

Light Scattering in Water

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Background

BS	Major: Biology; Minor: Physics, Music – Trinity University, TX	1992
PhD	Oceanography – University of Rhode Island (Percy Donaghay)	1998
Postdoc	Environmental Optics Fellowship – Oregon State University (Ron Zaneveld)	1998-1999

CURRENT POSITIONS

Professor, <i>Harbor Branch Oceanographic Institute, FAU</i>	2015-present
Affiliate Professor, <i>Ocean Engineering, FAU</i>	2017-present
Associate Director, <i>NOAA Cooperative Institute, HBOI</i>	2018-present
President, <i>Sunstone Scientific LLC</i>	2017-present
President, <i>Environmental Optics Consulting LLC</i>	2016-present
Program Lead, Maritime Sensing, <i>I-SENSE, FAU</i>	2016-present
Senior Engineer, <i>SEACORP Inc.</i>	2015-present

FORMER POSITION

Director of Research and Vice President, <i>WET Labs, Inc.</i>	2005-2015
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- Ocean optics research, basic science
- Sensor development in ocean optics
- NASA PACE Science Team

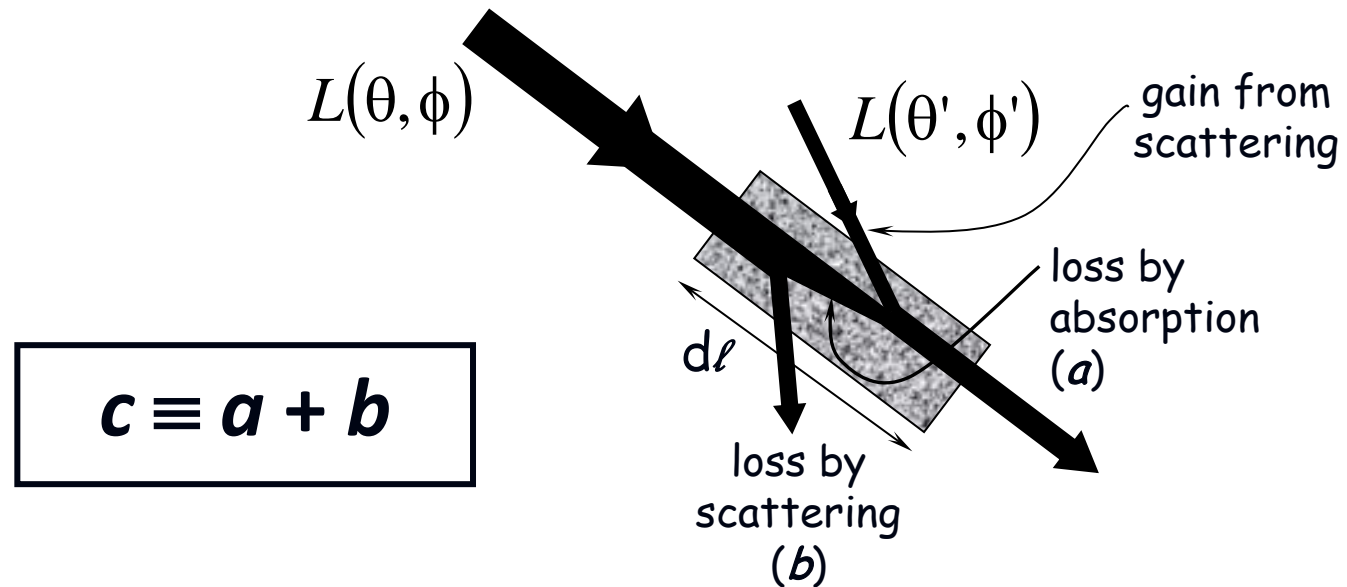
Lex G LW Lagoonfest 2017 Shake



“Lex Groovius”



Radiative Transfer in the Ocean



Inherent Optical Properties (IOPs)

Depend only on substances in water

[Attenuation (c), Absorption (a), Scattering, (b), and related subfractions]

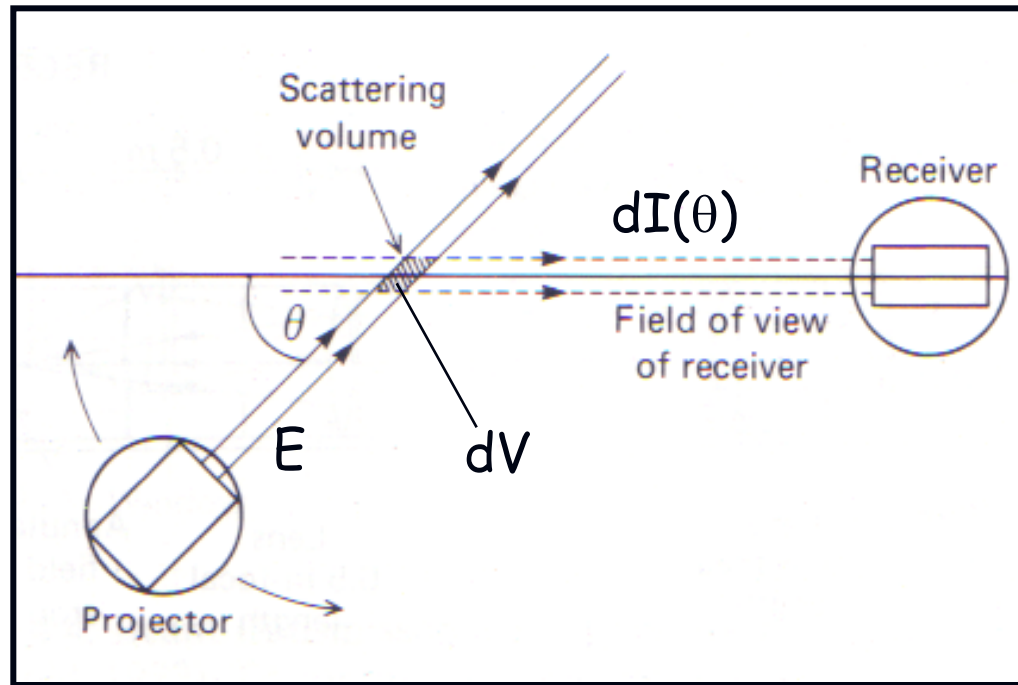
Apparent Optical Properties (AOPs)

Depend on substances in water AND ambient light field

[Reflectance (R), Diffuse attenuation (K), and related parameters]

Volume Scattering Function (VSF) defined

$$\beta(\theta) = \frac{dI(\theta)}{EdV} = \frac{W \cdot sr^{-1}}{W \cdot m^{-2} \cdot m^3} = m^{-1} \cdot sr^{-1}$$



