) + a_{dg}(\lambda)$$



$$\begin{cases} a(410) = a_w(410) + a_{ph}(410) + a_{dg}(410), \\ a(440) = a_w(440) + a_{ph}(440) + a_{dg}(440). \end{cases}$$

$$\zeta = \frac{a_{ph}(410)}{a_{ph}(440)}$$



$$\xi = \frac{a_{dg}(410)}{a_{dg}(440)}$$

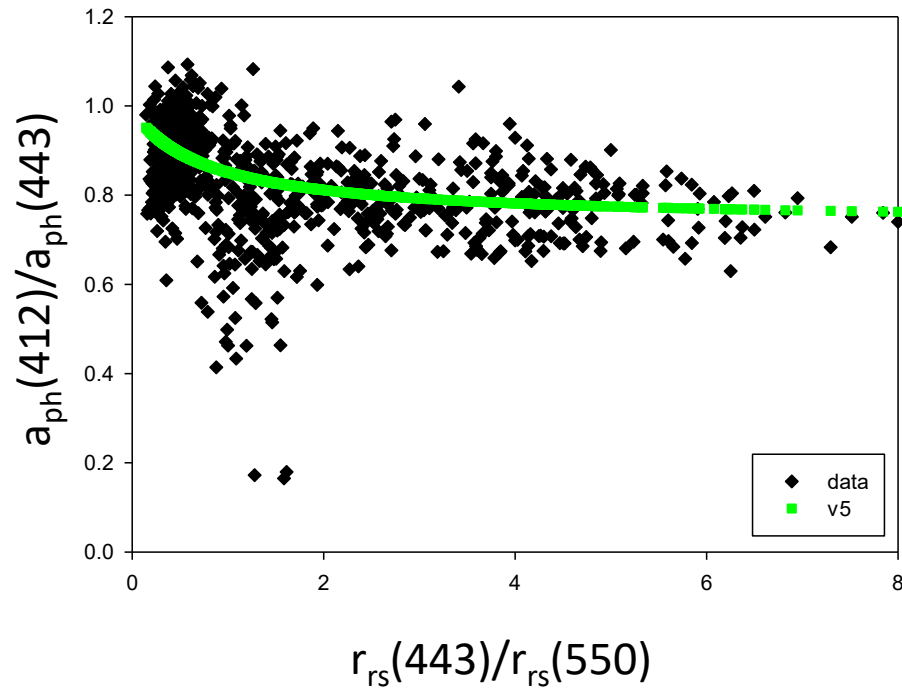
$$\begin{cases} a(410) = a_w(410) + \zeta a_{ph}(440) + \xi a_{dg}(440), \\ a(440) = a_w(440) + a_{ph}(440) + a_{dg}(440). \end{cases}$$



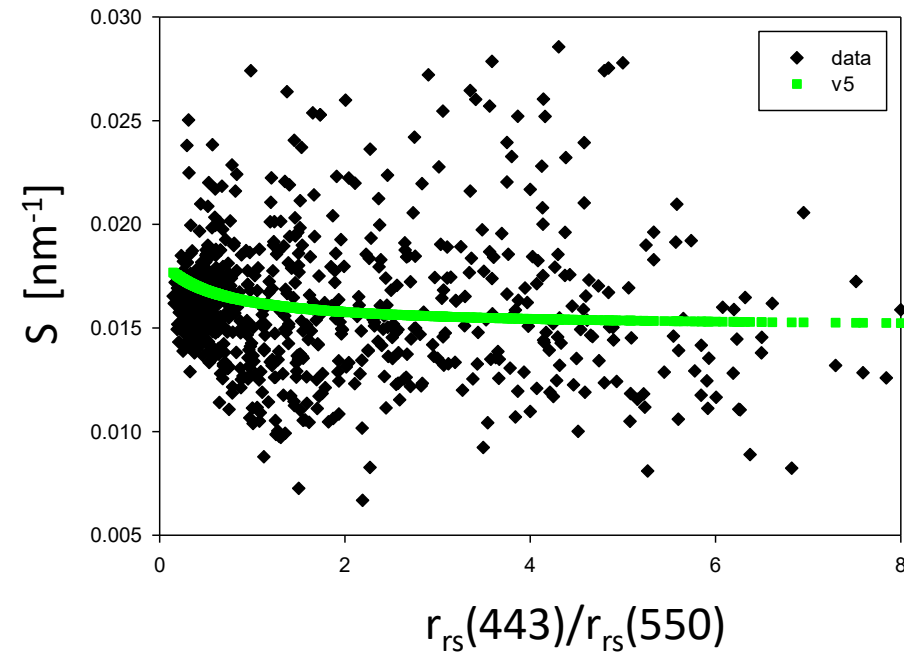
$$\begin{cases} a(410) = a_w(410) + \zeta a_{ph}(440) + \xi a_{dg}(440), \\ a(440) = a_w(440) + a_{ph}(440) + a_{dg}(440). \end{cases}$$



$$\begin{cases} a_g(440) = \frac{(a(410) - \zeta a(440)) - (a_w(410) - \zeta a_w(440))}{\xi - \zeta}, \\ a_{ph}(440) = a(440) - a_w(440) - a_{dg}(440). \end{cases}$$



$$\zeta = 0.74 + \frac{0.2}{0.8 + r_{rs}(443)/r_{rs}(550)}$$



$$\xi = e^{S(443-411)},$$

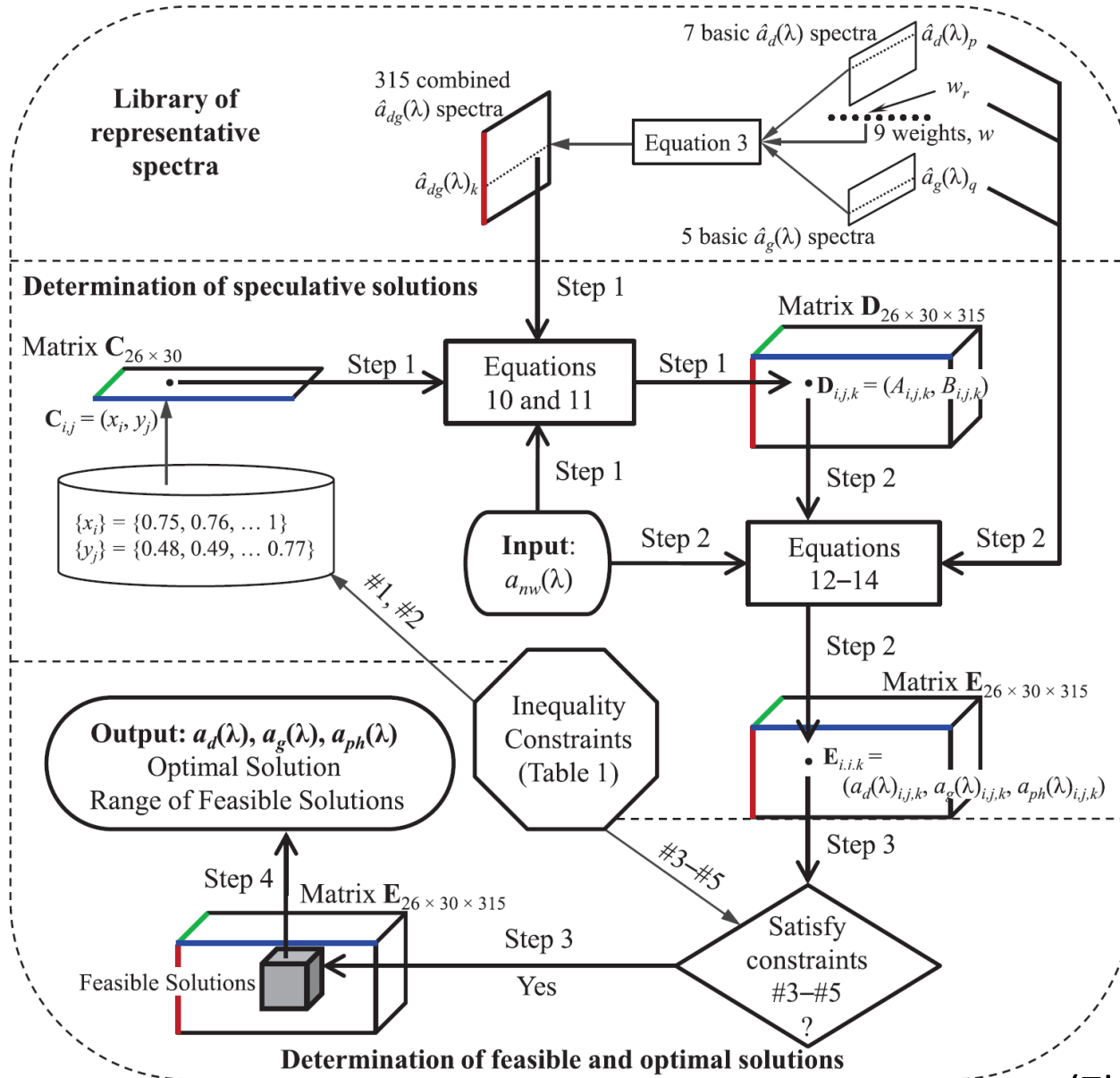
$$S = 0.015 + \frac{0.002}{0.6 + r_{rs}(443)/r_{rs}(550)}$$

Empirical!

Ensemble solutions:

Wang et al. 2006; Zheng et al. 2015

$$a(\lambda) = a_w(\lambda) + M_1 \langle a_{ph}(\lambda) \rangle + M_2 \langle a_{dg}(\lambda) \rangle$$



(Zheng et al. 2015)

What is band-ratio derived [Chl]?

$$[Chl] = f_1 \left(R_{rs}(\lambda_i) / R_{rs}(\lambda_j) \right)$$

$$R_{rs}(\lambda_i) / R_{rs}(\lambda_j) = f_2 \left(\frac{b_{bw}(\lambda_i) + b_{bp}(\lambda_i)}{b_{bw}(\lambda_j) + b_{bp}(\lambda_j)} \frac{a_w(\lambda_j) + a_{ph}(\lambda_j) + a_{dg}(\lambda_j)}{a_w(\lambda_i) + a_{ph}(\lambda_i) + a_{dg}(\lambda_i)} \right)$$

[Chl] is actually an IOP product

Key Points:

1. Various inversion algorithms for IOPs have been developed; but more/better ones are also expected.
2. BUS derives every component first, then (simultaneously) derives the total optical property.

Assume the spectral shapes of the optically active components are well characterized!

BUS relies more on the accuracy of forward bio-optical model.

3. TDS derives total first, then decompose to separate components.

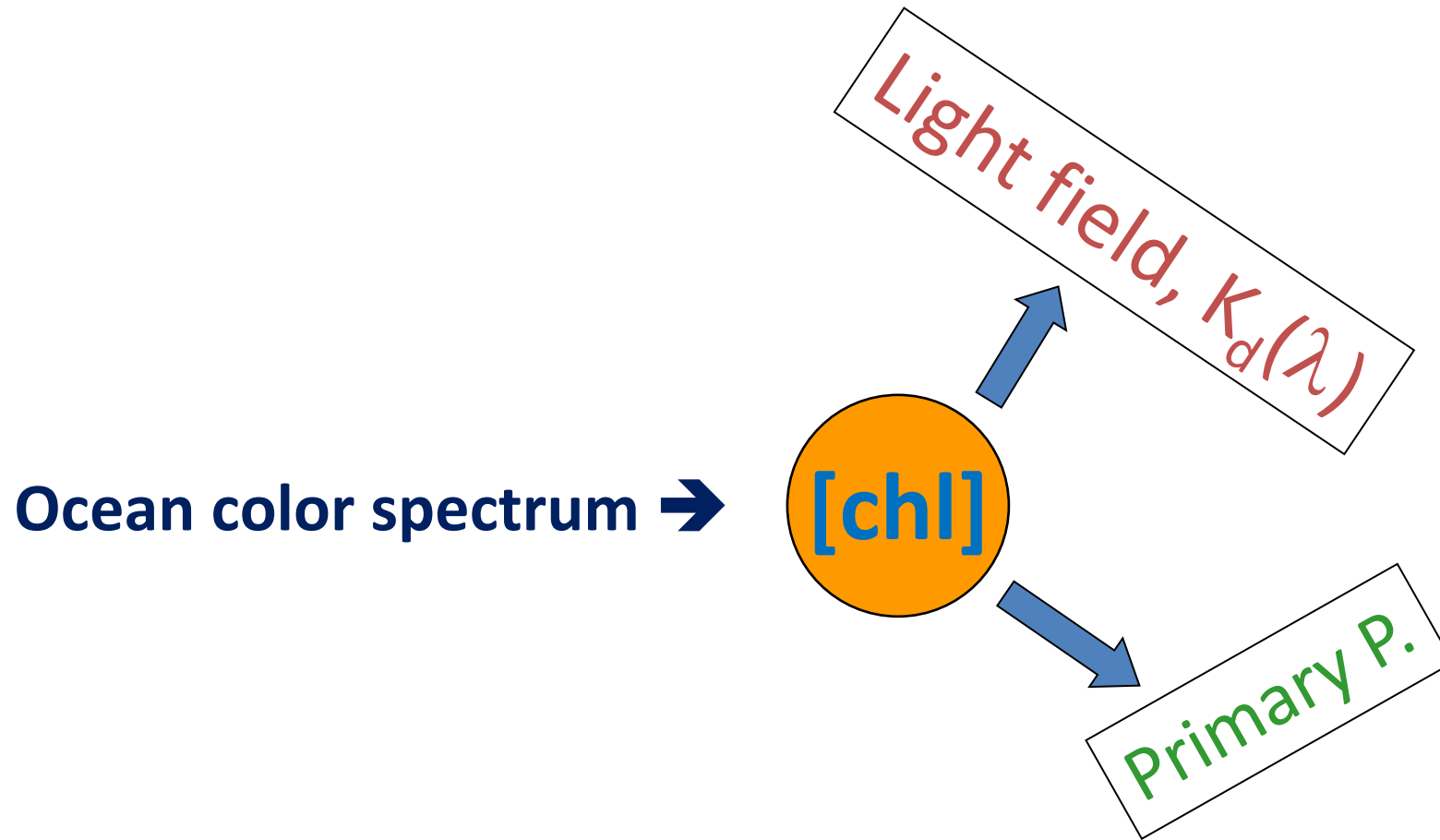
TDS relies more on the accuracy of Rrs measurement.

II. Applications of inverted IOPs

$Rrs(\lambda)$  IOPs

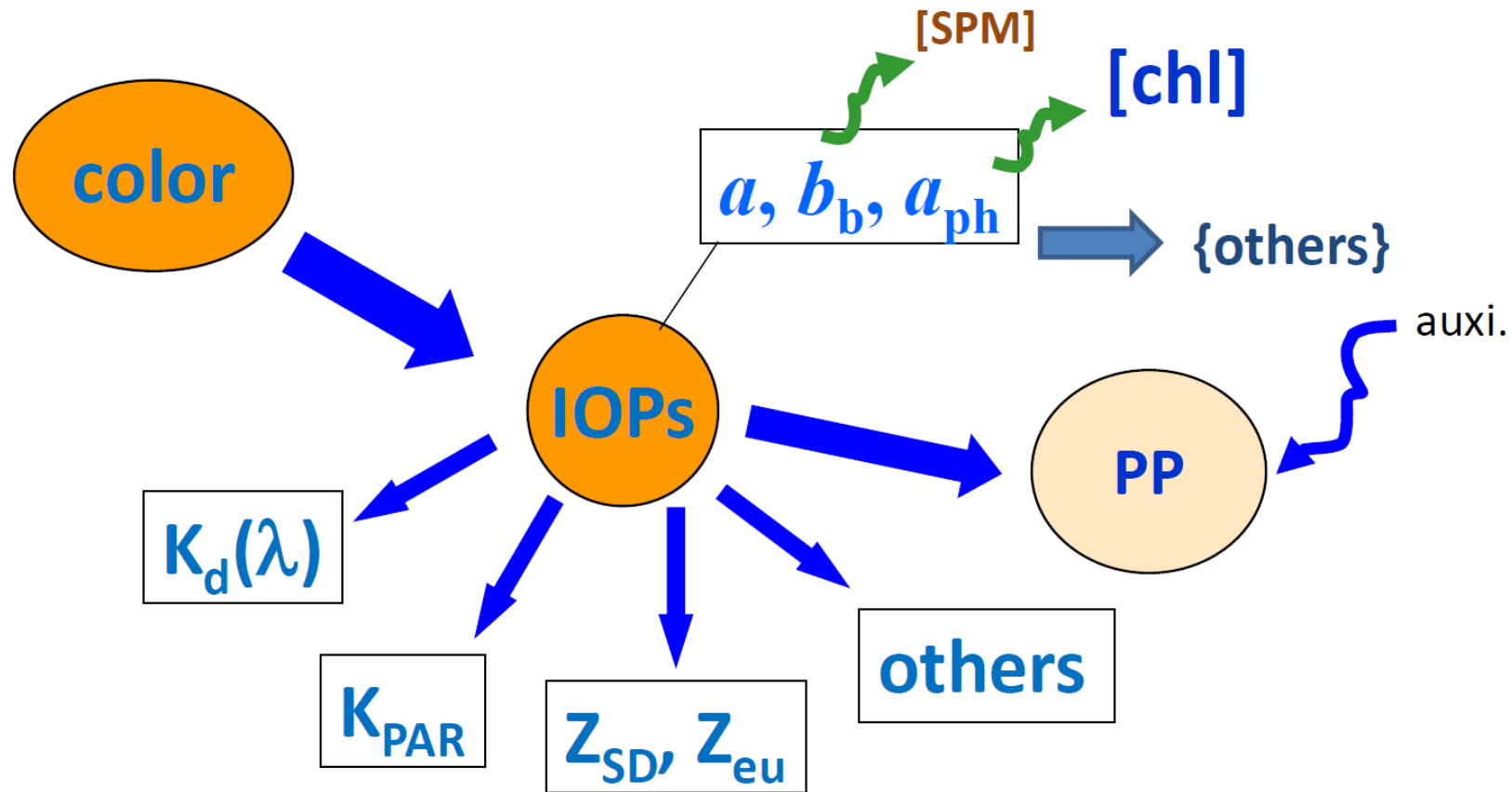
What to do with the retrieved IOPs?

Traditional strategy: [chl] centered system



Works for waters where IOPs co-vary with [Chl].