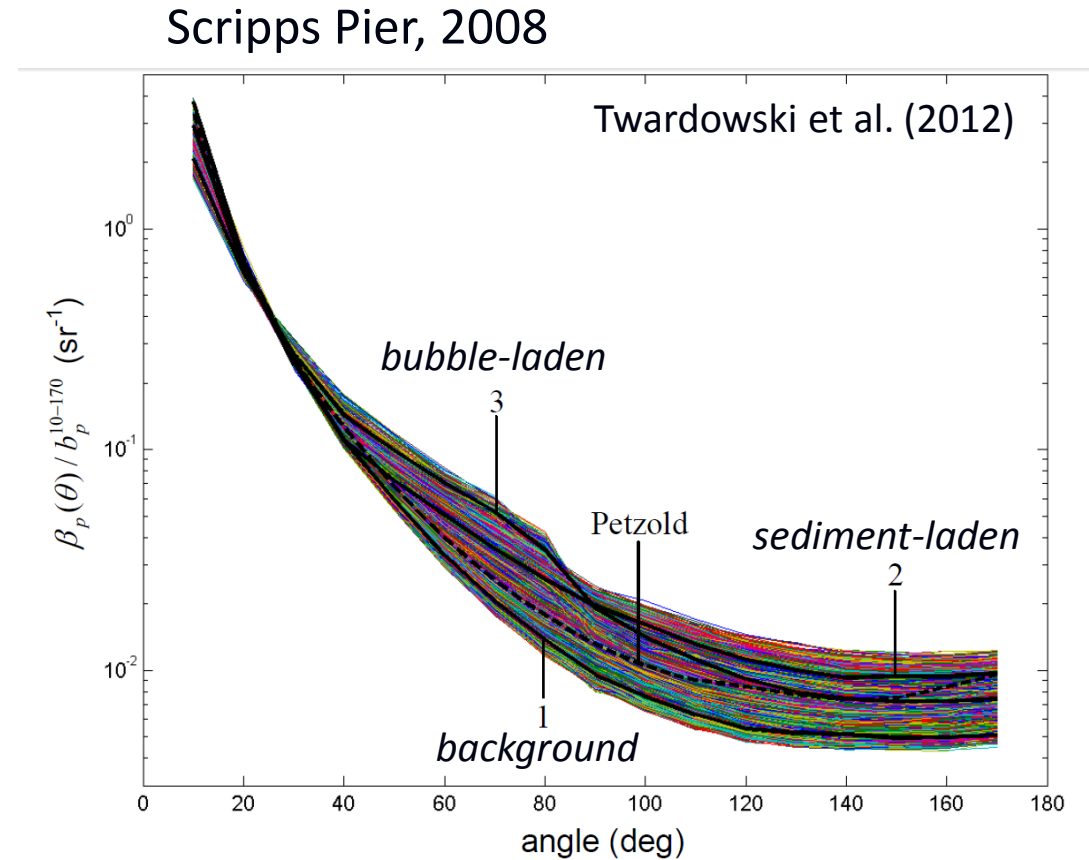
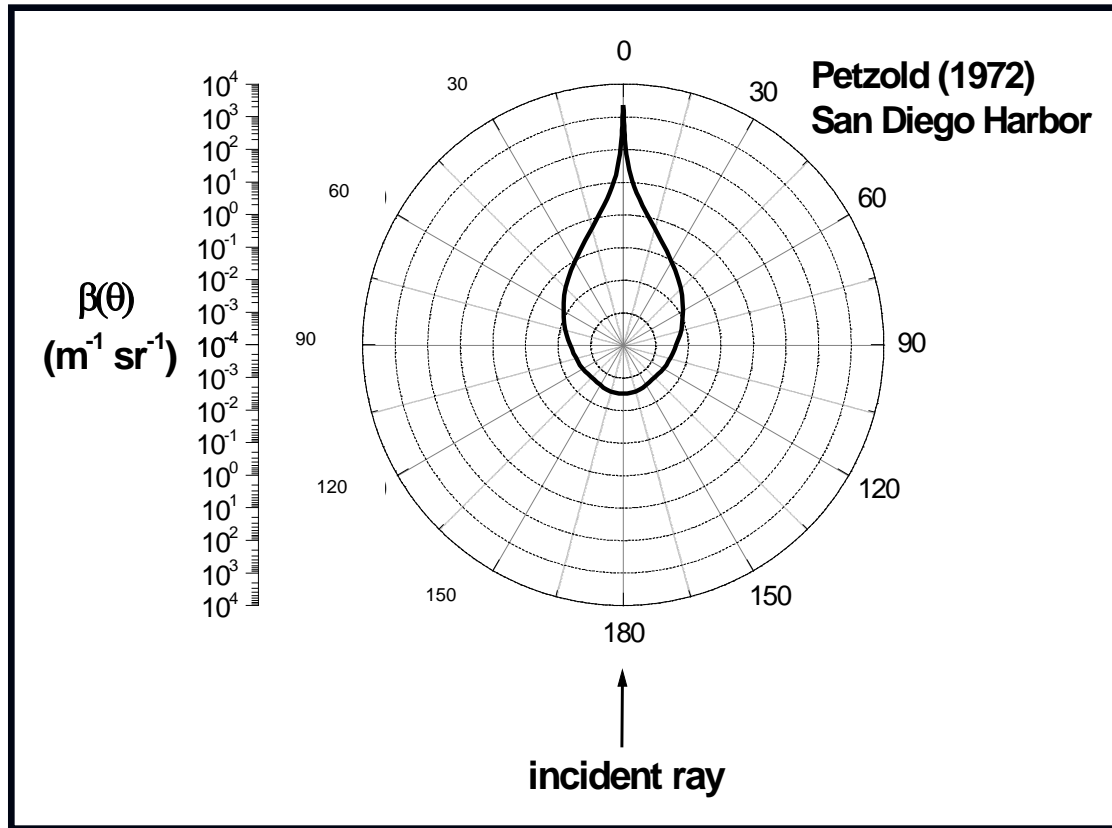
$dI(\theta)$ radiant flux
in direction
 $d\theta$ ($W \text{ sr}^{-1}$)

dV elemental
volume (m^3)

E incident
irradiance
($W \text{ m}^{-2}$)

Typical VSF

- *Log Scale
- Scale $\sim 10^7$
- Dynamic range
- *Very steeply forward peaked



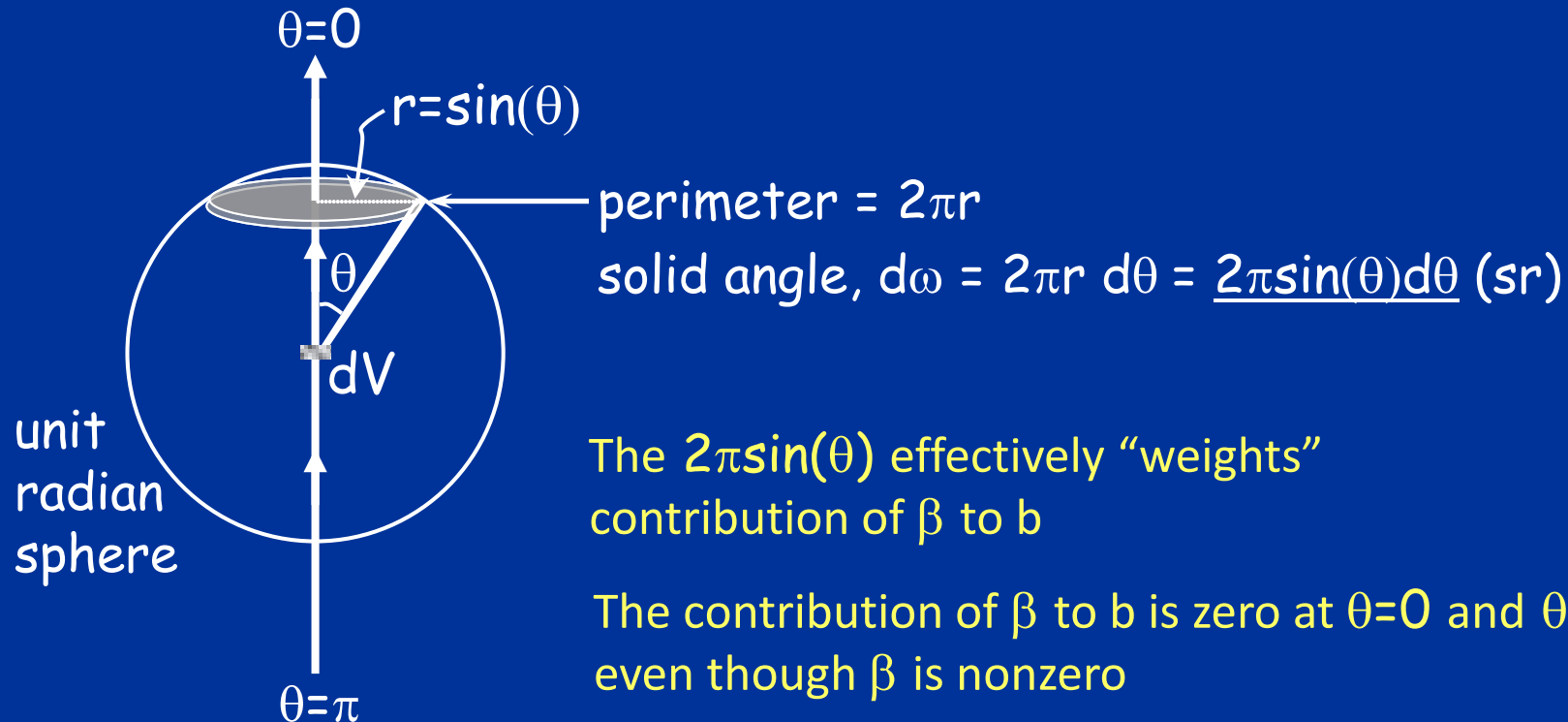
Typically, only $\sim 0.3-3\%$ of scattering (b) is backscattering (b_b)
 (however, in clear waters, b_w can increase this %)

VSF integration to obtain b

Remember...

$$b = 2\pi \int_0^{\pi} \sin(\theta) \beta(\theta) d\theta$$

Assuming
azimuthal
symmetry



Scattering components

Can partition with respect to constituent components..., e.g.:

$$b_t(\lambda) = b_w(\lambda) + b_p(\lambda) \quad \text{Units m}^{-1}$$

Also with respect to angular distribution:

$$b_x = 2\pi \int_i^j \sin(\theta) \beta(\theta) d\theta$$

Total scattering

set $x = t$

$[i, j] = [0, \pi]$

Forward scattering

set $x = f$

$[i, j] = [0, \pi/2]$

Backscattering

set $x = b$

$[i, j] = [\pi/2, \pi]$

Other scattering properties

Phase function:

$$\tilde{\beta}(\theta) = \frac{\beta(\theta)}{b} \quad \text{Units (sr}^{-1}\text{)}$$