Application examples of IOP products



No division of “Case-1” vs “Case-2” waters.

1. Estimation of diffuse attenuation coefficient ($K_d(\lambda)$)
2. Estimation of $K_d(\text{PAR})$ and euphotic-zone depth
3. Estimation of water clarity (Secchi disk depth)
4. Estimation of primary production
5. A few other examples

1. Estimation of diffuse attenuation coefficient ($K_d(\lambda)$)

Traditionally,

$$K_d(490) = A \left(\frac{L_w(\lambda_{blue})}{L_w(\lambda_{green})} \right)^B$$

Austin and Petzold (1981)

Or,

$$K_d(\lambda, [Chl]) = K_w(\lambda) + \chi(\lambda)[Chl]^{e(\lambda)} \quad (2)$$

(Morel and Maritorena 2001)

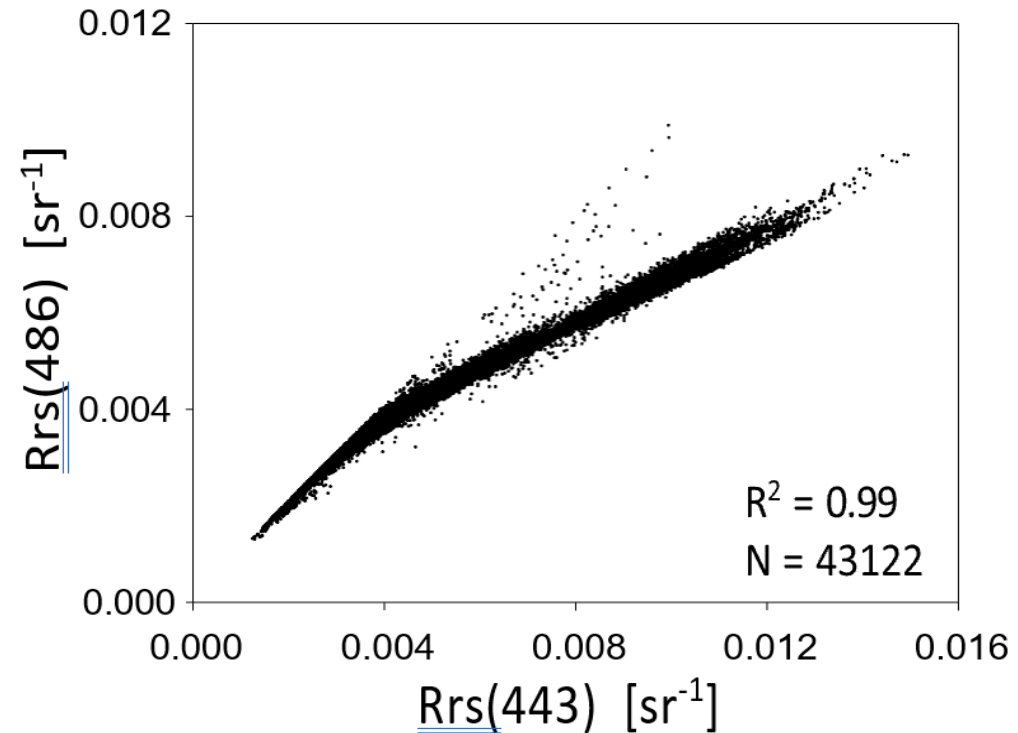
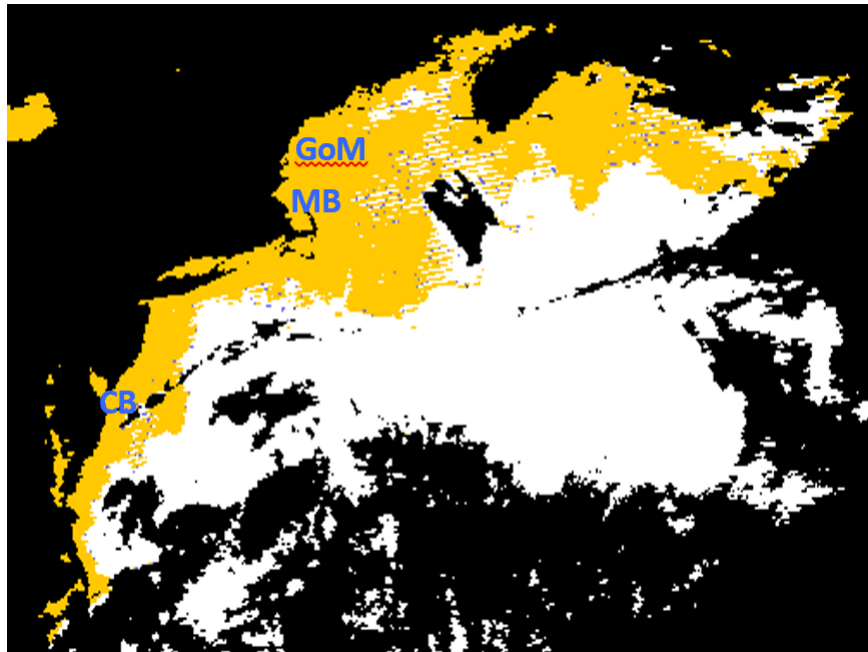
For “Case-1” waters

$$\log_{10}(K_{bio}(490)) = a_0 + \sum_{i=1}^4 a_i \log_{10}\left(\frac{R_{rs}(\lambda_{blue})}{R_{rs}(\lambda_{green})}\right)$$

$$Kd_{490} = K_{bio}(490) + 0.0166$$

$$\log_{10}(chlor_a) = a_0 + \sum_{i=1}^4 a_i \log_{10}\left(\frac{R_{rs}(\lambda_{blue})}{R_{rs}(\lambda_{green})}\right)^i,$$

$$Rrs(\lambda_{blue}) = Rrs(443) > Rrs(486)$$



The standard $K_d(490)$ and Chl products are 100% co-vary in coastal waters; further

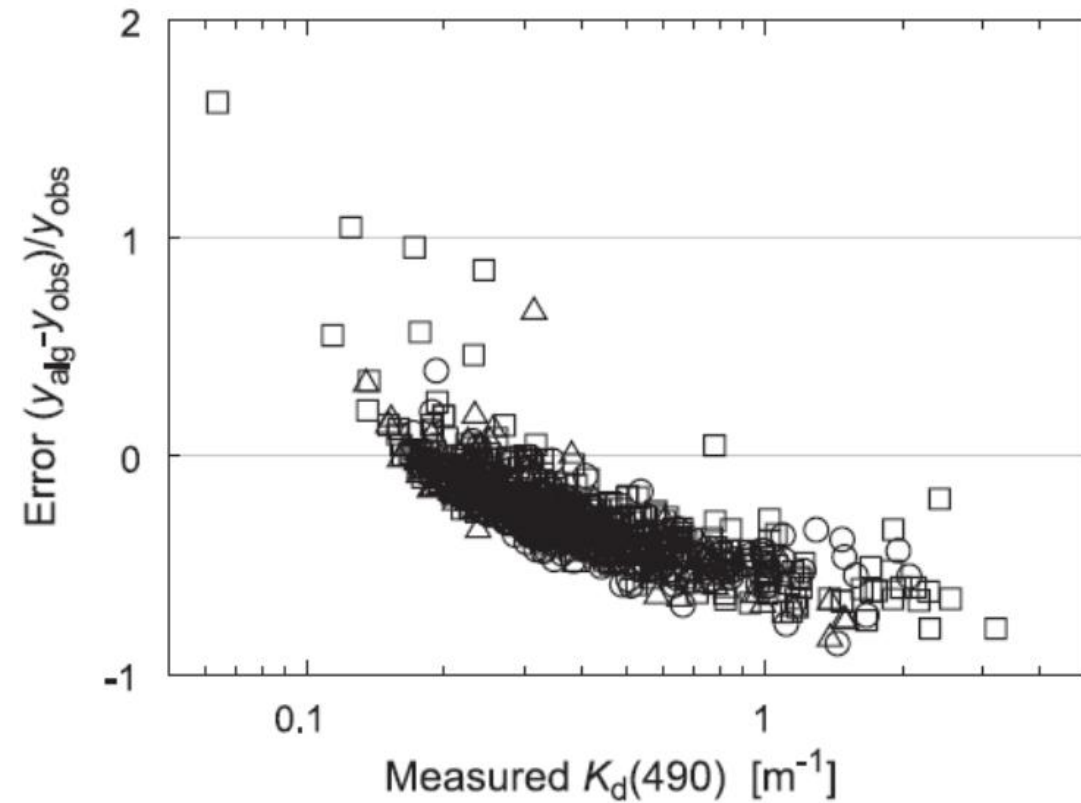
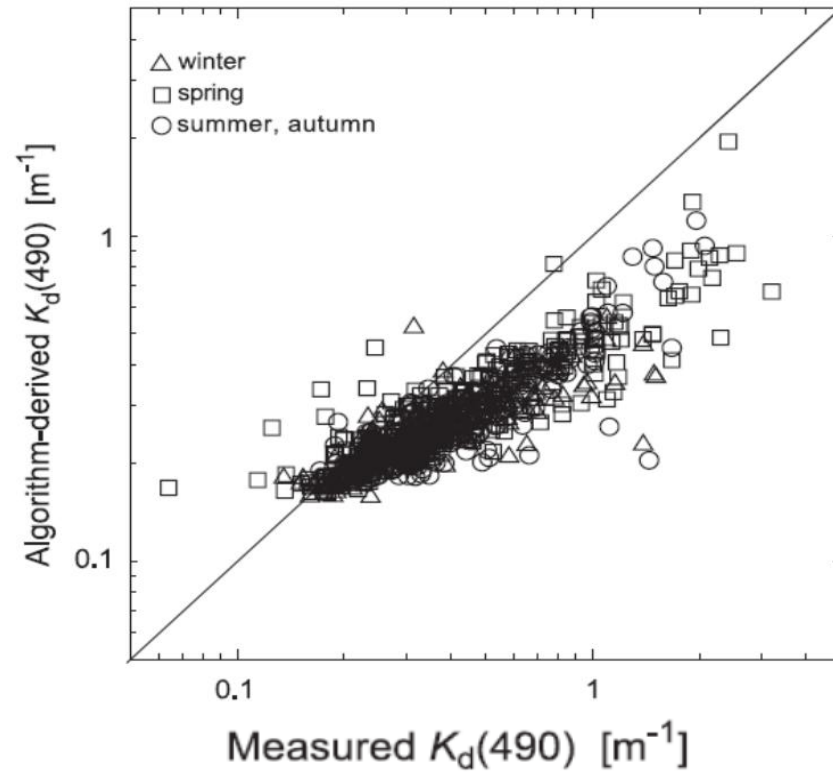
$$K_d(490) = Fun\left(\frac{R_{rs}(490)}{R_{rs}(555)}\right)$$

AOP: sun angle dependent

Nearly independent of sun angle.

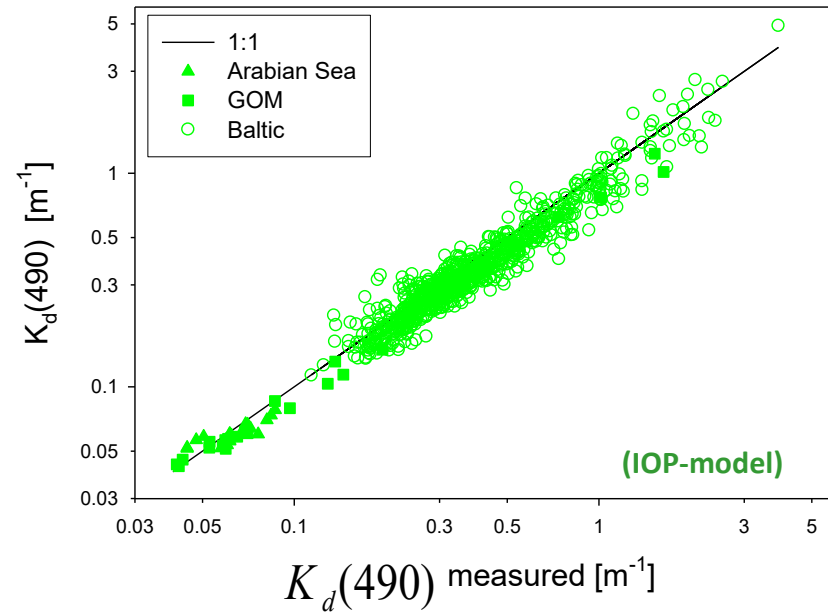
The two sides do **not** match in optical nature.

In addition, ratio-derived K_d has large uncertainties or errors in coastal waters.



(Darecki and Stramisk, 2004)

IOPs-based system:



**Oceanic &
Coastal waters**

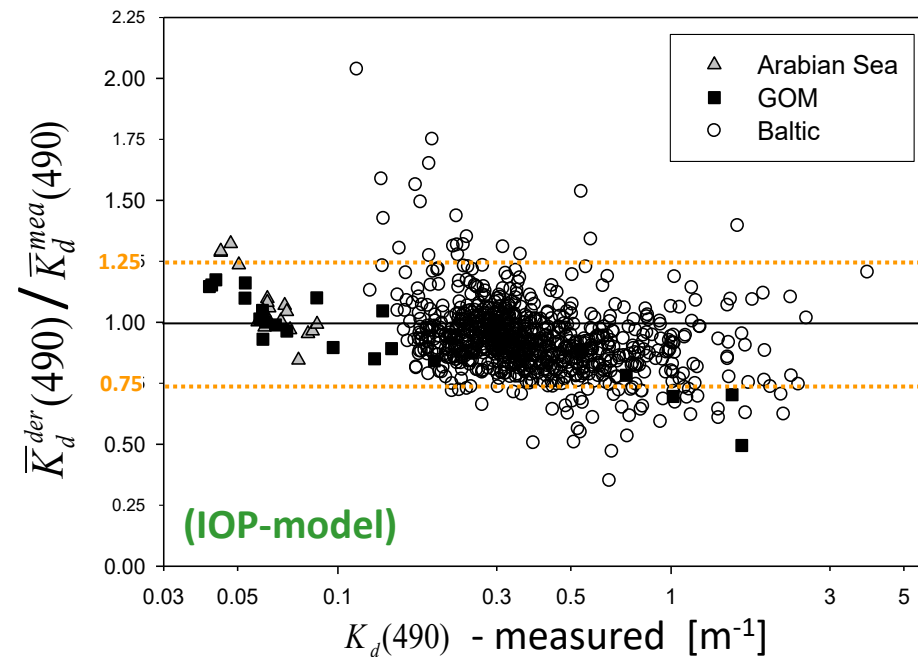
(Lee et al. 2005)

$$K_d = m_0 a + v b_b$$

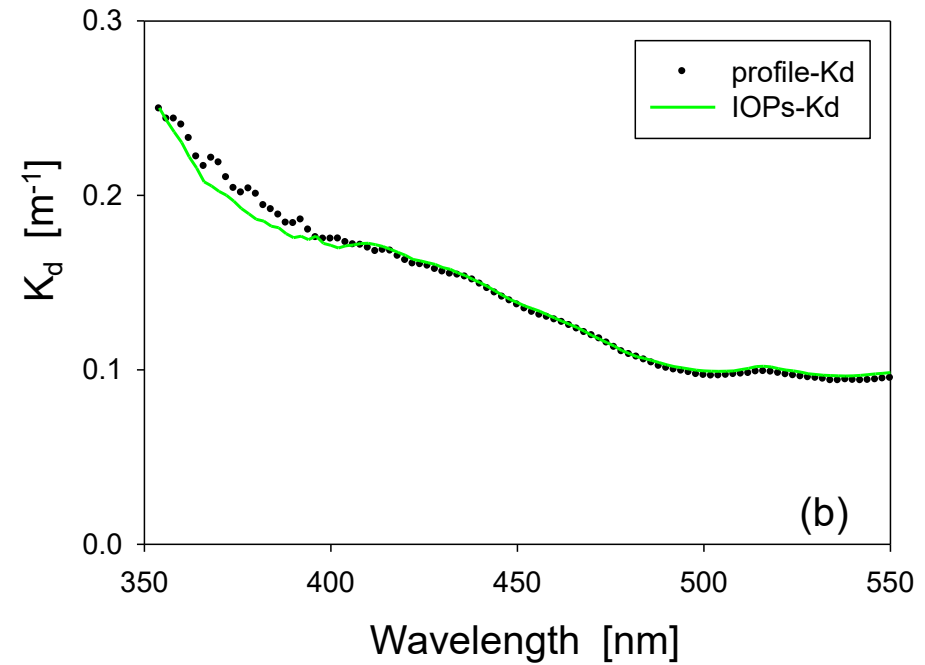
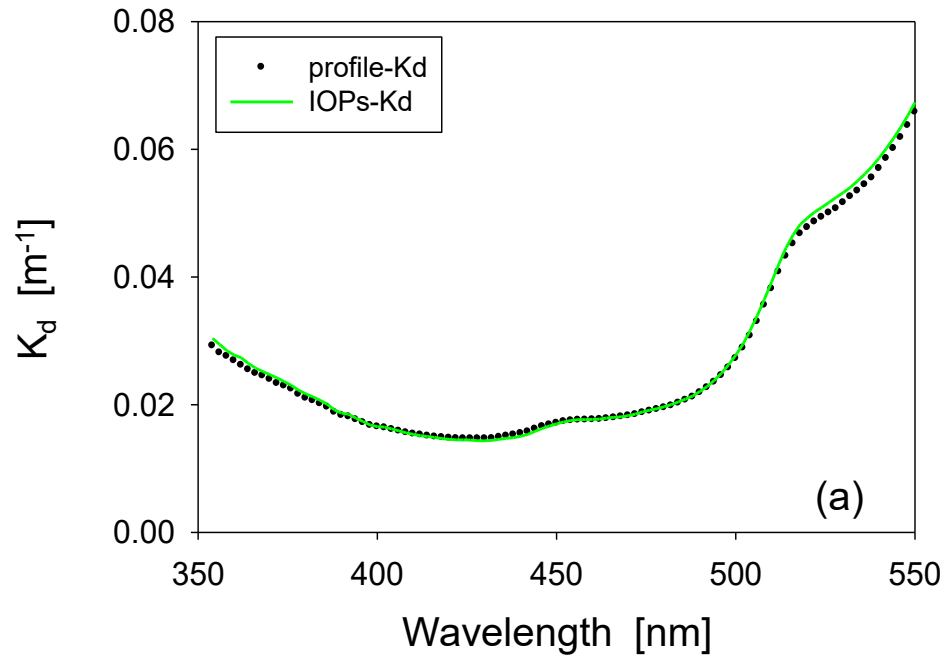
$$v = m_1(1 - m_2 e^{-m_3 a})$$

($m_{0,1,2}$ are wavelength independent)

No division of “Case 1” vs “Case 2” waters.



hyperspectral



(Lee et al. 2013)

Through a semi-analytical system, a K_d spectrum, not at a single band, can be derived.