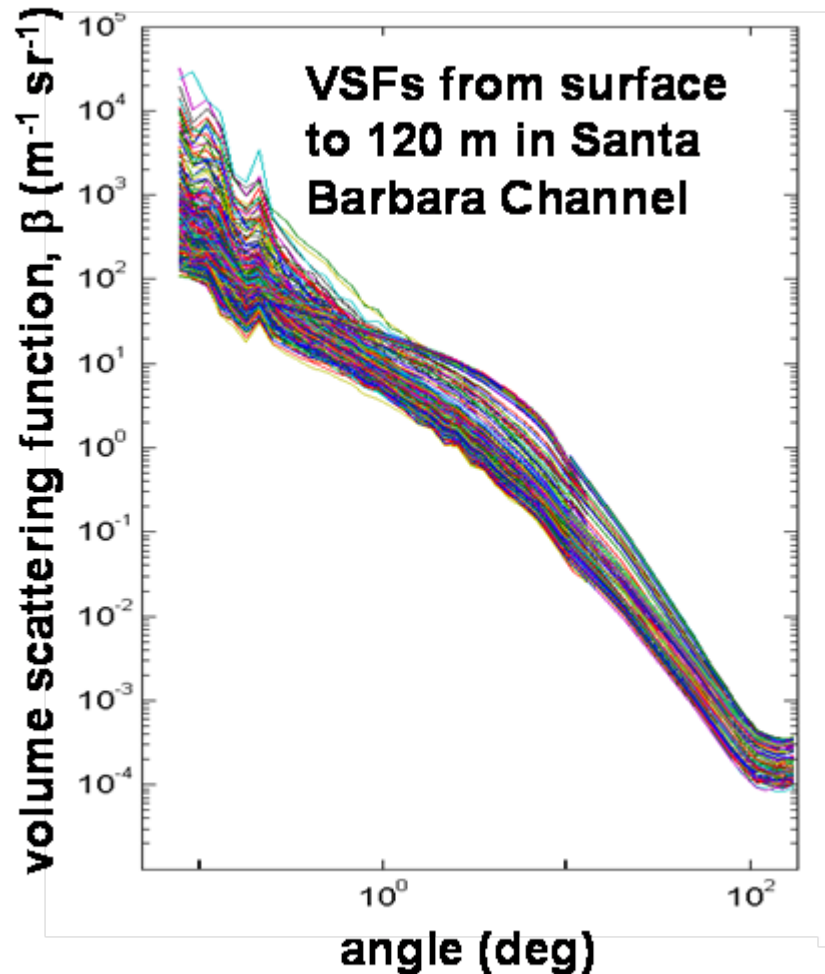
Asymmetry parameter (mean cosine):

$$g = \langle \cos(\theta) \rangle = 2\pi \int_0^{\pi} \tilde{\beta}(\theta) \cos(\theta) \sin(\theta) d\theta$$

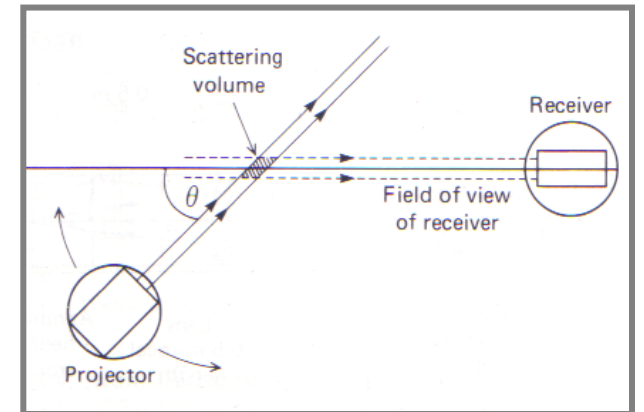
If symmetric around 90° , $g = 0$

If highly skewed $g \rightarrow 1$

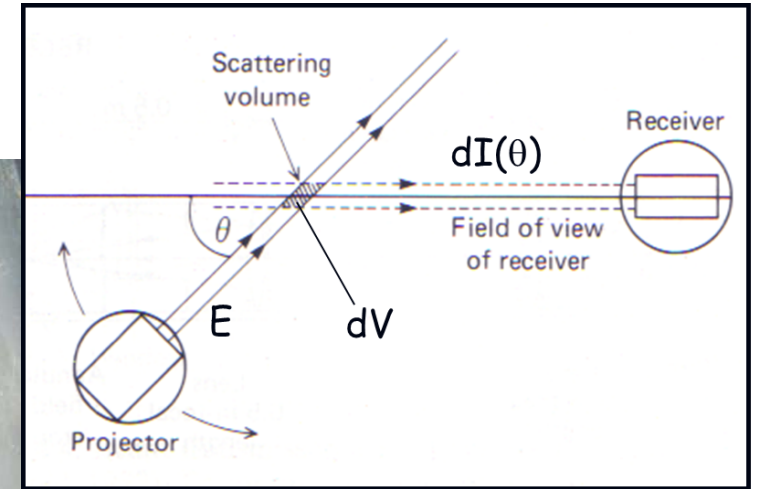
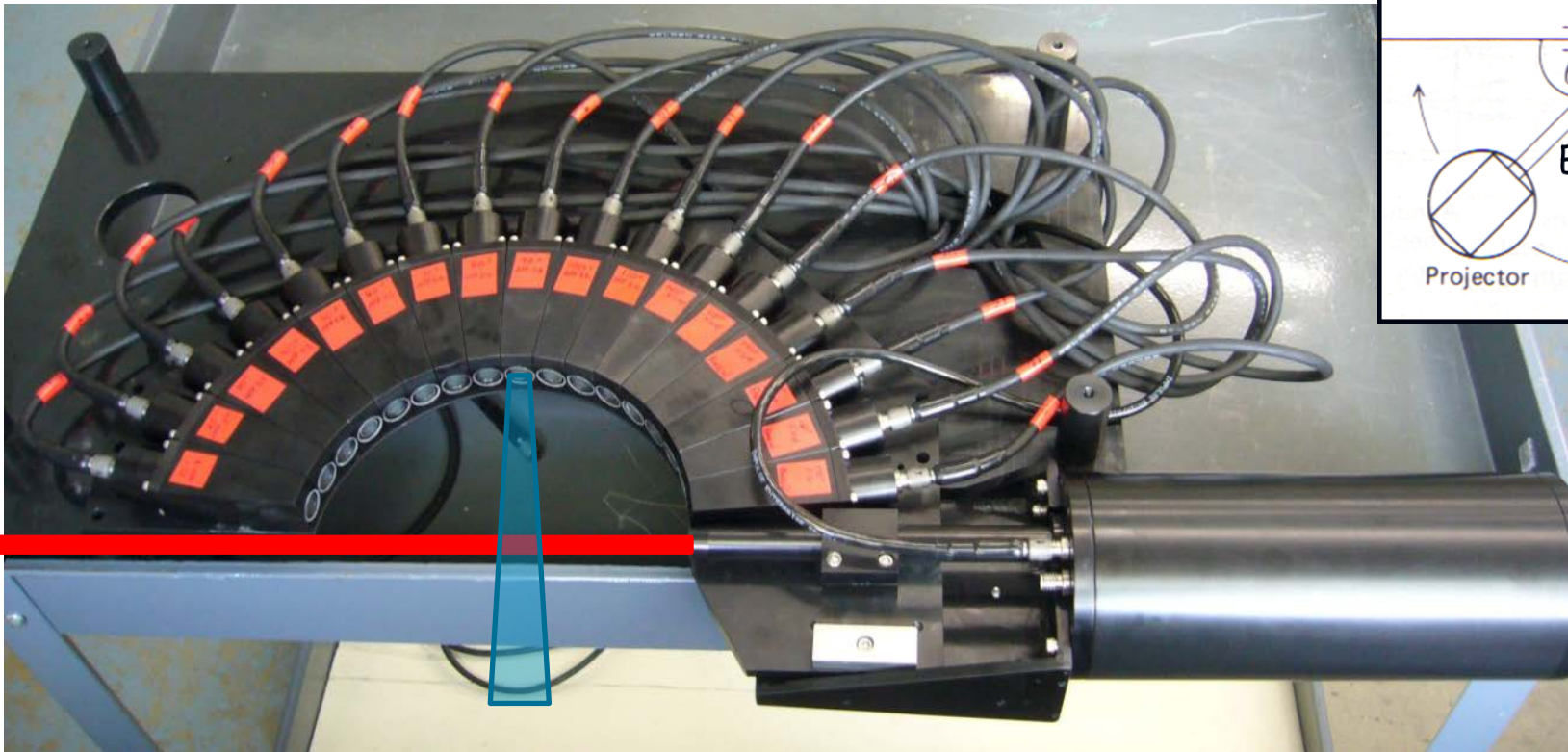
VSF Measurement Considerations



- 6+ orders of magnitude variation in intensity from the near-forward to backward in single VSF
- several orders of magnitude natural dynamic range in intensity at any single angle
- rapid temporal variability in particle fields in surface waters
- rejecting ambient light is challenging at surface, particularly for low scattering signals in the backward
- calibration without absolute “standard”