2. Estimation of K_{PAR} and euphotic depth

$$PAR(z) = PAR(0) e^{-K_{PAR} z}$$

$$K_{PAR} = K_w + k_c C + K_x$$

Good for earlier days,
Not so good for the 21st century

hence of K_{PAR} .

1. K_w is a value averaged over the whole spectrum. It is computed for a layer extending from zero to a certain depth Z within an ideally optically pure ocean. When computing this depth-averaged value, denoted $\bar{K}_w(0, Z)$, the spectral distribution of the light at the surface, $E_0(\lambda)$, and at the depth Z , $E_z(\lambda)$, intervenes according to

$$\bar{K}_w(0, Z) = -Z^{-1} \log \left\{ \frac{\int_{400}^{700} E_0(\lambda) \exp [-K_w(\lambda) Z] d\lambda}{\int_{400}^{700} E_0(\lambda) d\lambda} \right\} \quad (7)$$

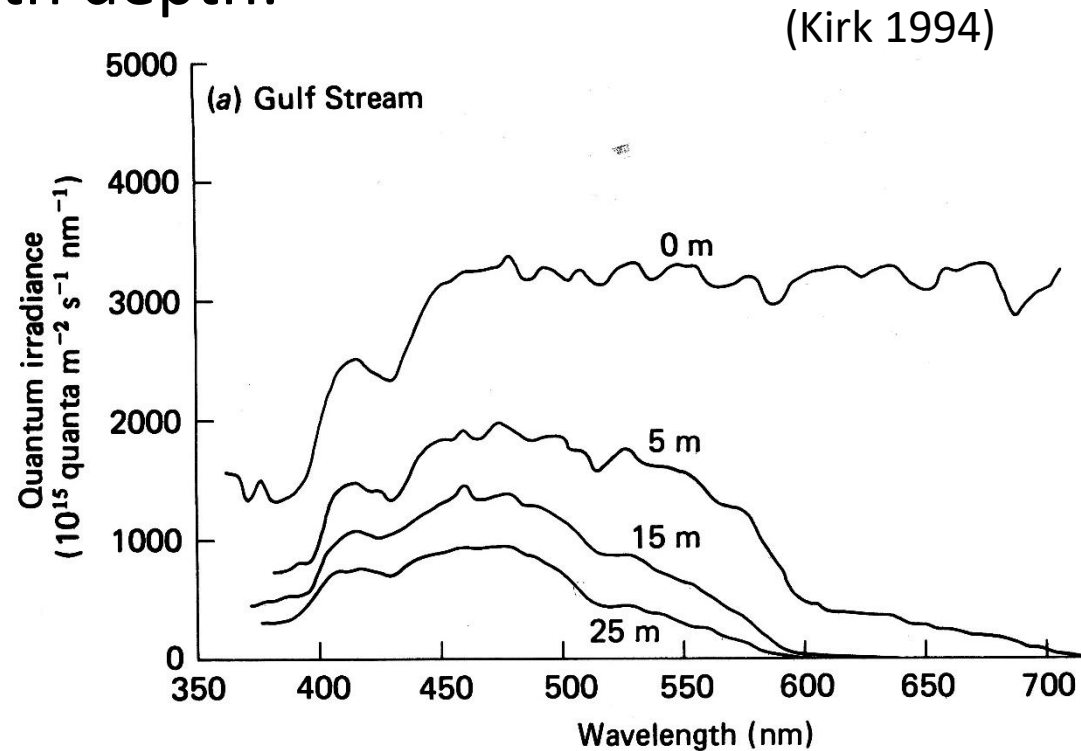
In other words, $\bar{K}_w(0, Z)$ is no longer a constant as soon as it is computed for a layer of variable thickness. When Z increases, the remnant light tends to become monochromatic, with the irradiance maximum centered on the minimum of K_w , and the averaged value $\bar{K}_w(0, Z)$ decreases accordingly (see Figure 4; $E_0(\lambda)$ is taken from Figure 8).

2. The constant coefficient k_c is also a doubly averaged value, over the spectrum and over the layer considered. The result of such averaging depends on the spectral composition of the underwater light and on its change with depth. Since the phytoplankton concentration depicted by C governs both

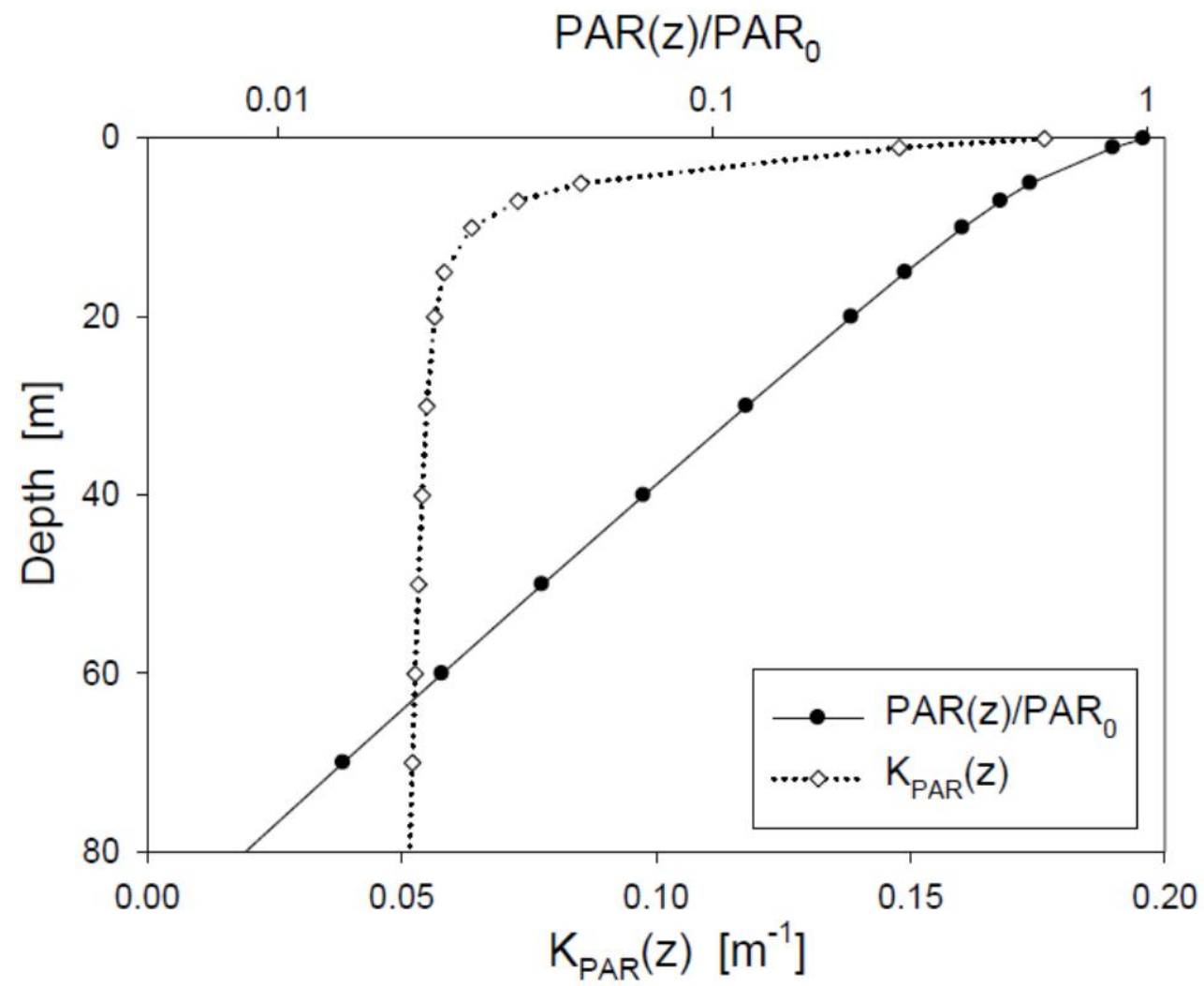
$$K_{PAR} = \frac{-1}{z} \ln \left(\frac{PAR(z)}{PAR(0)} \right) \quad PAR(z) = \int_{400}^{700} E_0(\lambda, 0) e^{-K(\lambda, z)z} d\lambda$$

K_{PAR} is light-quality weighted.

Change of light with depth:



➔ Light at deeper depth is associated with lower attenuation coefficient



$$PAR(z) = PAR(0) e^{-K_{par}(z) z}$$

$$K_{PAR}(z) \approx K_1 + \frac{K_2}{(1+z)^{0.5}}$$

$$K_1 = f_1(a(490), b_b(490)) \quad K_2 = f_2(a(490), b_b(490))$$

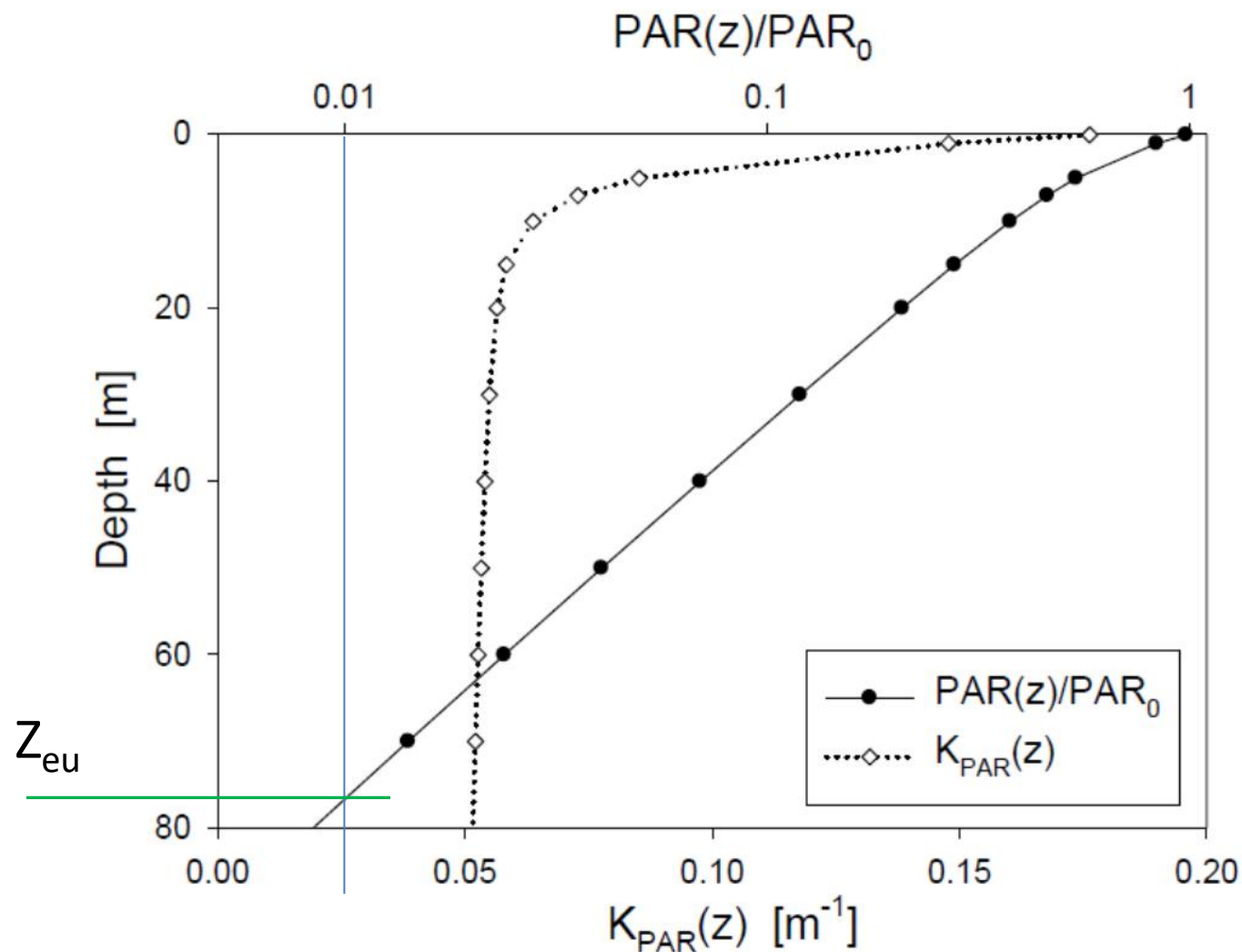
Key:

K_{PAR} varies with depth, especially in the upper water column!

Euphotic depth (z_{eu}), based on 1% definition:

$$z_{eu} = \frac{4.6}{K_{PAR}(z_{eu})}$$

$$\frac{PAR(z_{eu})}{PAR(0)} = 1\% \text{ (or } 0.5\%)$$

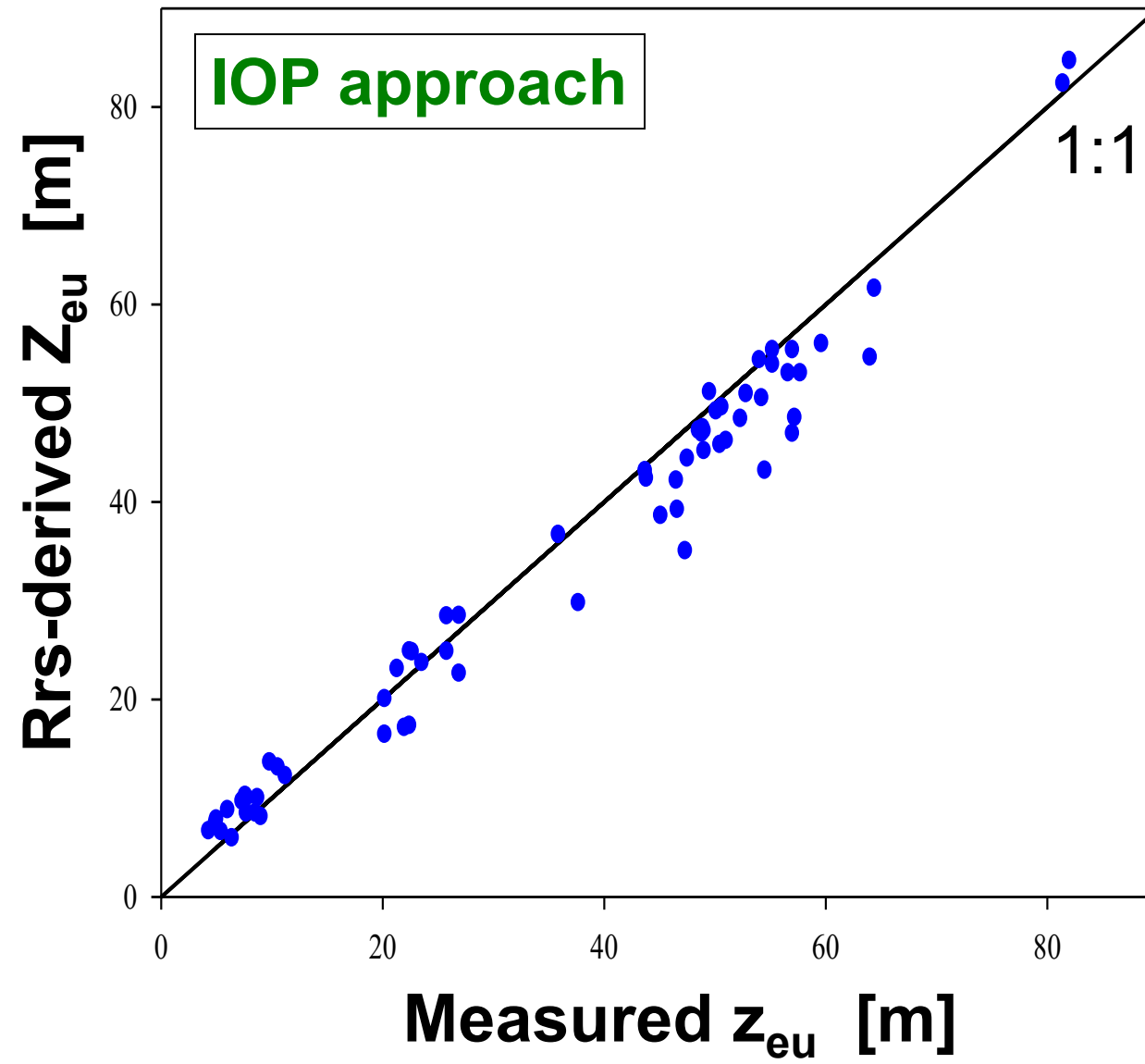




$$\left\{ K_1(a(490) \& b_b(490)) + \frac{K_2(a(490) \& b_b(490))}{(1+z_{eu})^{0.5}} \right\} z_{eu} = 4.6$$

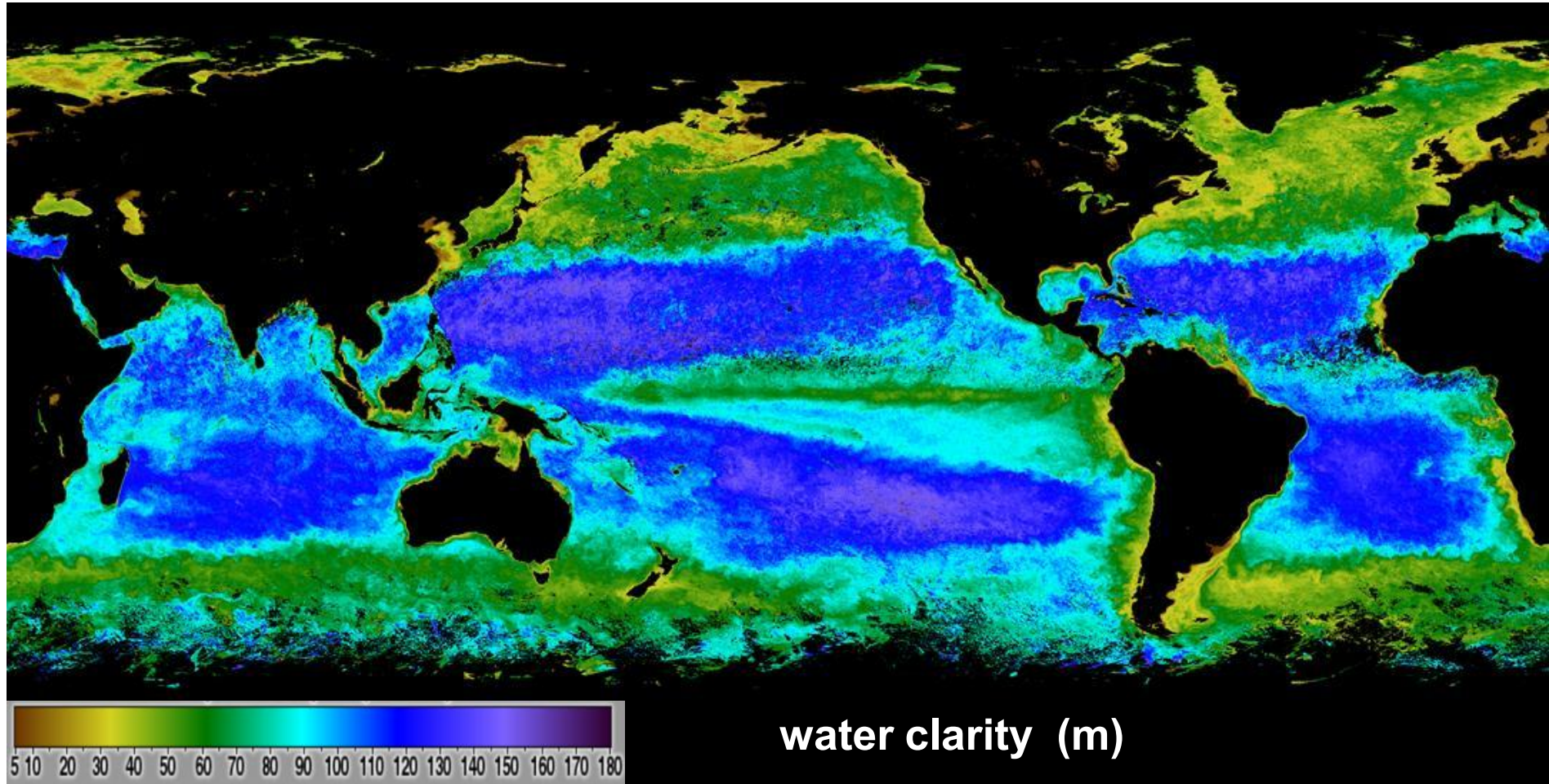
(or 5.3 if defined as 0.5%)

$$R_{rs}(\lambda) \rightarrow a(\lambda) \& b_b(\lambda) \rightarrow K_{PAR}(z) \rightarrow z_{eu}$$



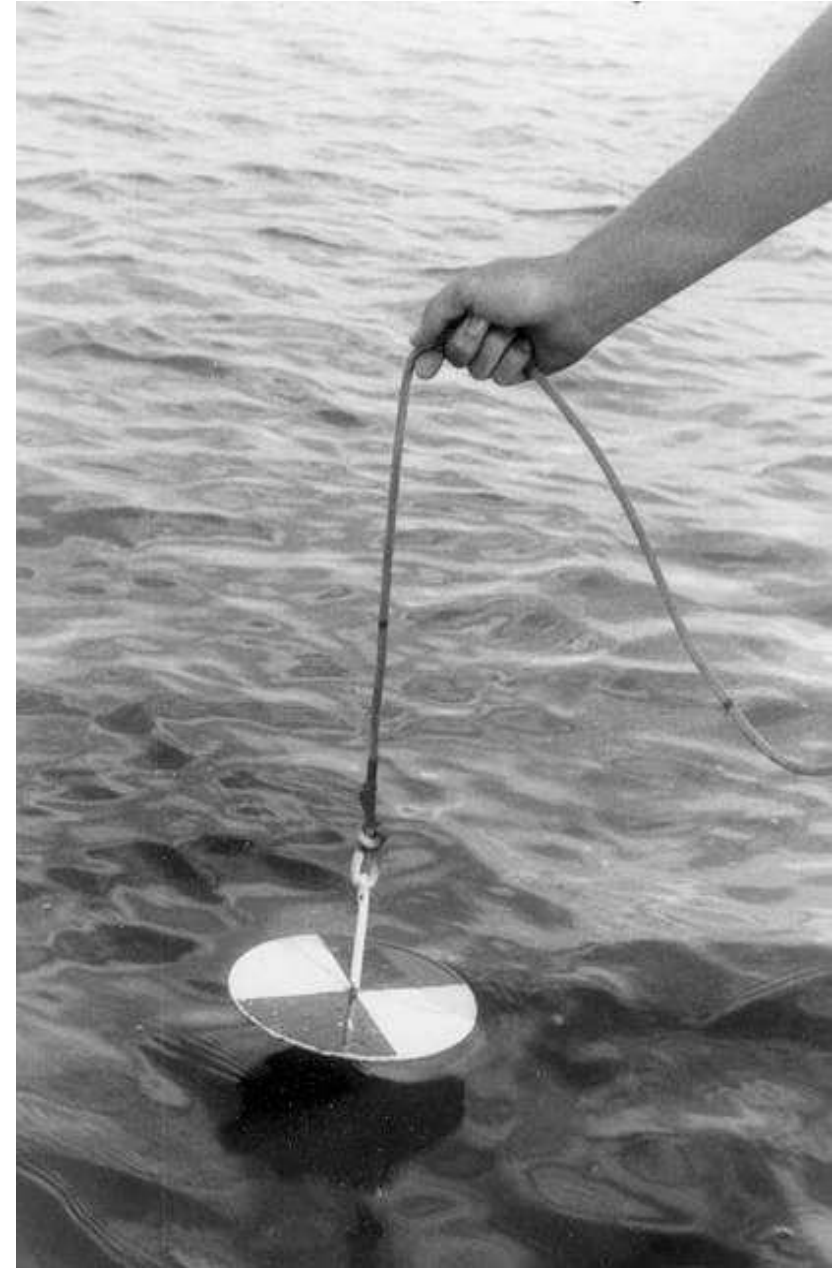
(Lee et al 2007)

Global distribution of Z_{eu}



3. Estimation of water clarity (Secchi disk depth)

Water clarity



Empirical relationships for Z_{SD} derived from measurements:

Formula	Z_{SD} range (m)	Reference
$Z_{SD} = 1.7/K_{PAR}$	1.9 - 35	Poole and Atkins (1929)
$Z_{SD} = 1.44/K_{PAR}$	2 - 12	Holmes (1970)
$Z_{SD} = 1.7/K_{PAR}$	0.1 - 35	Idso (1974)
$Z_{SD} = 1.54/K_{PAR}$	6 - 46	Megard and Berman (1989)
$Z_{SD} = 1.27/K_{PAR}$	0.2 – 2.2	Gallegos et al. (1990)
$Z_{SD} = 1.86/K_{PAR}$	2.3 – 14.7	Kolengings et al. (1991)
$Z_{SD}^{1.16} = 1.48/K_{PAR}$	1.2 - 5	Montes-Hugo et al. (2005)
$Z_{SD} = 1.36/K_{PAR}$	0.1 - 42	Lugo-Fernandez (2008)
$Z_{SD}^{0.76} = 2/K_{PAR}$	0.2 - 6	Padial and Thomaz (2008)
$Z_{SD} = 1.8/K_{PAR}$	0.6 – 4.2	Bracchini et al. (2009)
$Z_{SD}^{0.85} = 1.76/K_{PAR}$	1.7 – 7.0	Ficek and Zapadka (2010)
$Z_{SD} = 1.4/K_{PAR}$	0.5 – 2.5	Gallegos et al. (2011)
$Z_{SD} = 1.37/K_{PAR}$	0.1 – 2.4	Zhang et al. (2012)

$$Z_{SD} = (1.4-1.7)/K_{PAR}$$

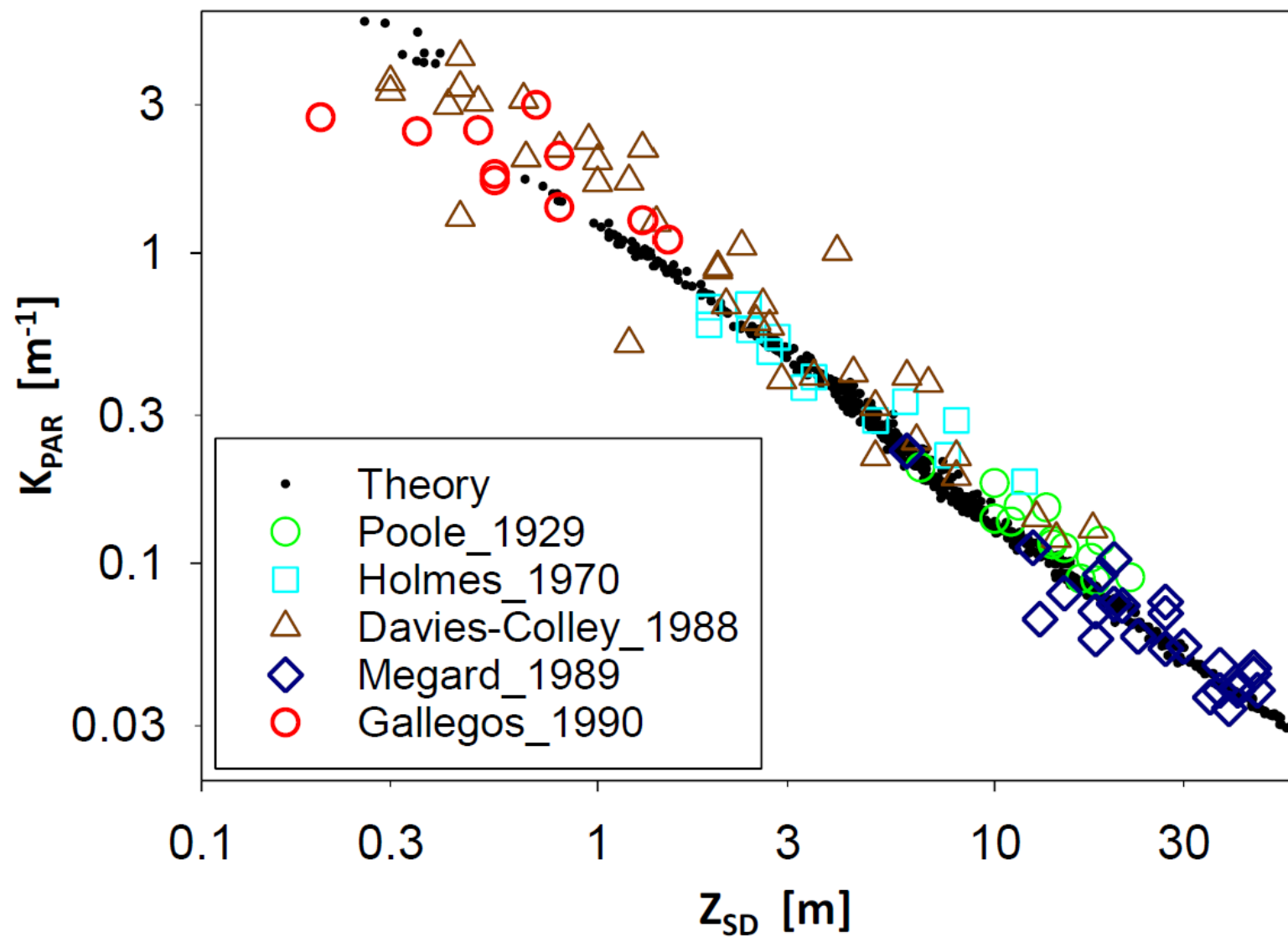
New theoretical relationship for Z_{SD} :

$$Z_{SD} \approx \frac{1}{2.5K_d^{tr}} \ln \left(\frac{|r_T - r_w^{tr}|}{0.013} \right) \quad (\text{Lee et al 2015})$$

K_d^{tr} : attenuation coefficient in the transparent window

$$Z_{SD} \approx \frac{1}{K_d^{tr}} \approx \frac{1.4}{K_{PAR}} \quad (\text{Lee et al 2018})$$

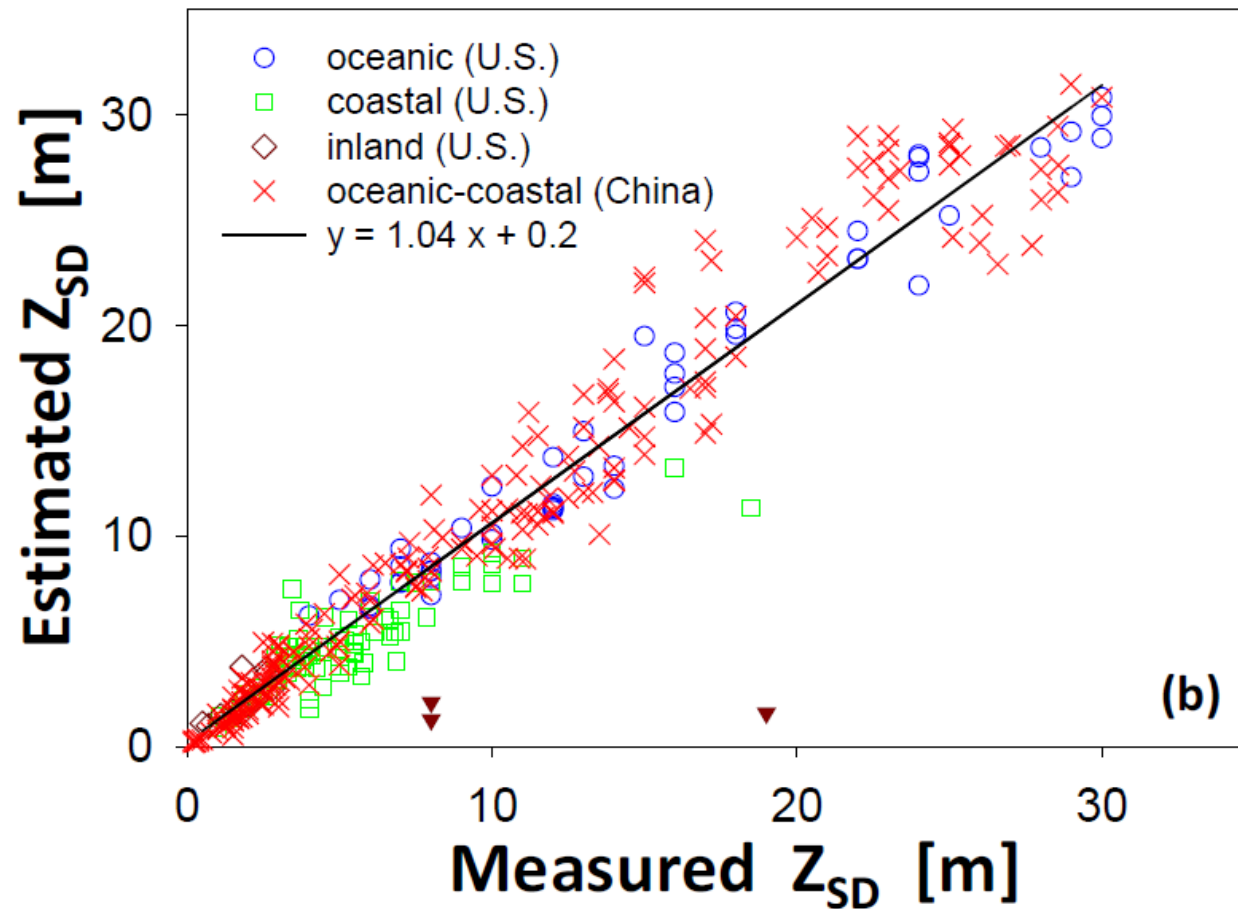
Now theory and measurements are consistent.



(Lee et al. 2018)

Verification of the new Secchi disk theory

$$R_{rs} \longrightarrow a \& b_b \longrightarrow K_d \longrightarrow Z_{SD}$$



(Lee et al 2015)

4. Estimation of primary production

Protocol. A primary goal of ocean-colour remote sensing is to produce synoptic fields of chlorophyll pigment, an index of phytoplankton biomass. It is the single most

(IOCCG Report #2, 1999)

“One of the principal applications of satellite ocean color data is to derive **net primary production** (NPP).”

--- McClain (Annu. Rev. Mar. Sci., 2009)

Traditionally Chl is used to represent phytoplankton

I. Wavelength-resolved models (WRMs)

$$\sum PP = \int_{\lambda=400}^{700} \int_{t=\text{sunrise}}^{\text{sunset}} \int_{z=0}^{Z_{\text{eu}}} \Phi(\lambda, t, z) \times \text{PAR}(\lambda, t, z) \times a^*(\lambda, z) \times \text{Chl}(z) d\lambda dt dz - R$$

II. Wavelength-integrated models (WIMs)

$$\sum PP = \int_{t=\text{sunrise}}^{\text{sunset}} \int_{z=0}^{Z_{\text{eu}}} \varphi(t, z) \times \text{PAR}(t, z) \times \text{Chl}(z) dt dz - R$$

III. Time-integrated models (TIMs)

$$\sum PP = \int_{z=0}^{Z_{\text{eu}}} P^b(z) \times \text{PAR}(z) \times DL \times \text{Chl}(z) dz$$

IV. Depth-integrated models (DIMs)

$$\sum PP = P^b_{\text{opt}} \times f[\text{PAR}(0)] \times DL \times \text{Chl} \times Z_{\text{eu}}$$

VGPM:

$$PP_{\text{eu}} = 0.66125 \times P^b_{\text{opt}} \times [E_0 / (E_0 + 4.1)] \times Z_{\text{eu}} \times C_{\text{opt}} \times D_{\text{irr}}$$

(Behrenfeld and Falkowski, 1997)

I. Wavelength-resolved models (WRMs)

$$\sum PP = \int_{\lambda=400}^{700} \int_{t=\text{sunrise}}^{\text{sunset}} \int_{z=0}^{Z_{eu}} \Phi(\lambda, t, z) \times \text{PAR}(\lambda, t, z) \times a^*(\lambda, z) \times \text{Chl}(z) d\lambda dt dz - R$$

Quantum yield of photosynthesis

$$a^* = \frac{a_{ph}}{\text{Chl}}$$

a_{ph} : phytoplankton absorption coefficient

$$\sum PP = \int_{t=\text{sunrise}}^{\text{sunset}} \int_{z=0}^{Z_{eu}} \varphi(t, z) \times \text{PAR}(t, z) \times \text{Chl}(z) dt dz - R$$

$$\sum PP = \int \int \int \phi \times \text{PAR}(\lambda, t, z) \times a_{ph}(\lambda, z) dt dz d\lambda - R$$

Centered on a_{ph}

5. Conclusions and Expectations

(1) It is not necessary to know B for the calculation of P with remote-sensing methods. What is

(Lee et al., 1996, Appl Opt)

$$\sum PP = \int_{t=\text{sunrise}}^{\text{sunset}} \int_{z=0}^{Z_{\text{eu}}} \varphi(t, z) \times \text{PAR}(t, z) \times \text{Chl}(z) dt dz - R$$

$$\sum PP = \int \int \int \phi \times \text{PAR}(\lambda, t, z) \times a_{ph}(\lambda, z) dt dz d\lambda - R$$

Contrast in mathematics and physics of the two approaches:

φ vs ϕ :

φ involves both ϕ and a^* .