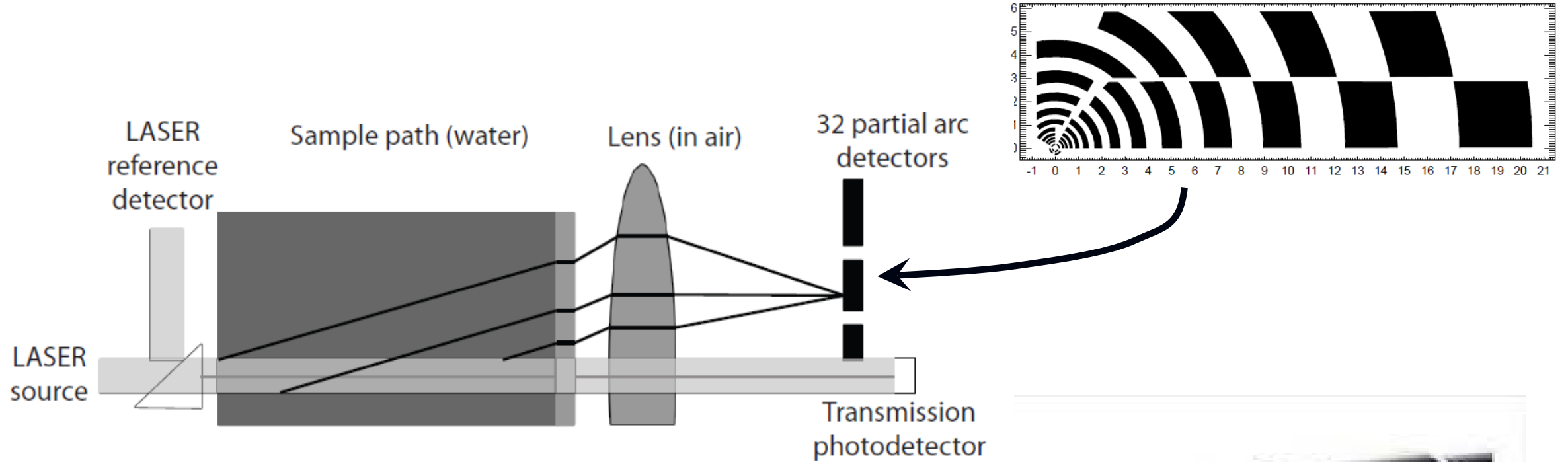


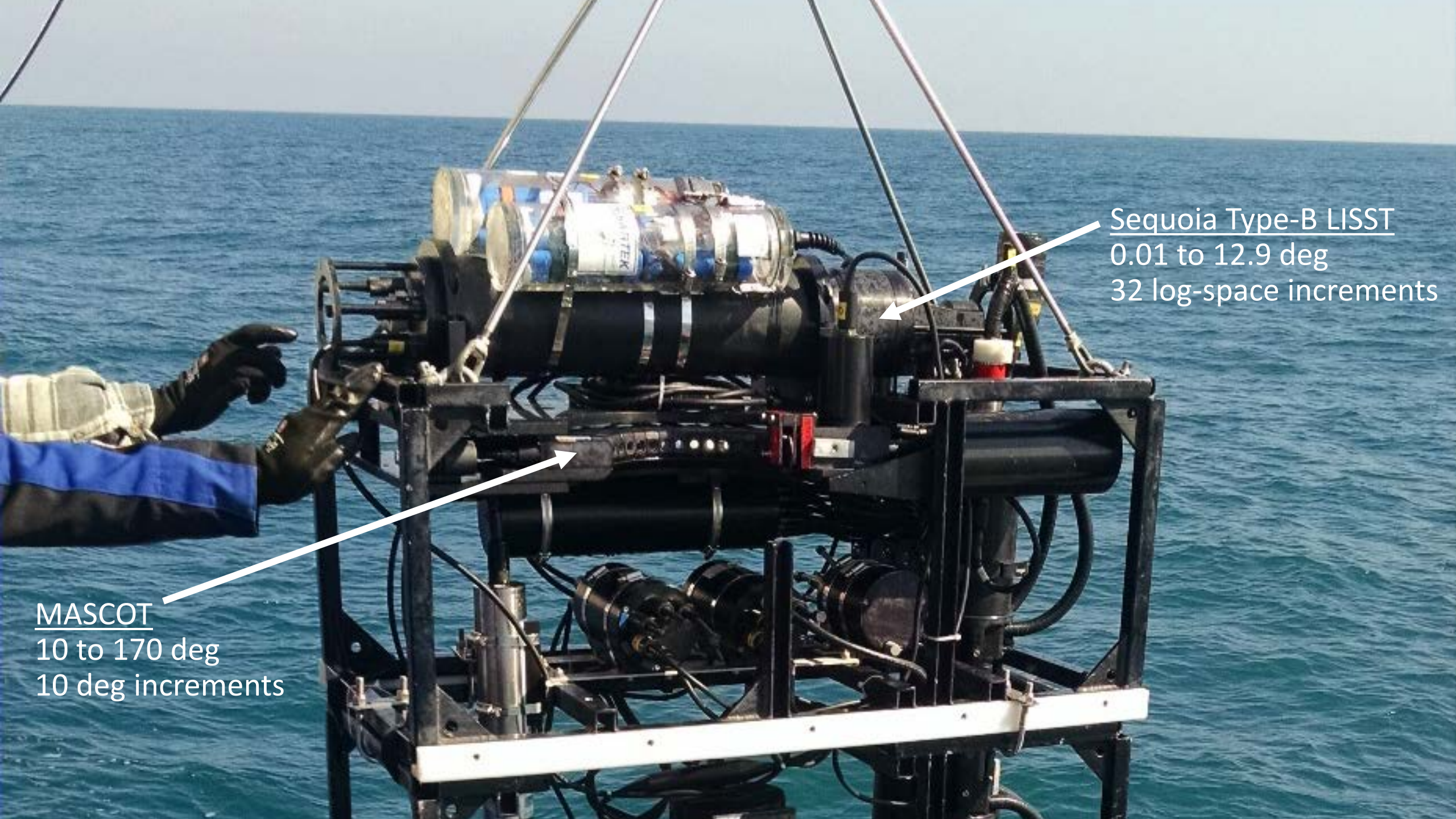
Measuring the VSF: MASCOT (HBOI)



- Measures VSF from 10° to 170°
- 0.8 - 5° detector FOVs
- 20 Hz sampling rate
- Wedge depolarizer on source

LISST-100X (Sequoia)