Chl vs a_{ph} :

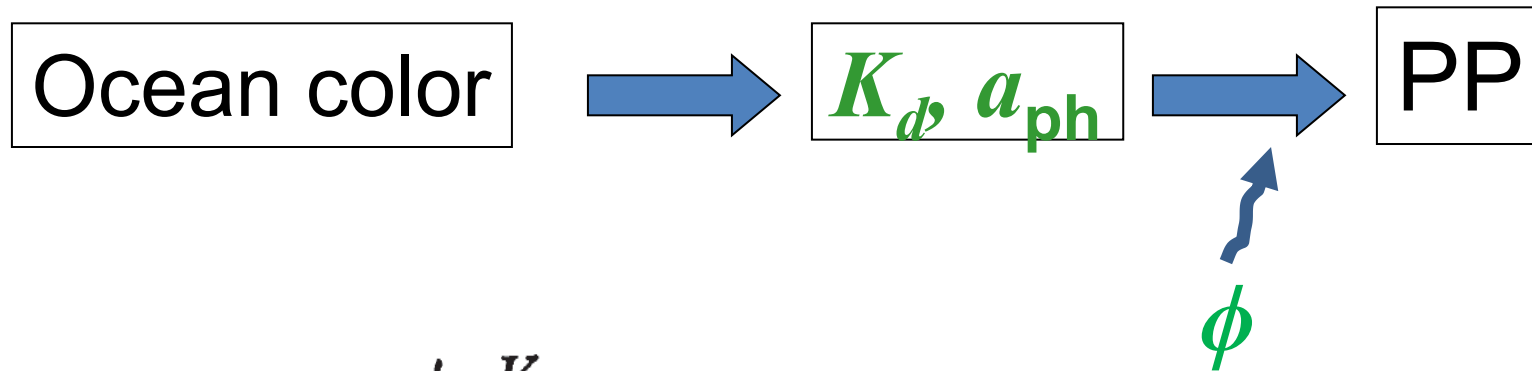
Chl is a biological property; **could not be** directly obtained from OC remote sensing.

a_{ph} is an optical property; ocean color measures optical property.

Absorption based on PP model

$$PP(z) = \iint \phi \times E_0(\lambda, t, z) \times a_{ph}(\lambda, z) d\lambda dt$$

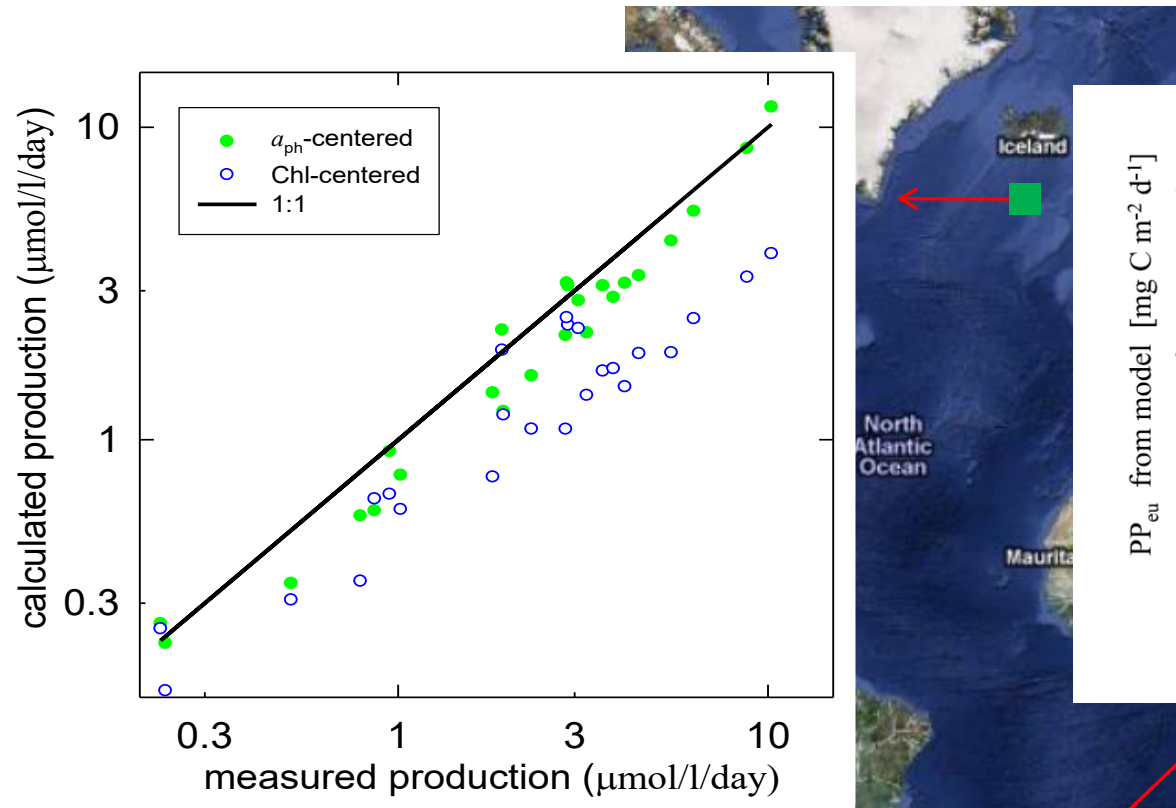
A more direct representation of photosynthesis.



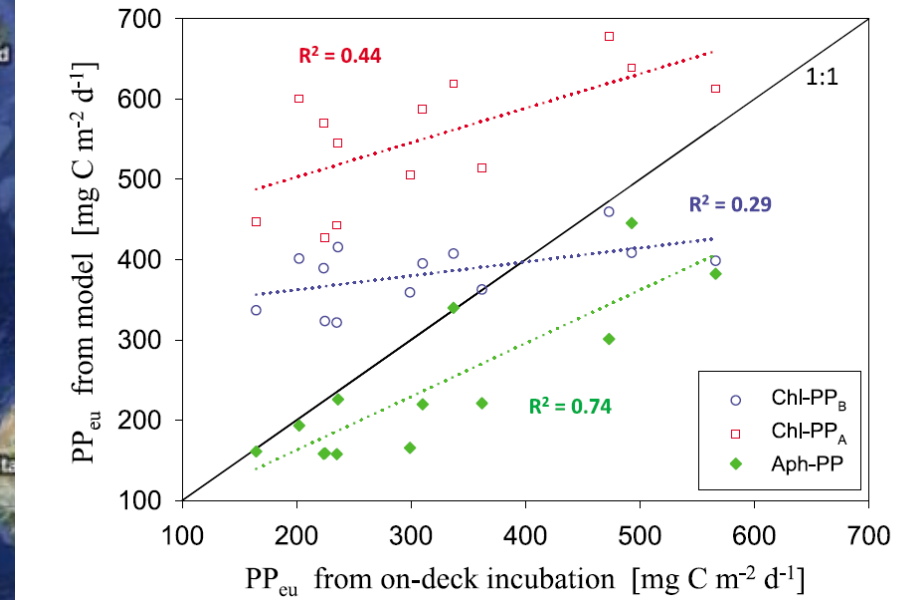
$$\phi(E_0) = \frac{\phi_m K_\phi}{K_\phi + E_0} \quad (2)$$

(Kiefer and Mitchell, 1983, L&O)

Remotely-estimated PP compared with measured PP

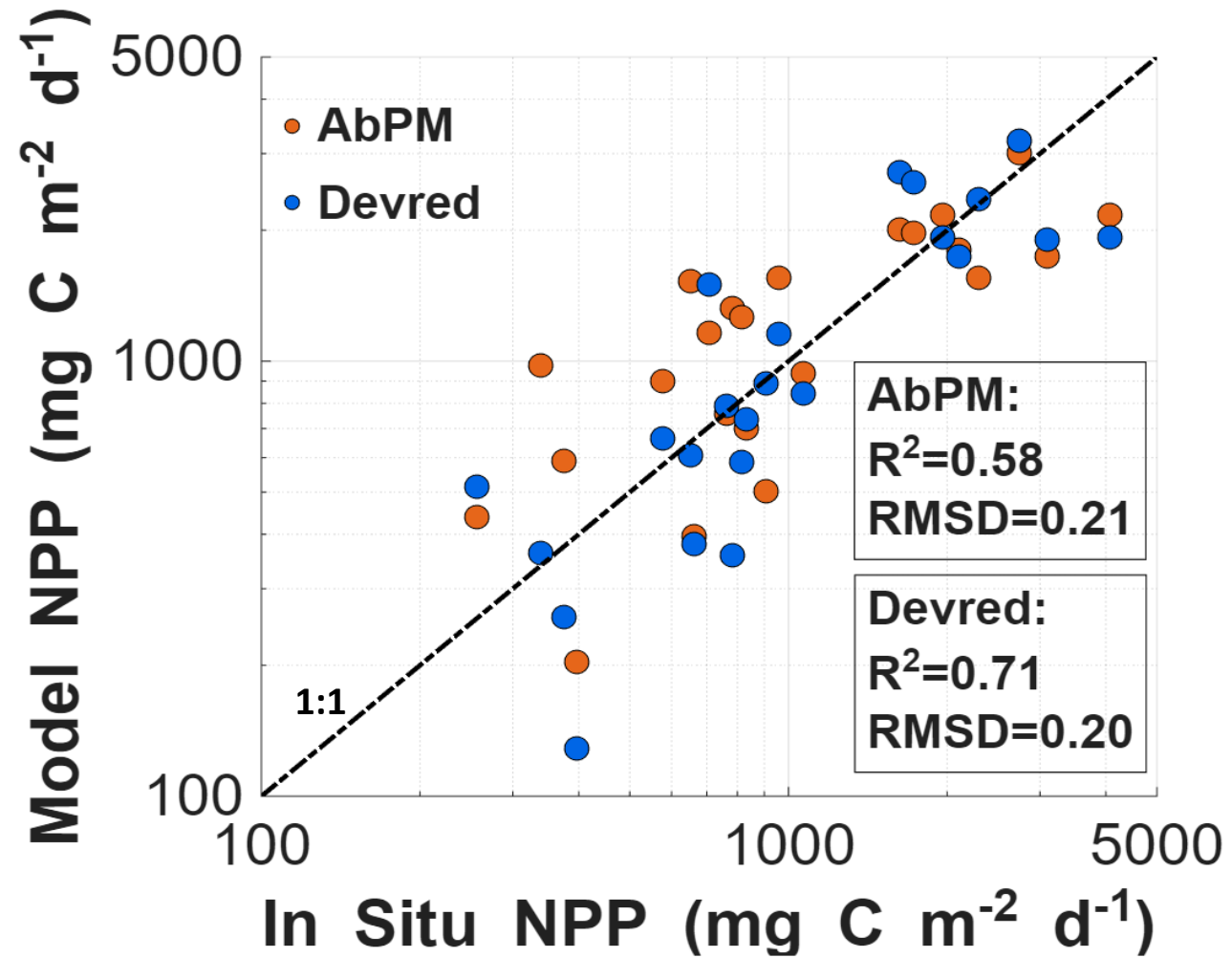


(redraw from *Lee et al. 1996*)



(*Lee et al. 2010*)

Labrador Sea



(Lee et al., under revision)

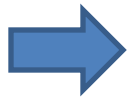
Why a_{ph} based approach is likely better?

Essence of present satellite Chl product:

$$Chl = fun\left(\frac{R_{rs}(\lambda_1)}{R_{rs}(\lambda_2)}\right)$$

$$R_{rs} \approx G \frac{b_b}{a + b_b}$$

$$\frac{R_{rs}(440)}{R_{rs}(550)} \approx \frac{a(550) b_{bw}(440) + b_{bp}(440)}{a(440) b_{bw}(550) + b_{bp}(550)}$$

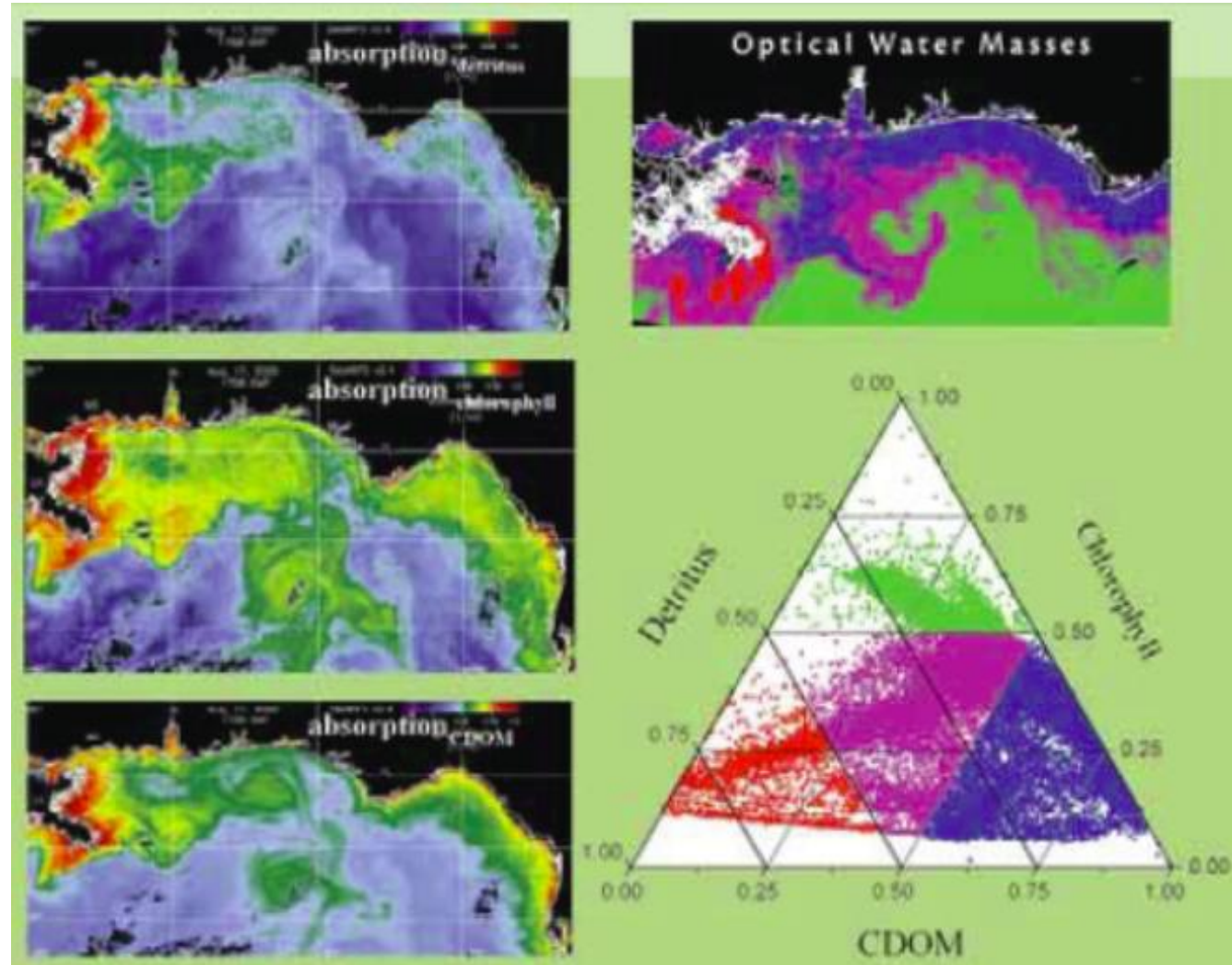


$$\frac{R_{rs}(440)}{R_{rs}(550)} \propto \frac{a(550)}{a(440)} = \frac{a_w(550) + a_{dg}(550) + a_{ph}^*(550) Chl}{a_w(440) + a_{dg}(440) + a_{ph}^*(440) Chl}$$

Change of R_{rs} band ratio not necessarily represents change of [Chl].