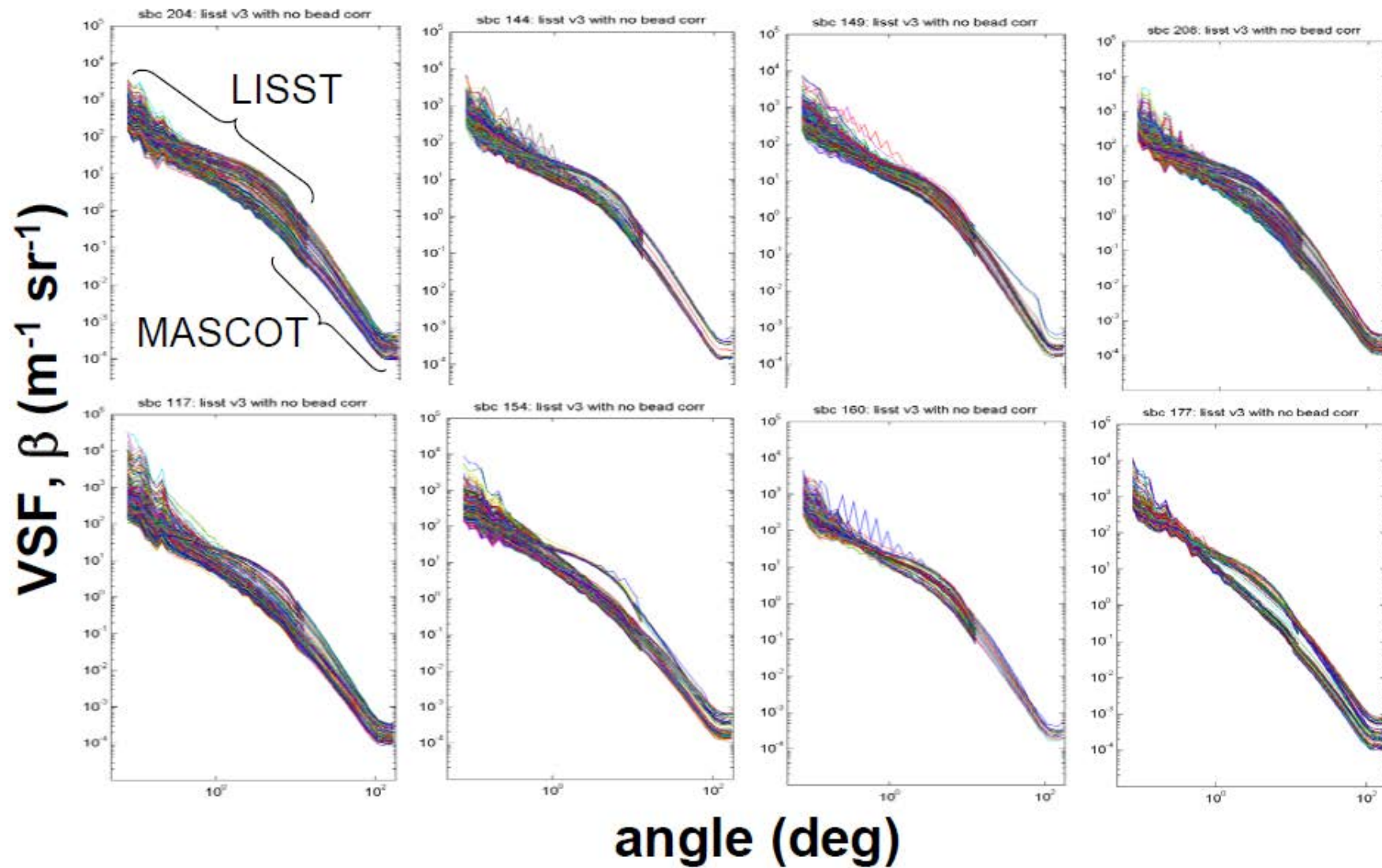




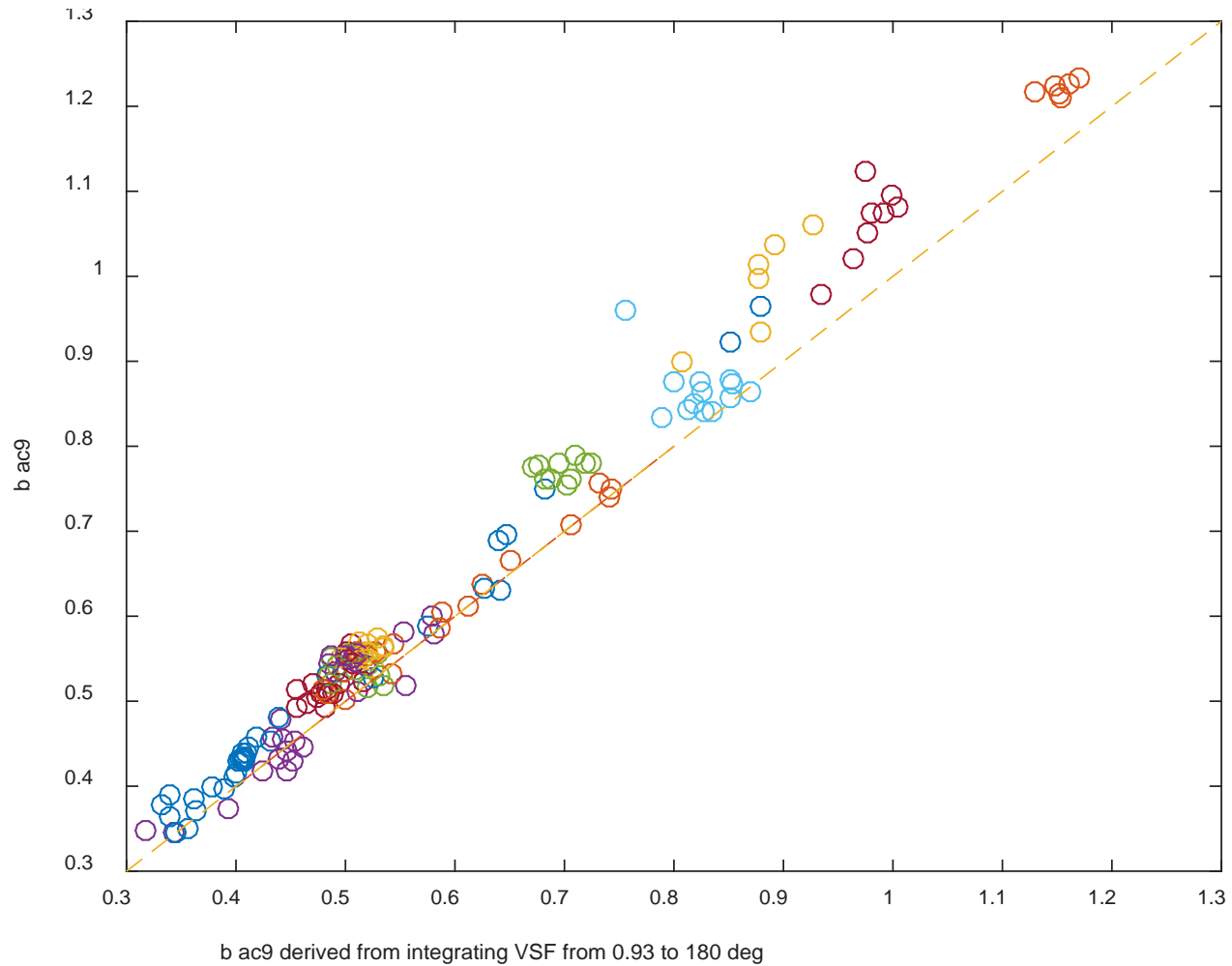
Sequoia Type-B LISST
0.01 to 12.9 deg
32 log-space increments