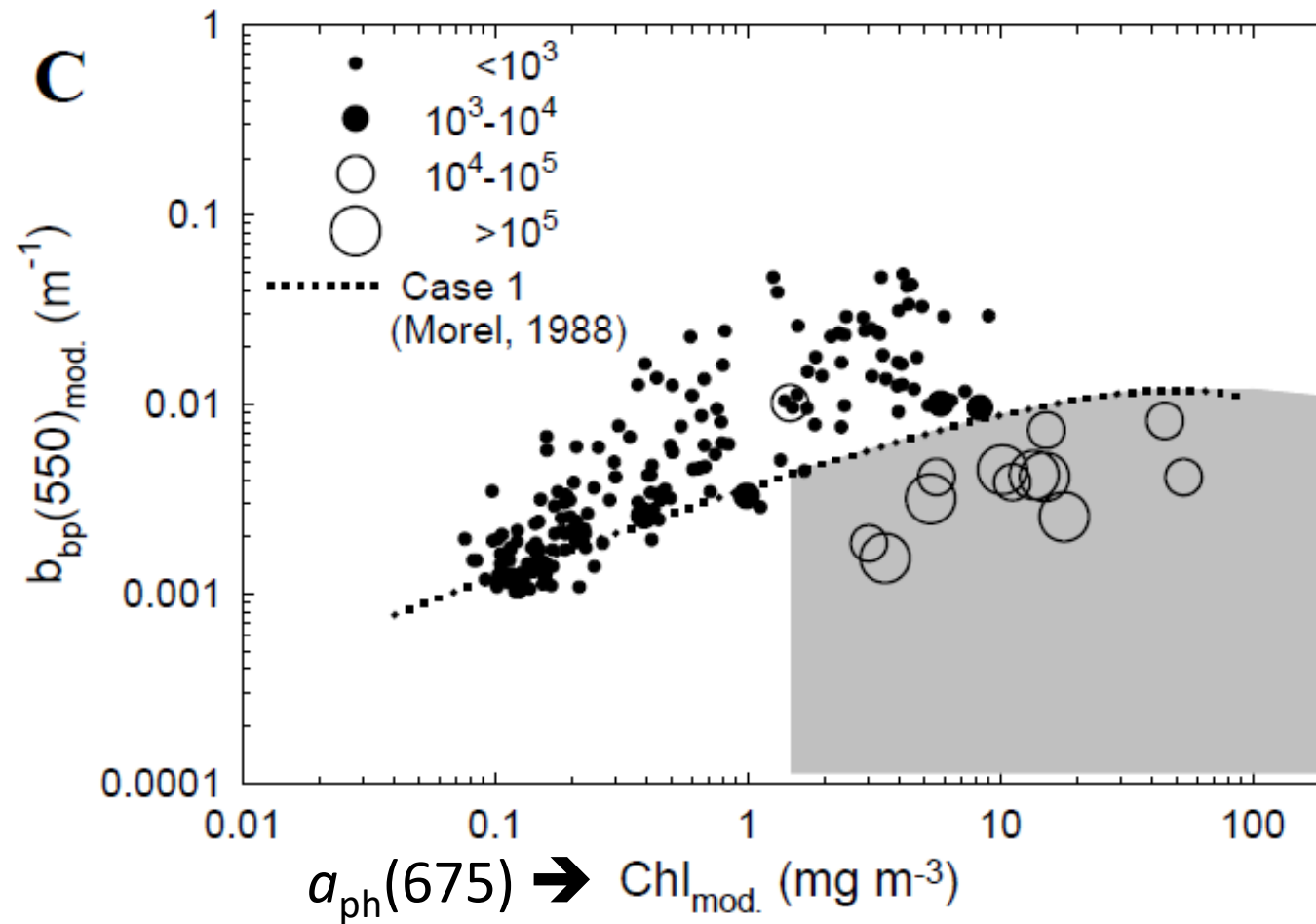
5. A few other examples

5a. Water mass classification



(Arnone et al. 2004)

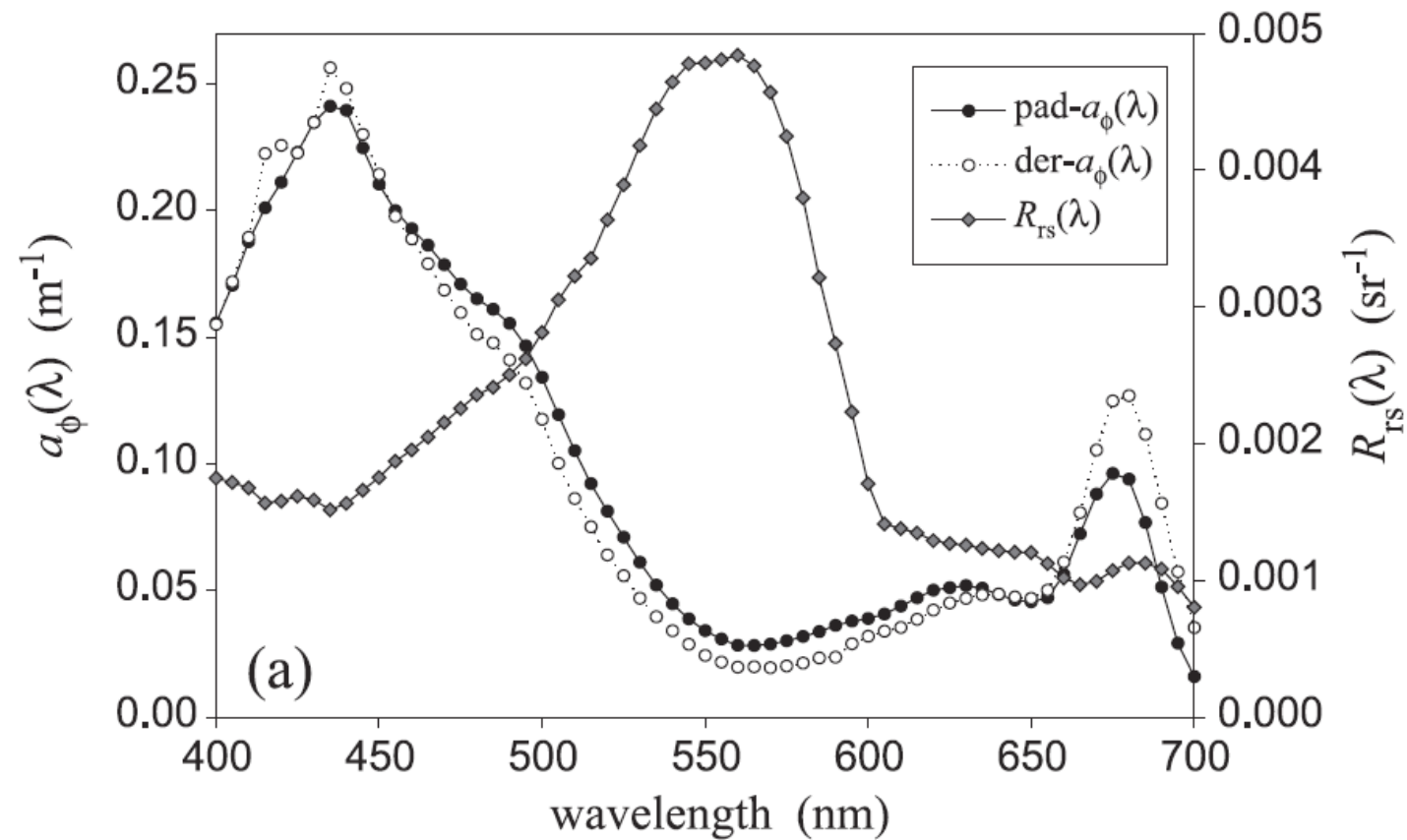
5b. HAB identification-1



(Carnizzaro et al. 2008)

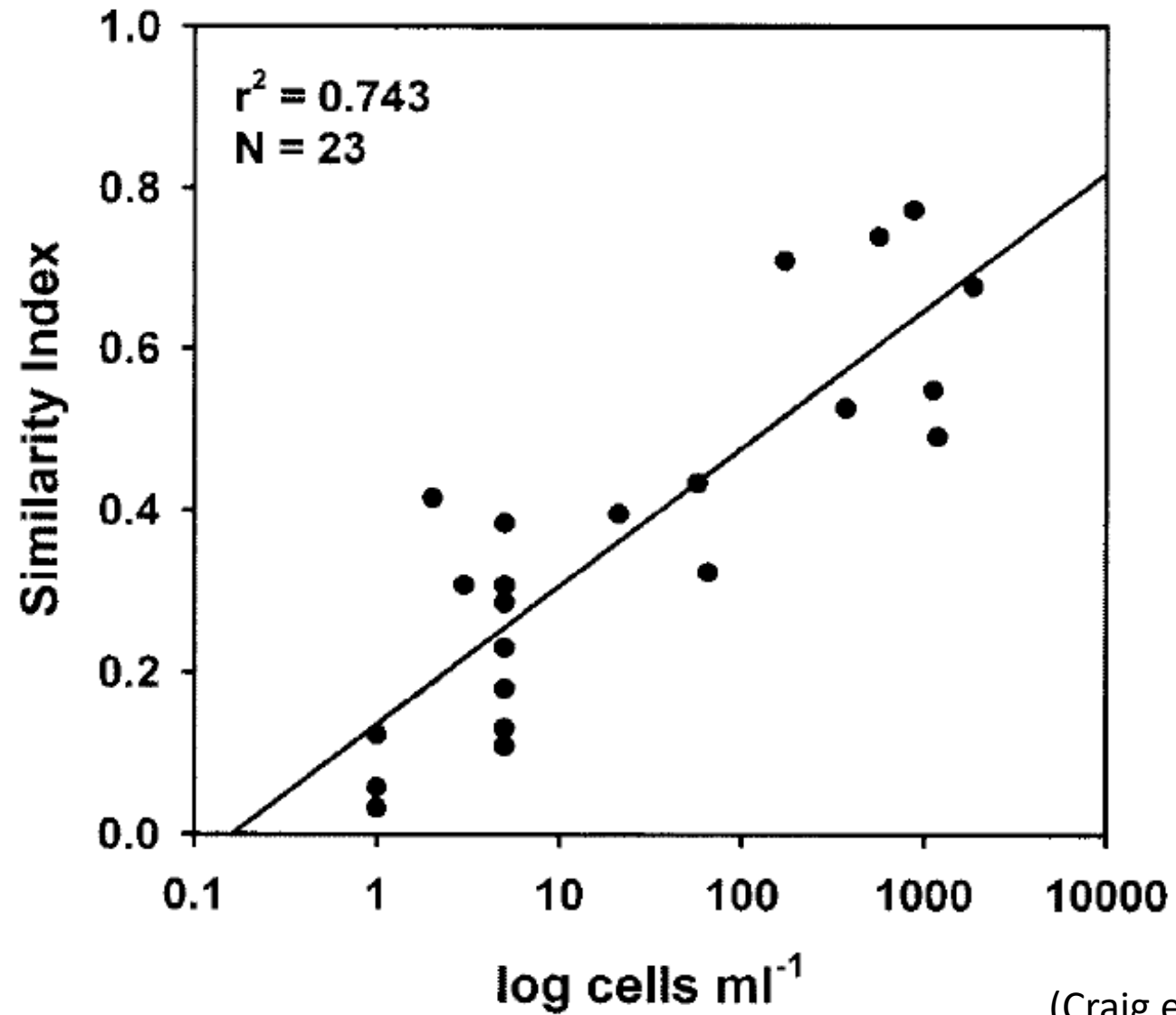
5b. HAB identification-2

$$R_{rs}(\lambda) \xrightarrow{\text{QAA}} a_{ph}(\lambda) = a(\lambda) - a_{dg}(\lambda) - a_w(\lambda)$$



(Lee and Carder 2004)

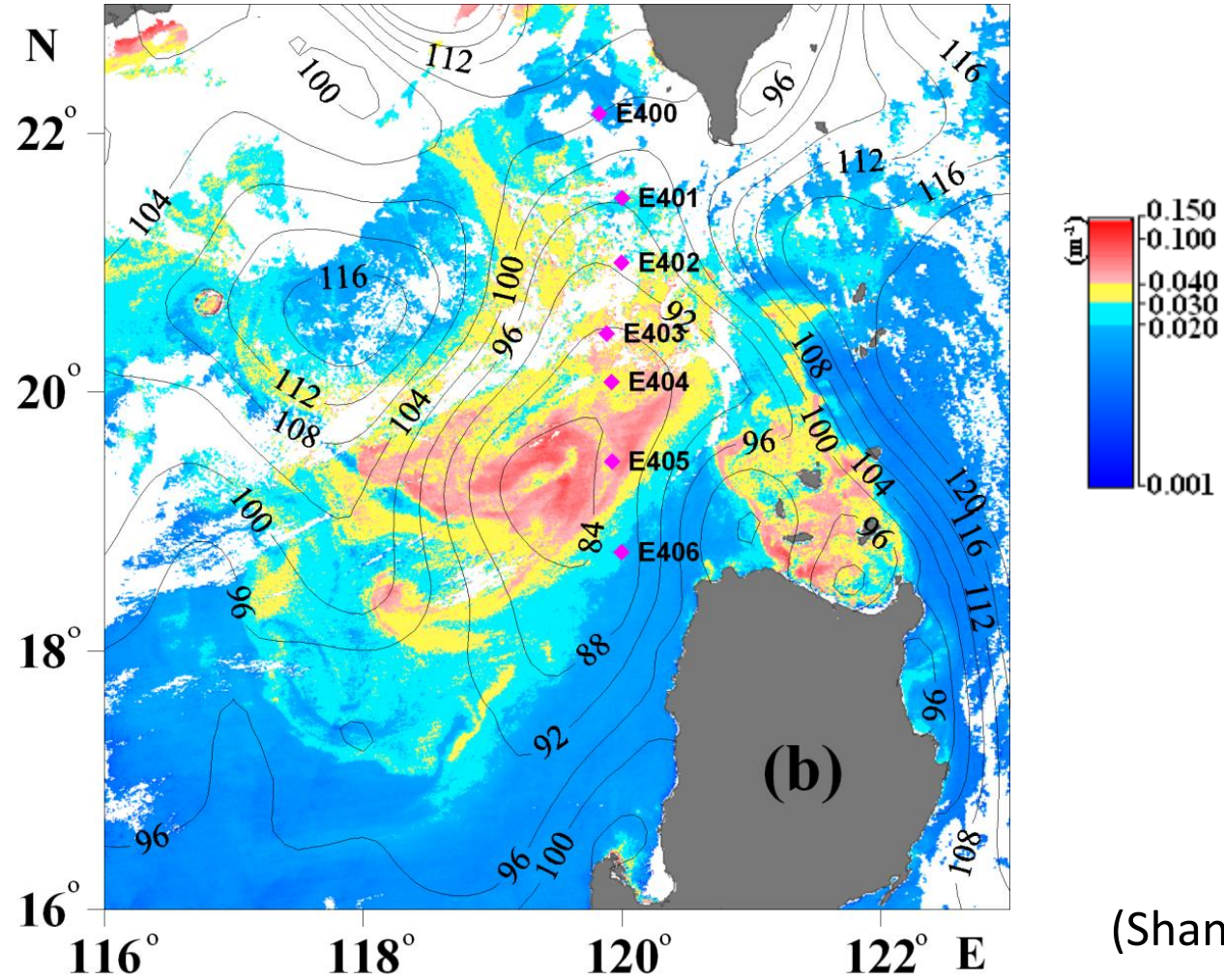
K. brevis



(Craig et al 2006)

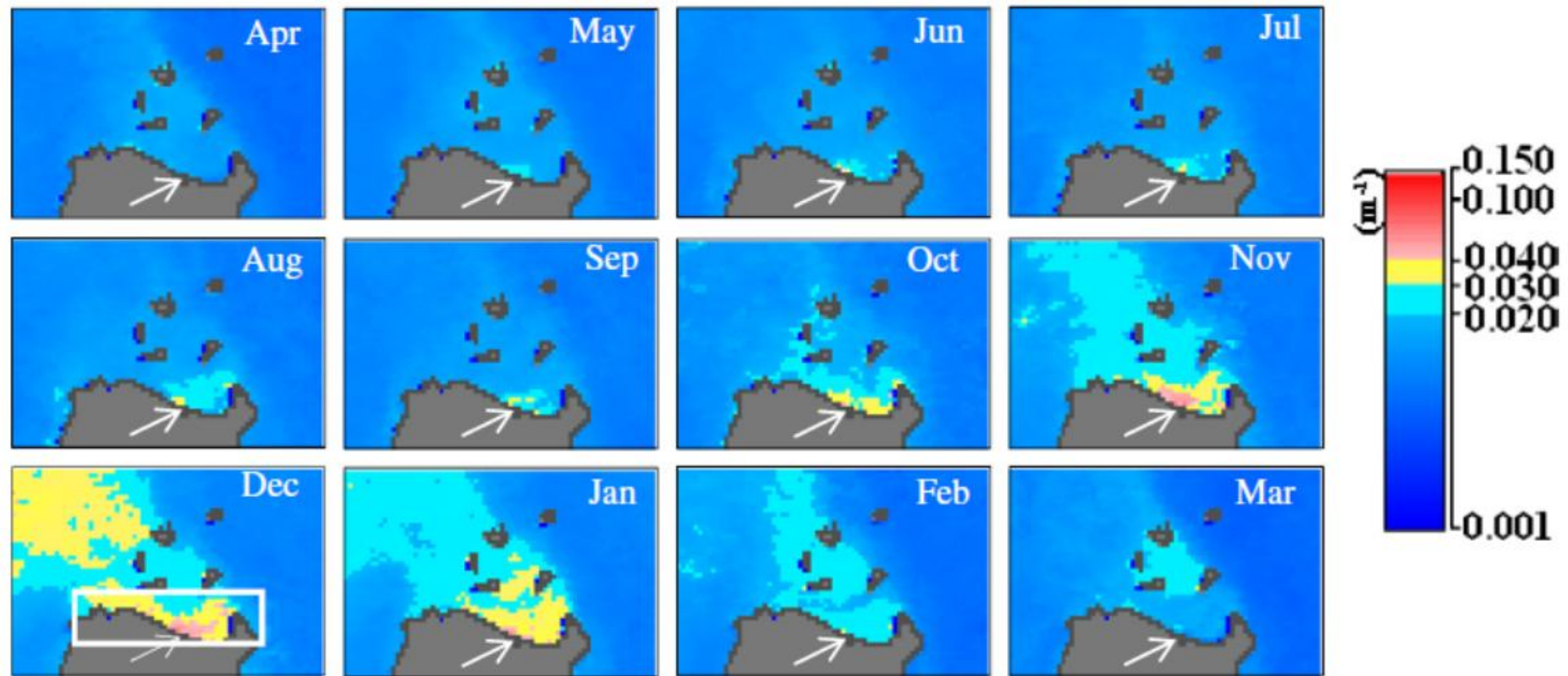
5c. Bloom dynamics

Distribution of $a_{ph}(440)$ at Luzon Street



(Shang et al, 2012)

Monthly distribution of $a_{ph}(440)$ at Luzon Street



(Shang et al, 2012)

5d. Global physiology of ocean phytoplankton

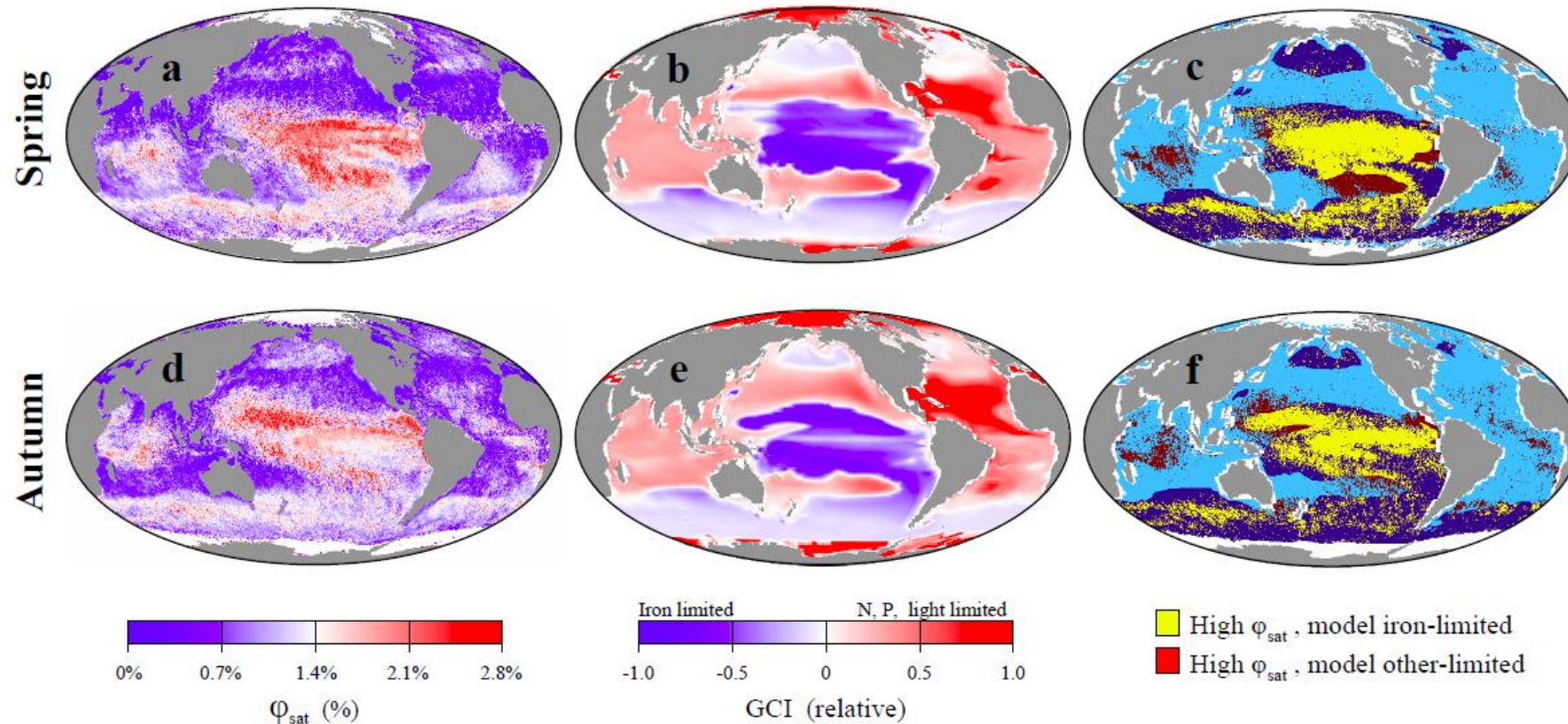
IOP

$$F_{\text{sat}} = \text{Chl}_{\text{sat}} \times \langle a_{ph}^* \rangle \times \phi \times S,$$

(2)

ϕ : quantum yield of fluorescence

(Behrenfeld et al 2009)



(Behrenfeld et al 2009)

5e. Salinity estimation

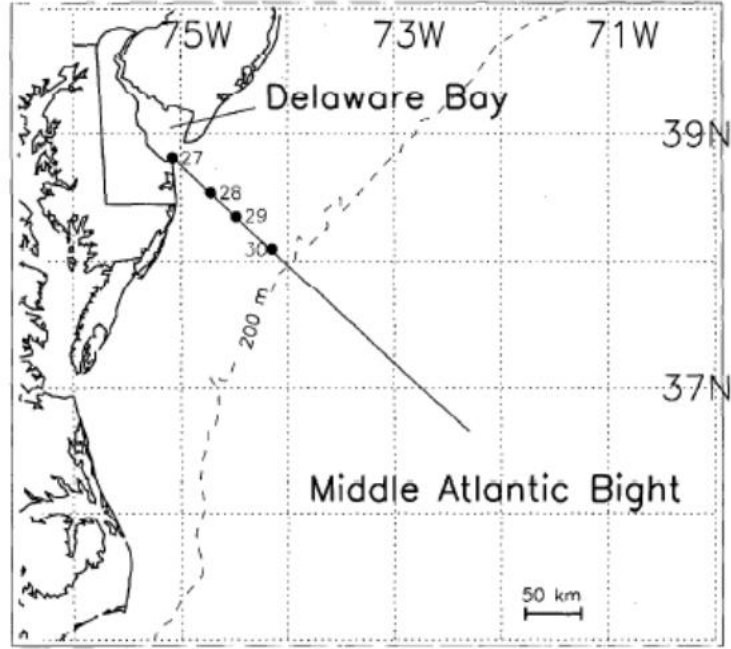
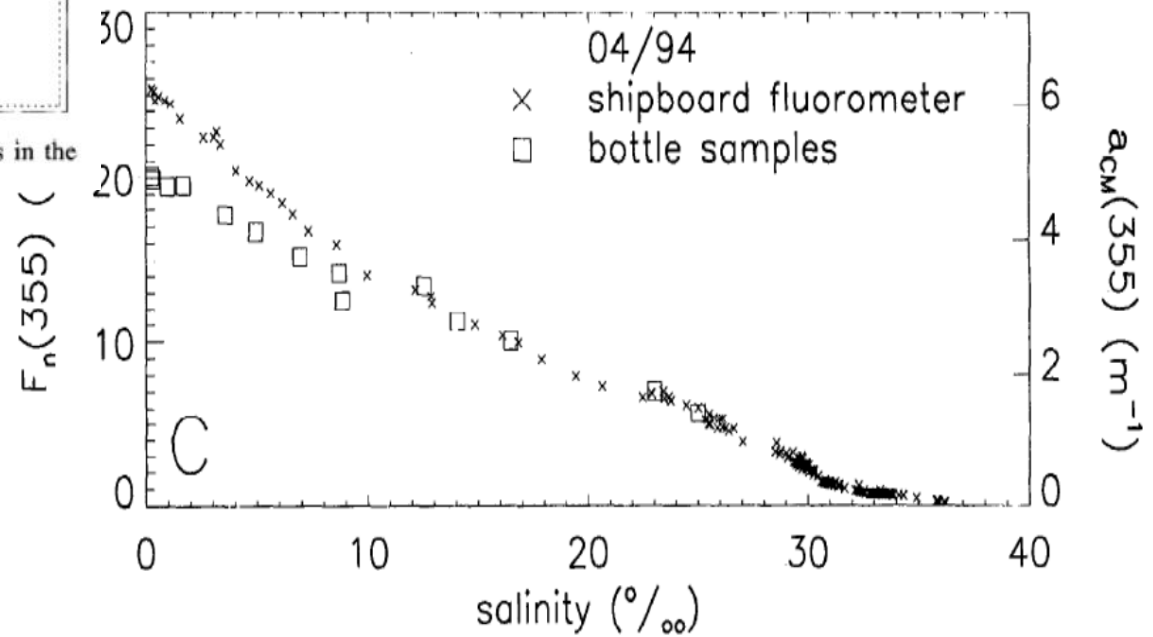
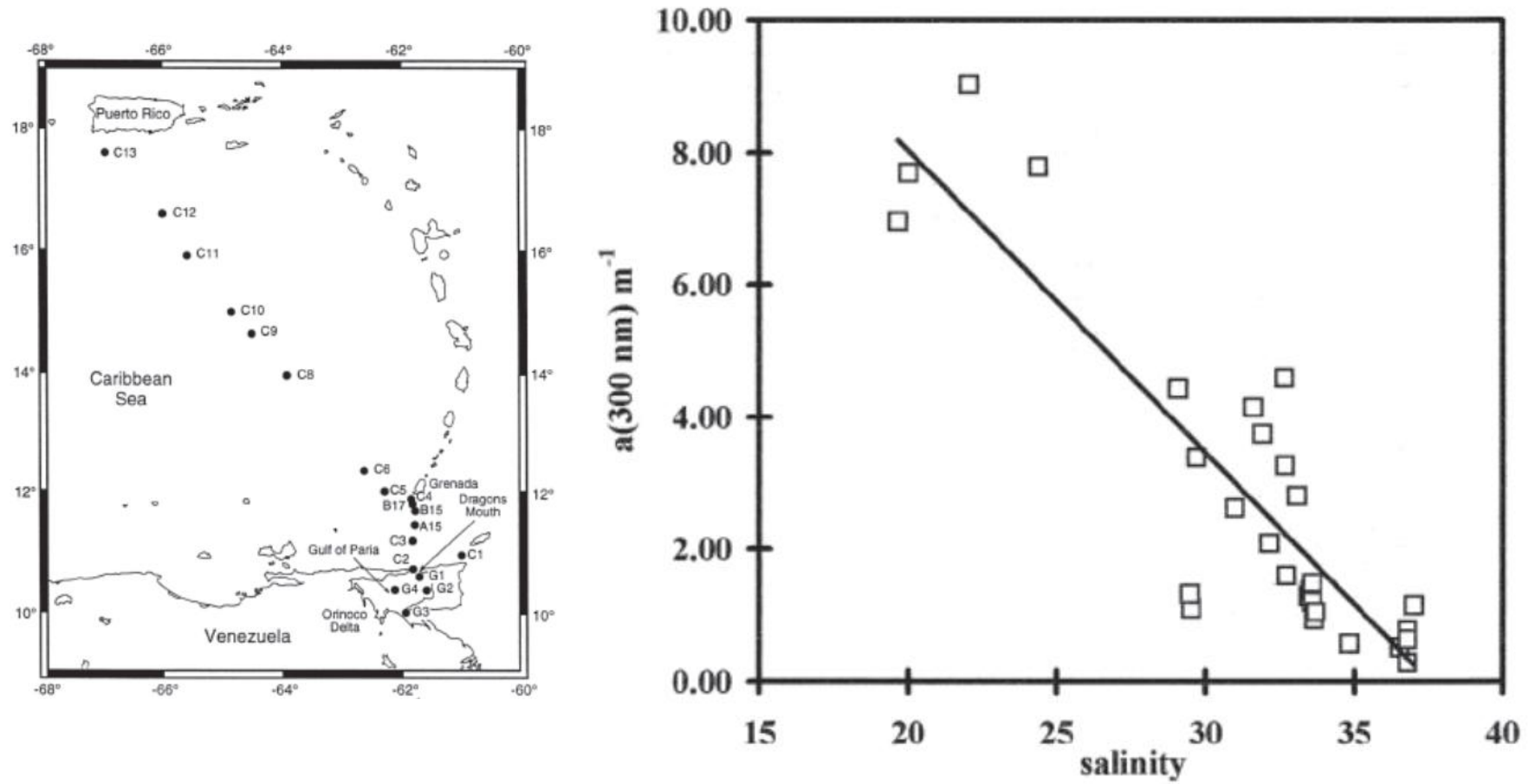


Fig. 1. Locations of the transect and hydrocast stations in the Middle Atlantic Bight.



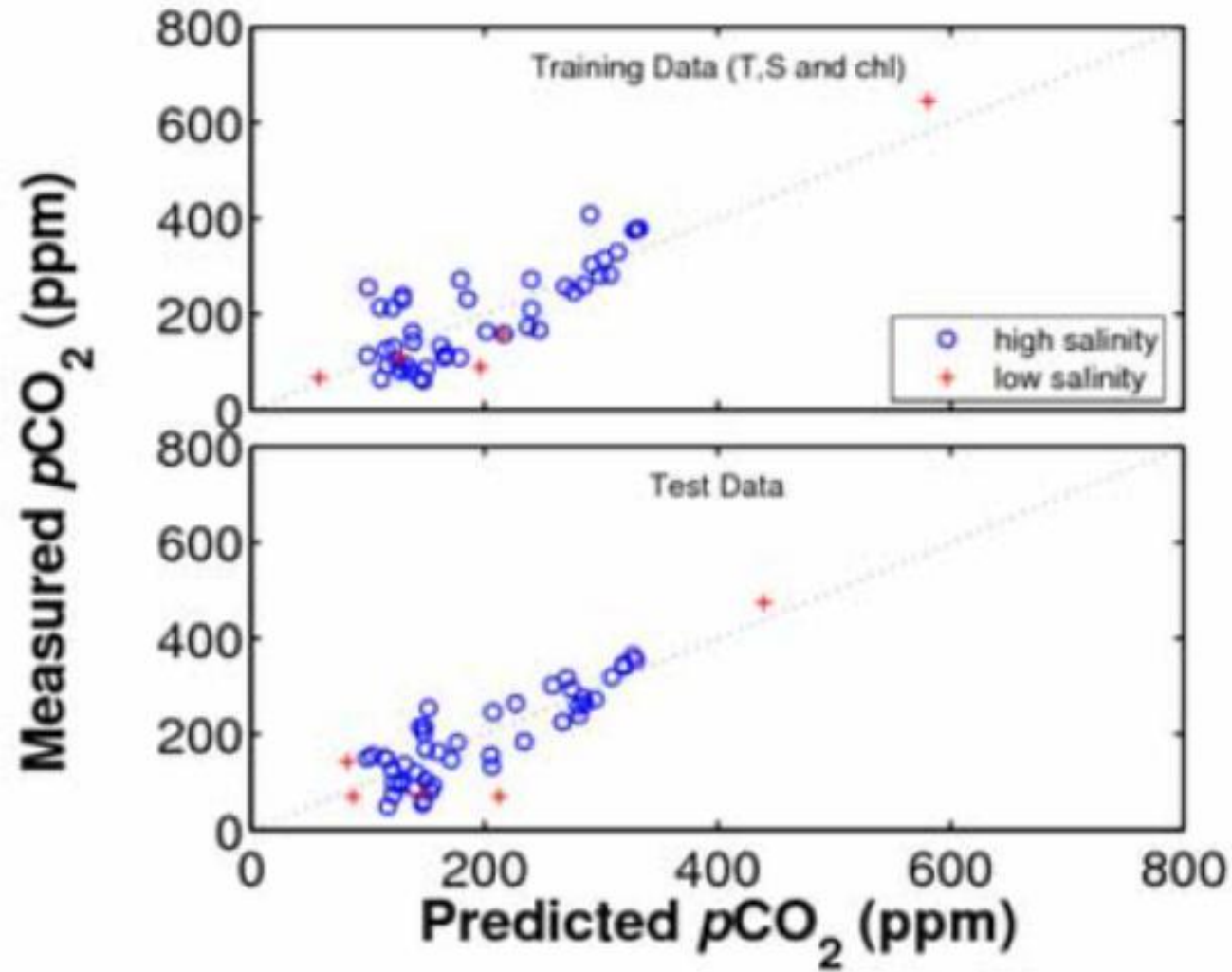
(Vodacek et al 1997)



$$SSS = x a_{\text{CDOM}} + y$$

(Castellio et al 1999)

5f. pCO₂ estimation



Lohrenz and Cai (2006)

$$pCO_2 = f(T, S, Chl)$$

Key Points:

1. Many applications traditionally built around [Chl] can be built around IOPs.
2. Remote sensing and applications centered around IOPs avoided, when necessary, concentration-normalized optical properties.
3. With IOPs as inputs, many products, e.g. K_d , Z_{eu} , Z_{sd} , PP, could be estimated easily and more accurately.
4. When IOPs are known, many other applications could be carried out.

Be creative.

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Zhongping Lee^{1*}, Longteng Zhao¹, Chuanmin Hu², Daosheng Wang¹, Junfang Lin³, and Shaoling Shang¹

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A SCIENCE PARTNER JOURNAL

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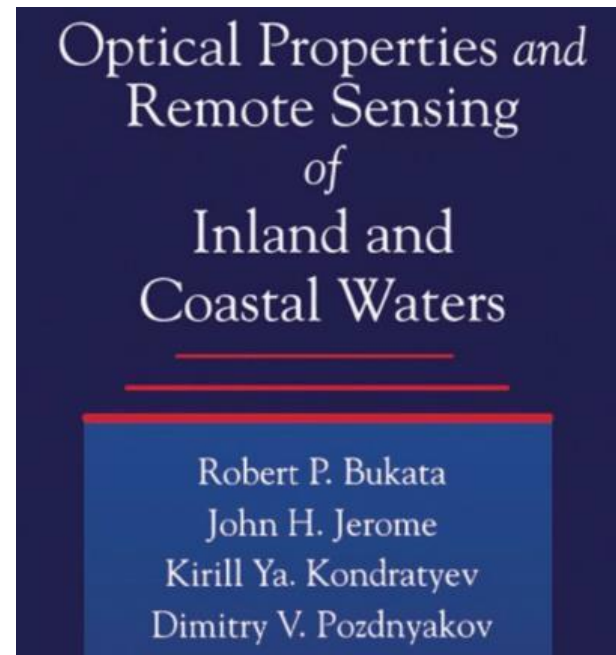
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An analysis of model and radiance measurement errors**

Frank E. Hoge

NASA Goddard Space Flight Center, Wallops Flight Facility, Wallops Island, Virginia