MASCOT
10 to 170 deg
10 deg increments

VSF profile data

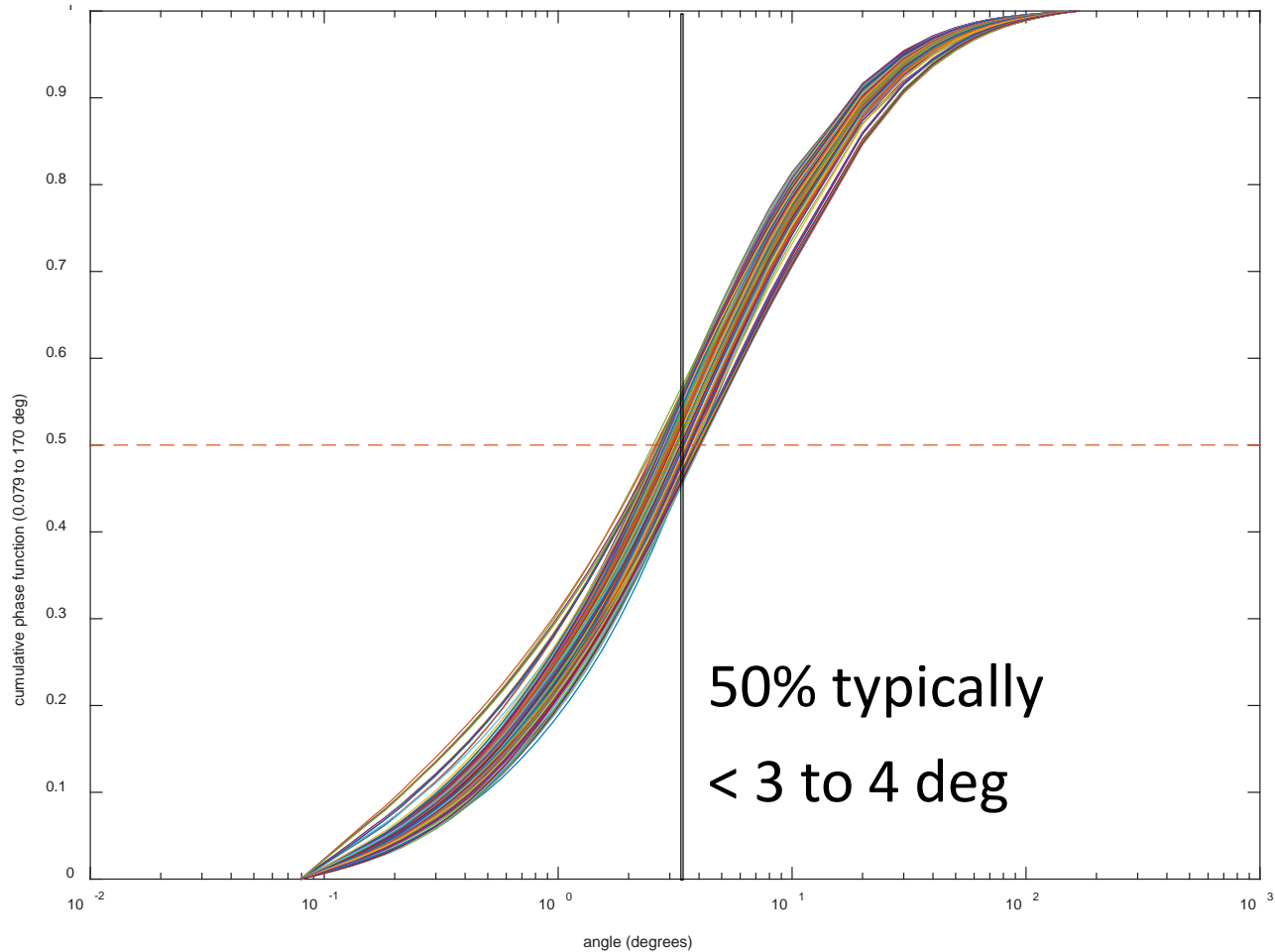


Integrating the VSF: test closure



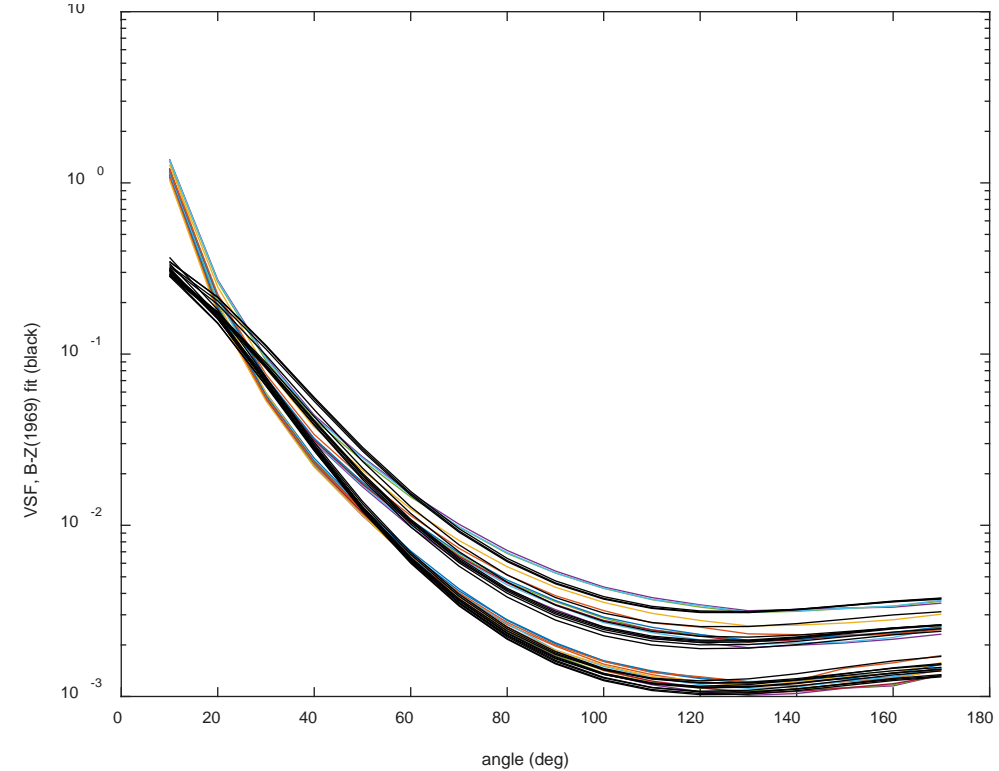
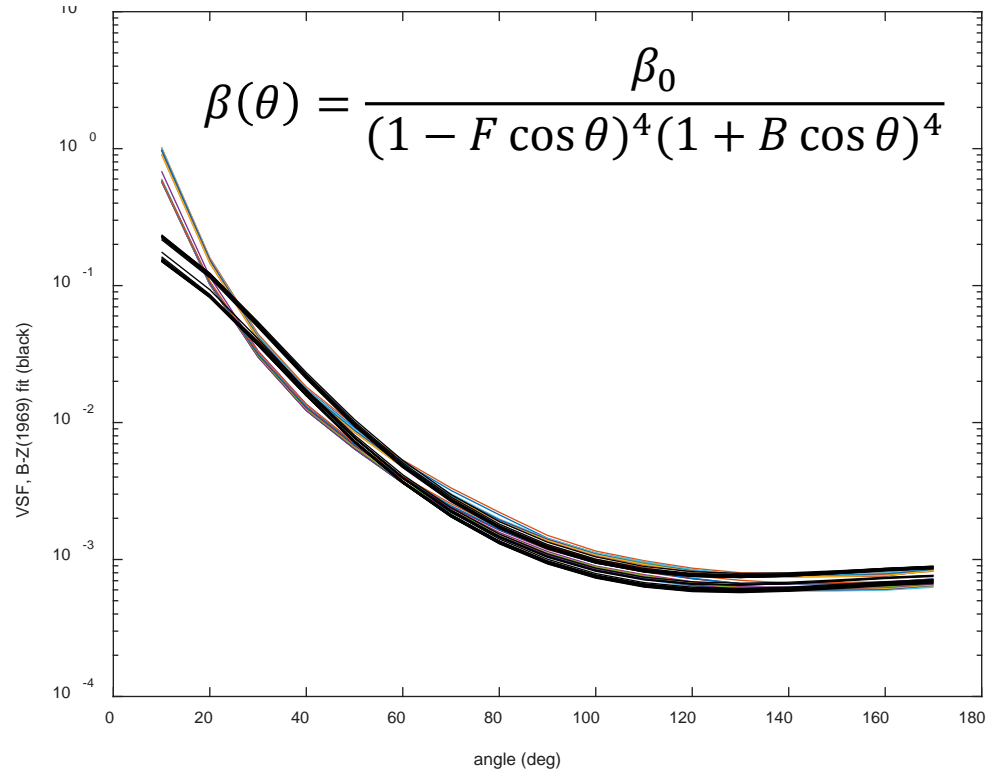
$$b_x = 2\pi \int_i^j \sin(\theta) \beta(\theta) d\theta$$

Cumulative scattering contribution



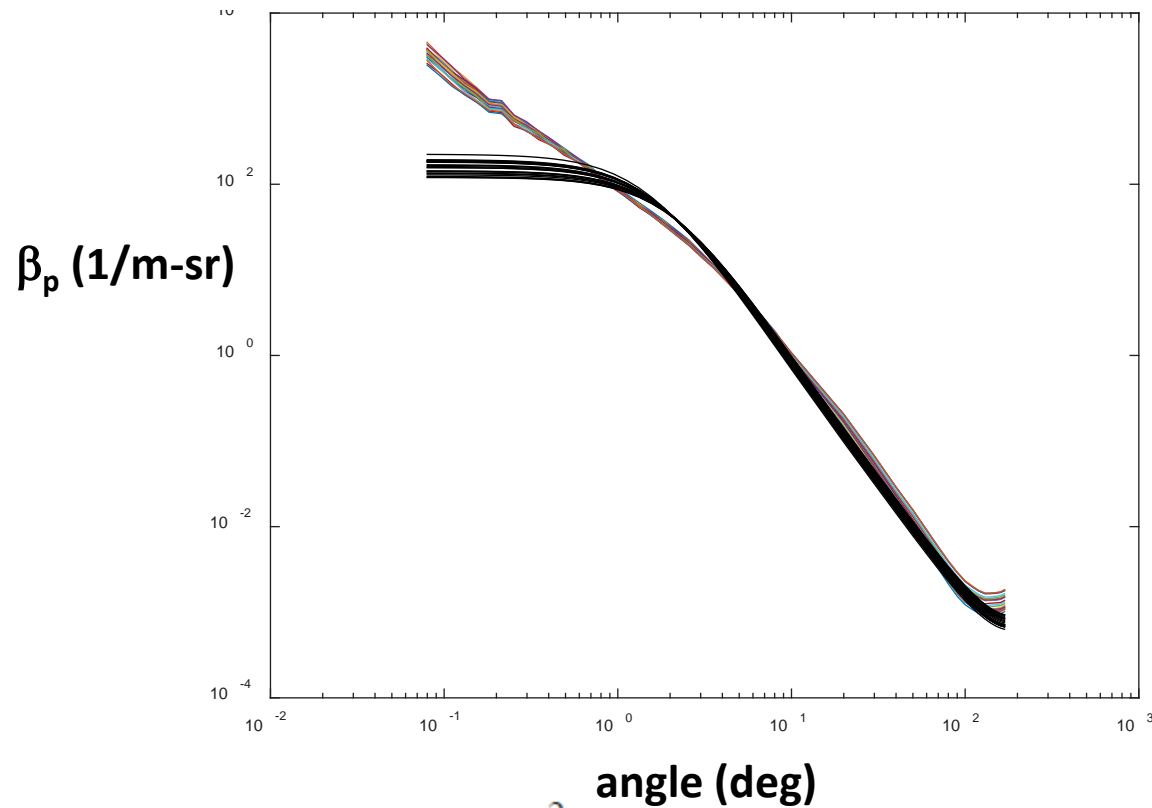
$$b_x = \frac{2\pi \int_i^j \sin(\theta) \beta(\theta) d\theta}{b}$$

Analytical modeling: Beardsley-Zaneveld (1969)

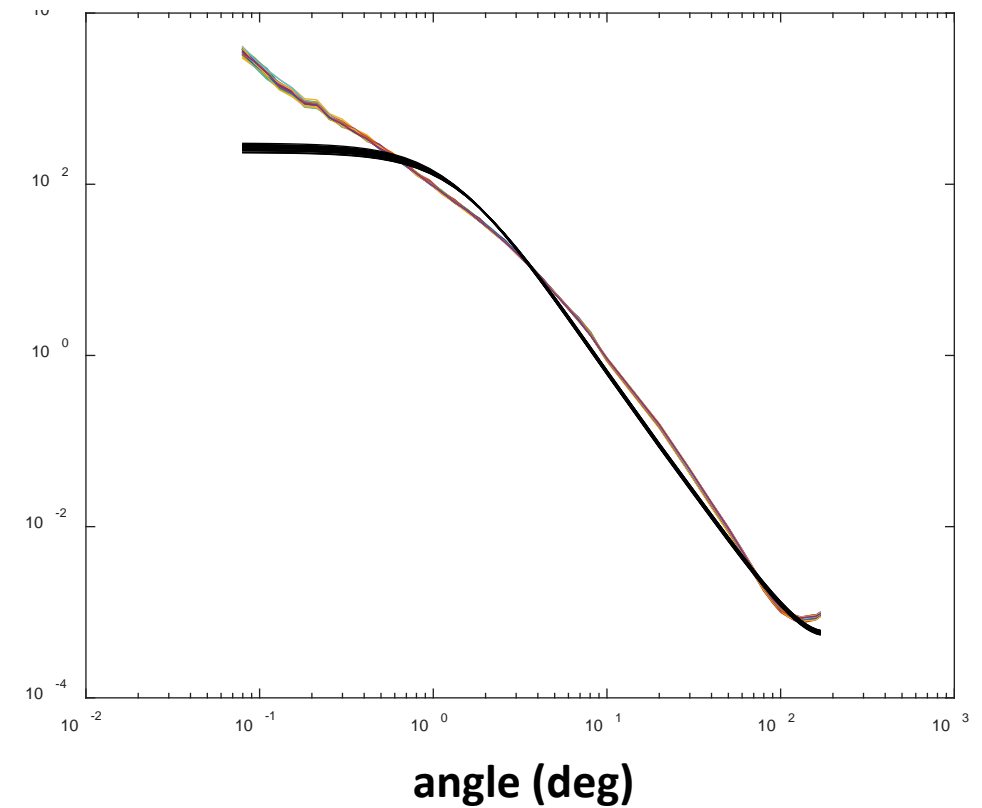


Excellent fitting algorithm in backward
(as noted by Balch et al. and others)

Analytical modeling: fitted Kattawar-Haltrin 2-term, 1-parameter Henyey-Greenstein



$$p_{HG}(\mu, g) = \frac{1 - g^2}{(1 - 2g\mu + g^2)^{3/2}}, \quad \mu = \cos \vartheta,$$



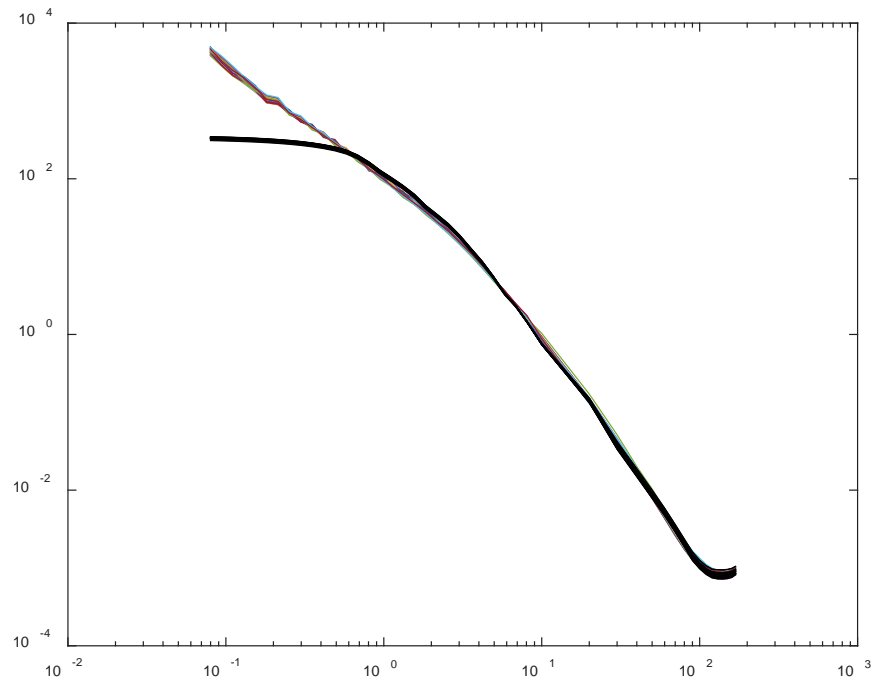
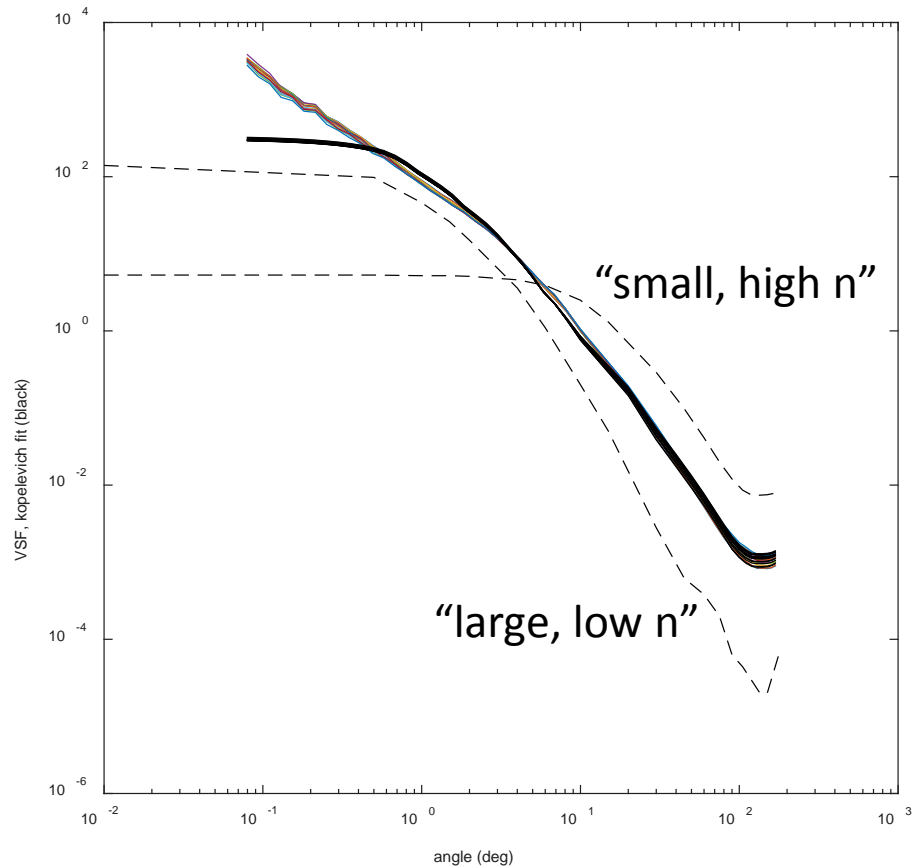
$$p_{TTHG}(\mu, \alpha, g, h) = \alpha p_{HG}(\mu, g) + (1 - \alpha) p_{HG}(\mu, -h)$$