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Steven E. Lohrenz

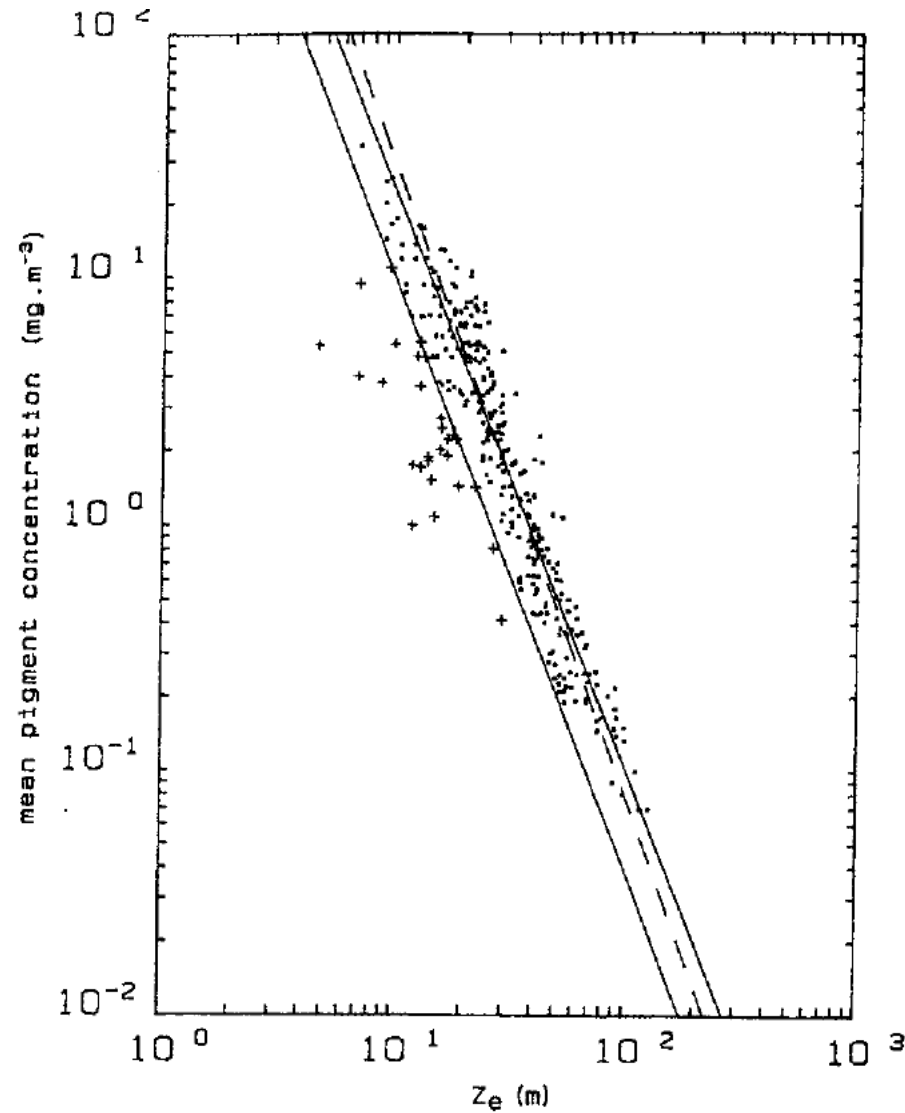
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Wei-Jun Cai

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[Chl] (empirical) approach:

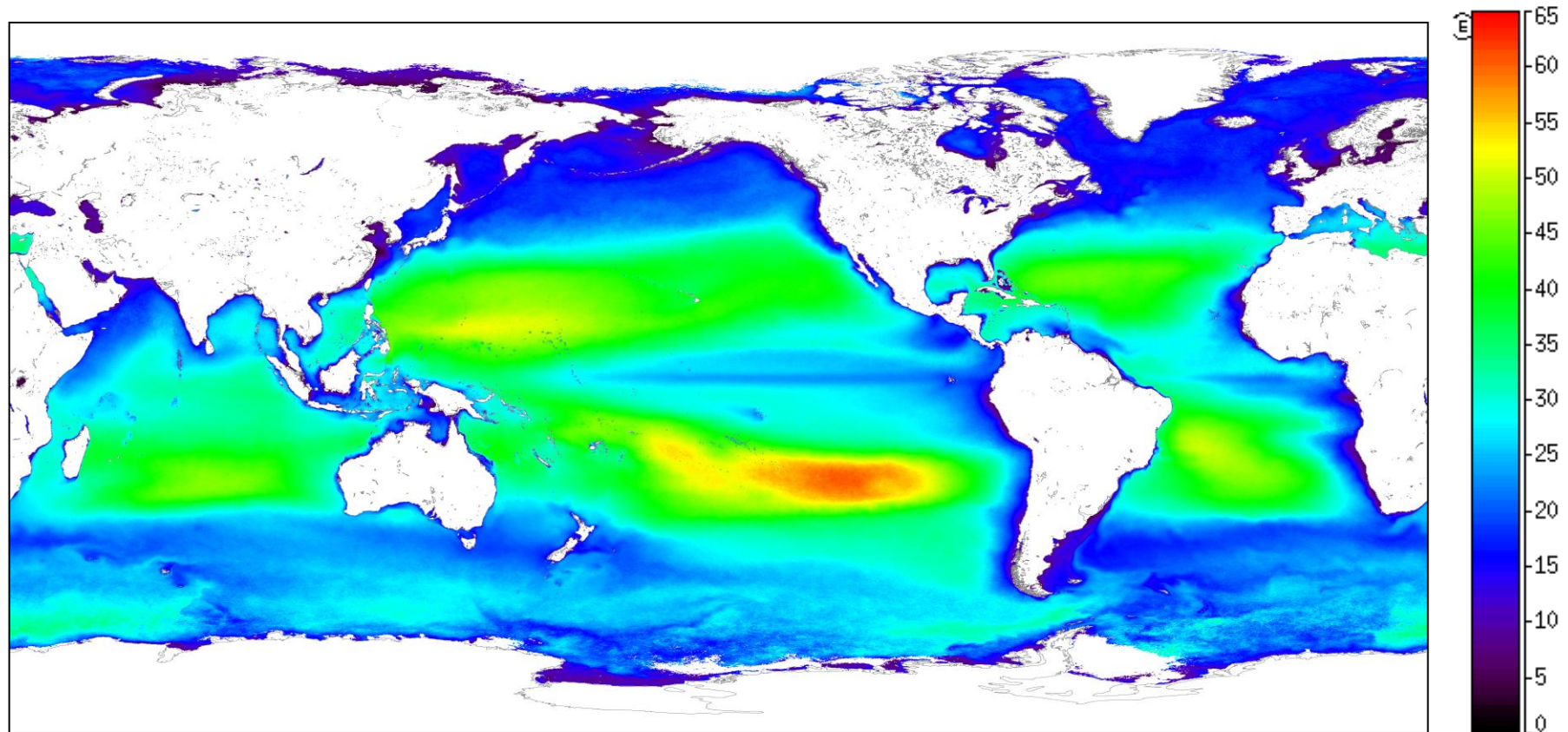
$$R_{rs}(\lambda) \rightarrow [\text{Chl}] \rightarrow z_{eu}$$



$$Z_e = 38.0C^{-0.428}$$

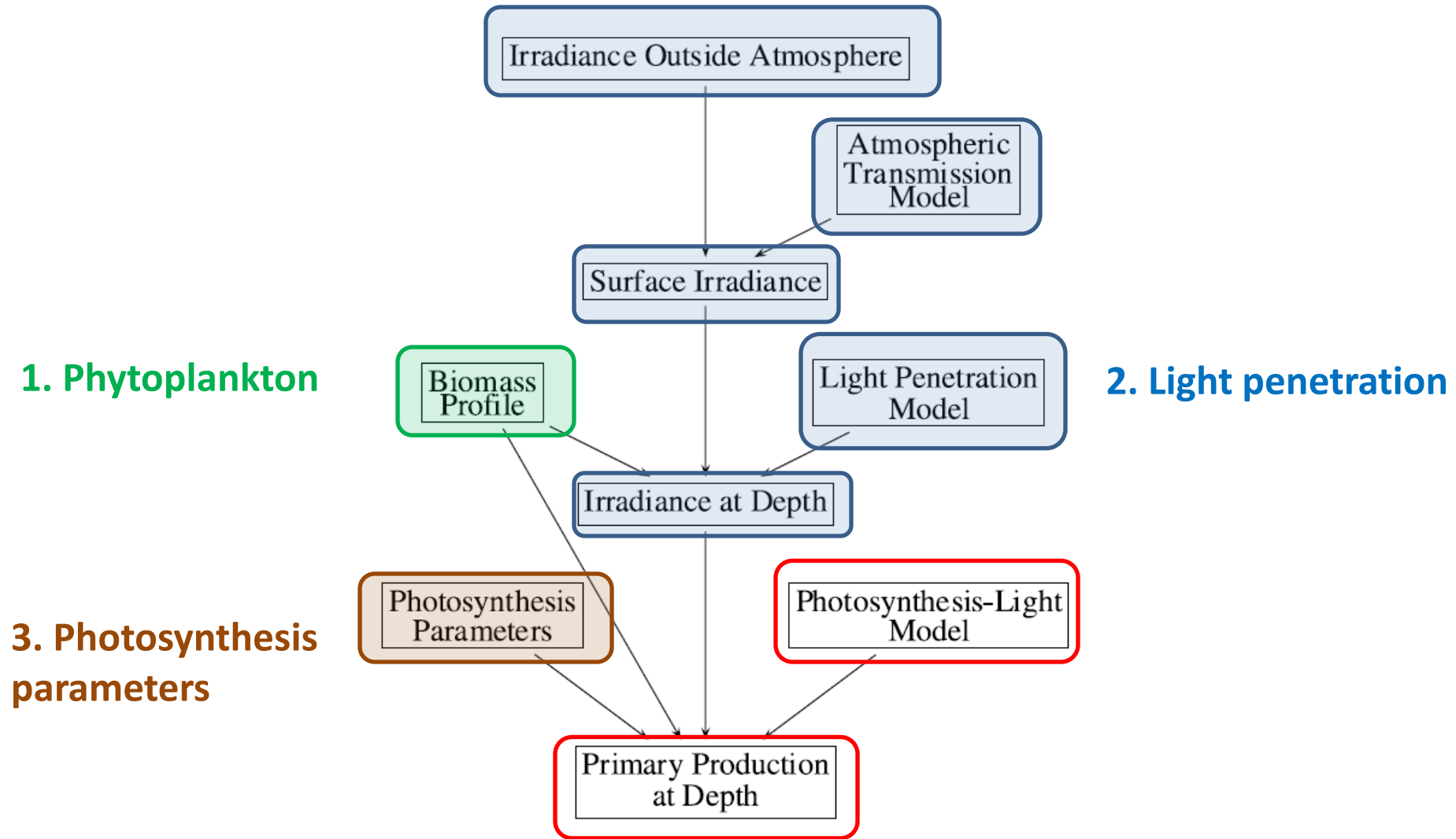
(Morel 1988)

Global Z_{SD}



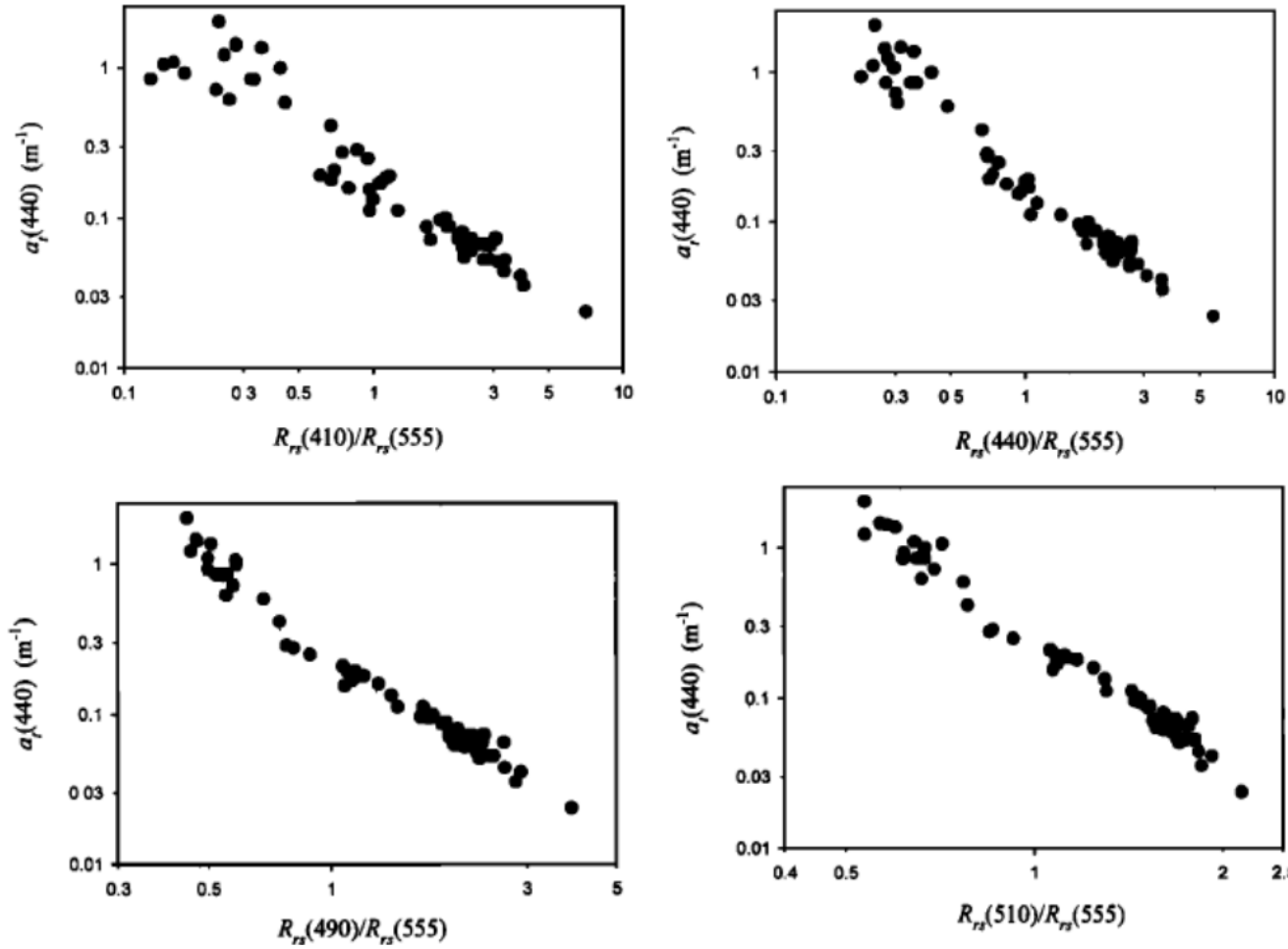
A much more straightforward product for water clarity!

Components for PP estimation:



(Platt and Sathyendranath, 2007)

Empirical:



$$a_i(440) = 10^{-0.674 - 0.531\rho_{25} - 0.745\rho_{25}^2 - 1.469\rho_{35} + 2.375\rho_{35}^2}, \quad (14)$$

$$a_\phi(440) = 10^{-0.919 + 1.037\rho_{25} - 0.407\rho_{25}^2 - 3.531\rho_{35} + 1.579\rho_{35}^2}, \quad (20)$$

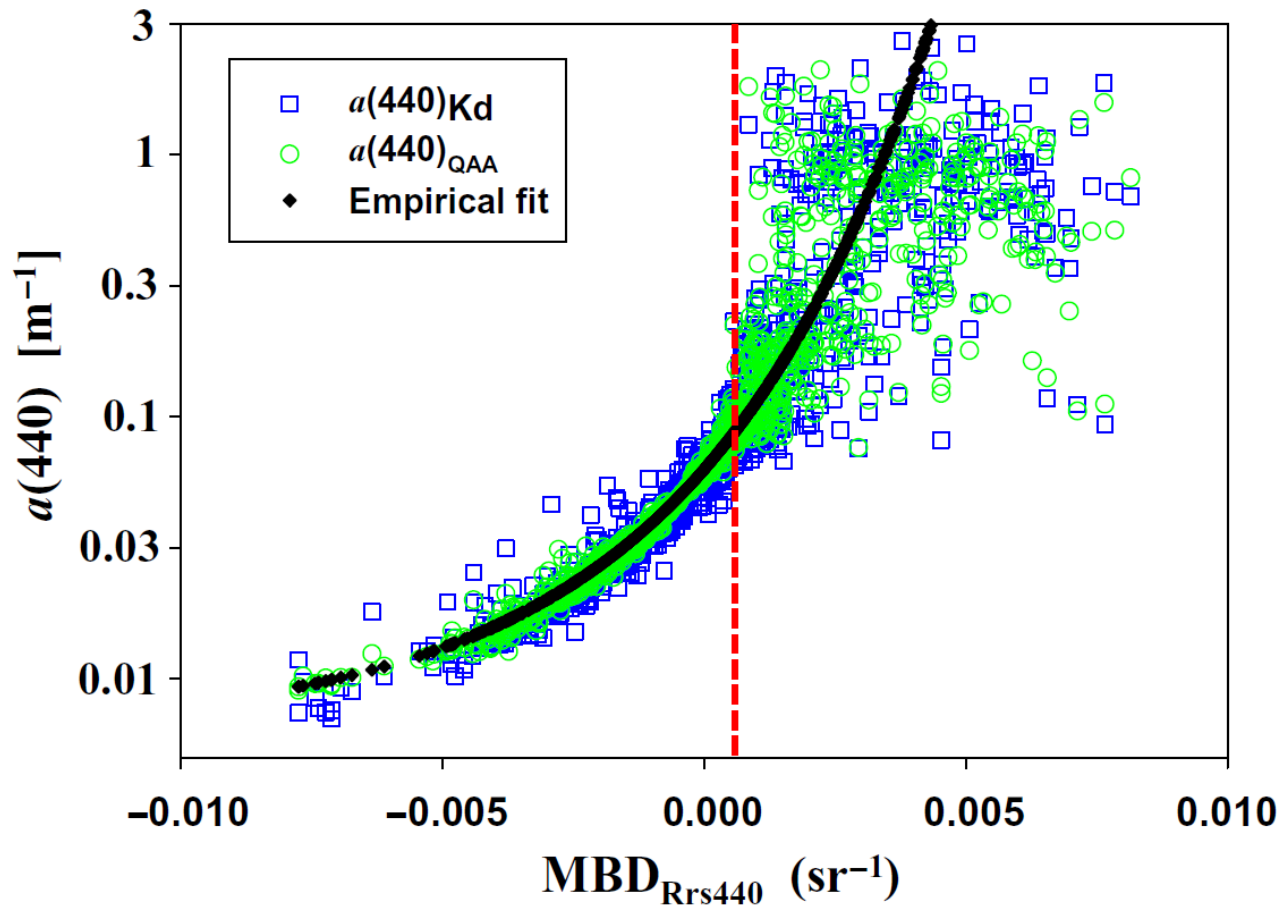


Fig.3. Relationship between $a(440)$ and MBD_{Rrs440} . The red vertical line indicates the location of $MBD_{Rrs440} = 0.0005 \text{ sr}^{-1}$.

(Lee et al., 2023)

$$MBD_{Rrs440} = R_{rs}(555) - \left[R_{rs}(443) + \frac{555 - 443}{670 - 443} (R_{rs}(670) - R_{rs}(443)) \right]$$