$h(g)$ and $\alpha(g)$

$0 \leq \alpha, g, h \leq 1.$

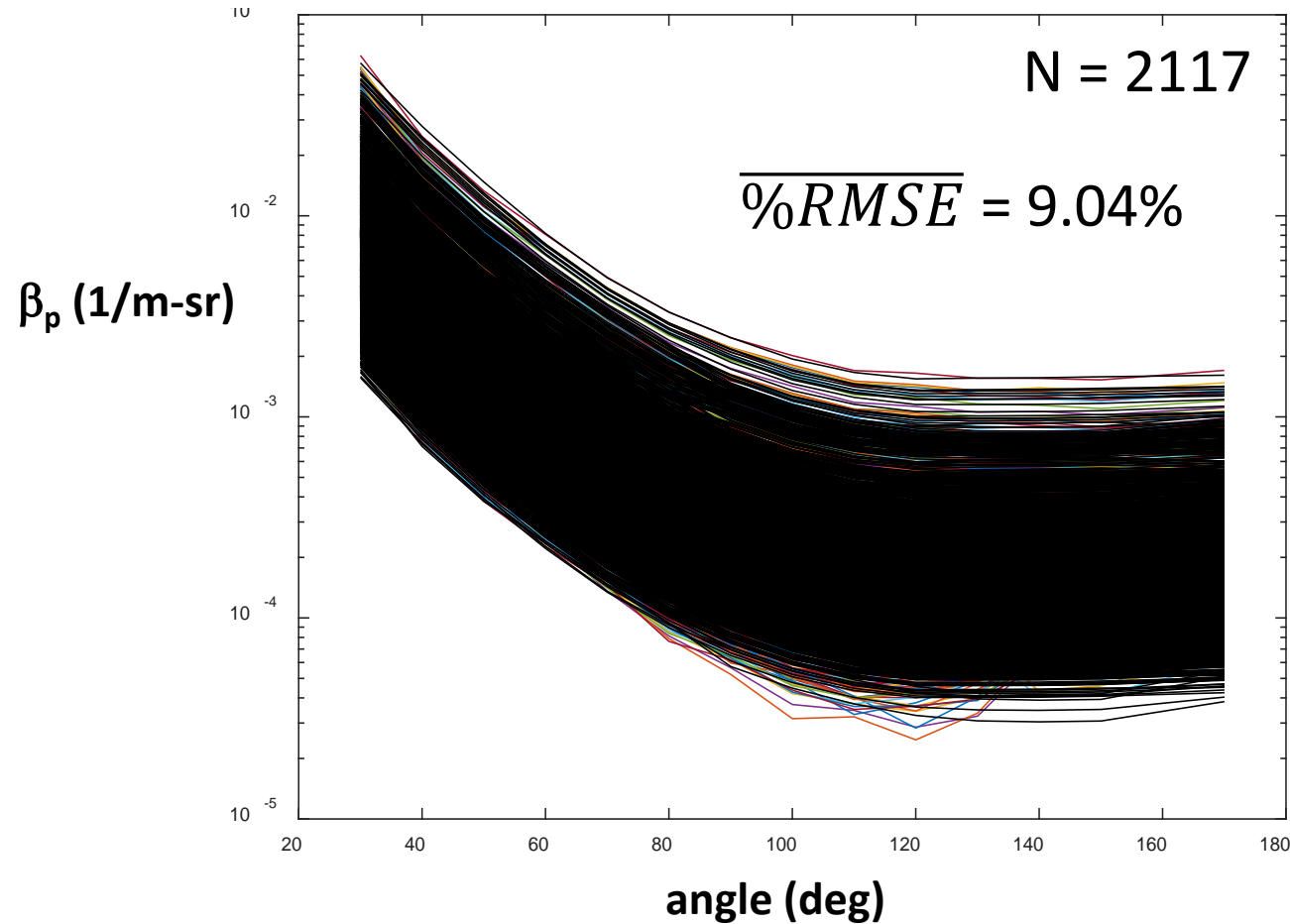
Analytical modeling: fitted Kopelevich

Fit 2 basis vectors recommended by Kopelevich (1983)



Very good results $> \sim 0.6$ deg
(as noted by Berthon et al. 2007)

Analytical modeling: fitted Kopelevich



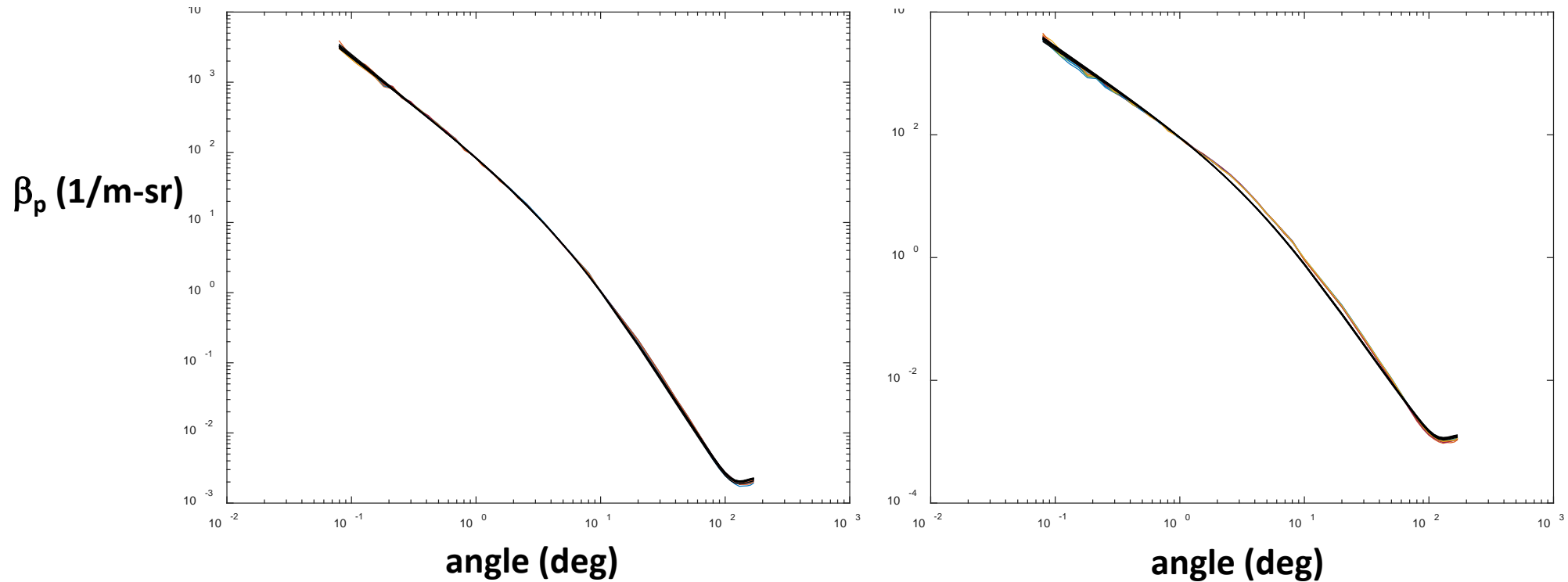
SABOR

NW Atlantic 08/2014

>10 deg only

Analytical modeling: fitted Fournier-Forand (1994, 1999)

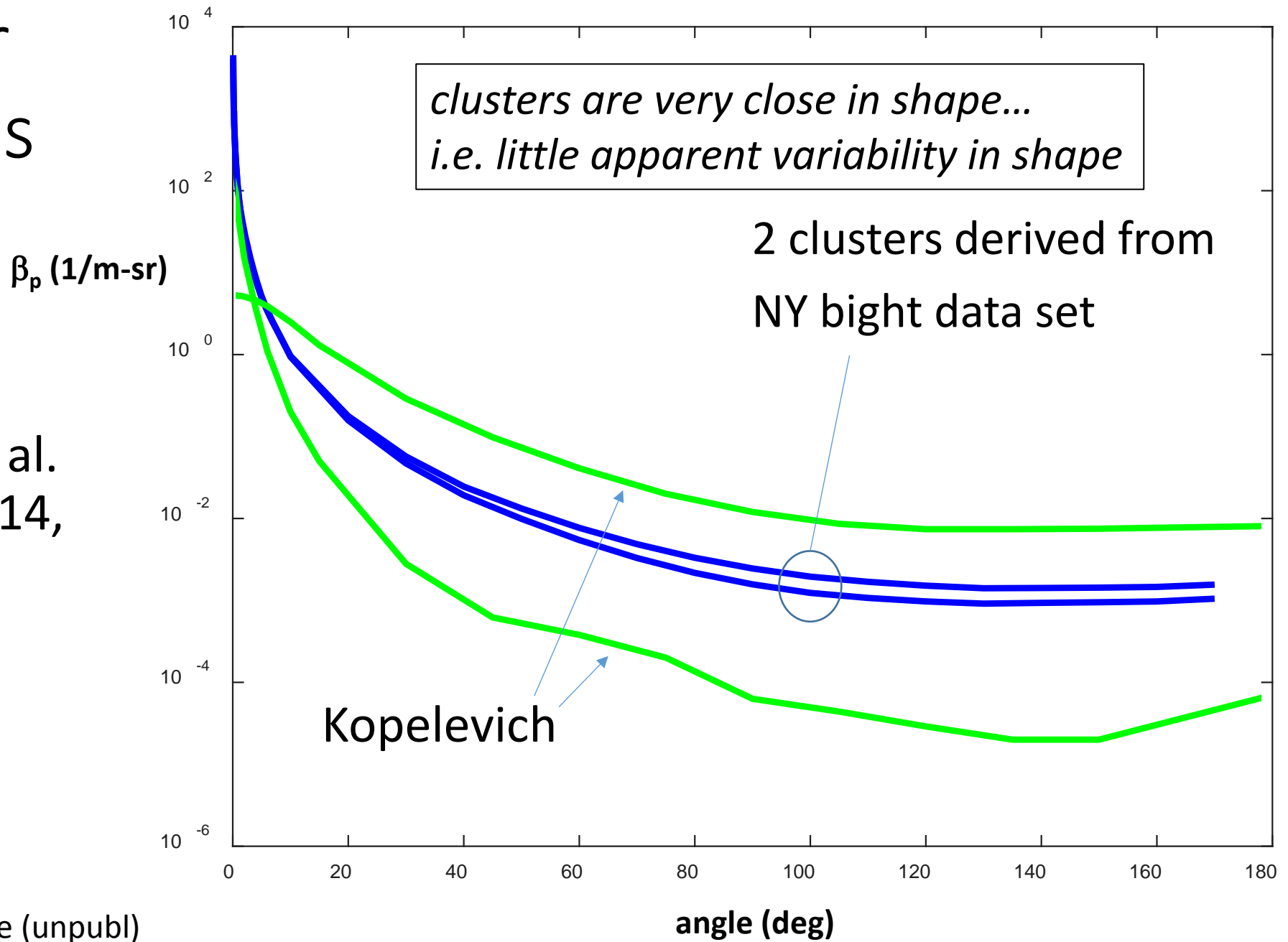
see Jonasz and Fournier (2007, with erratum)



Excellent fits for entire angular range (0.079 to 180 deg)

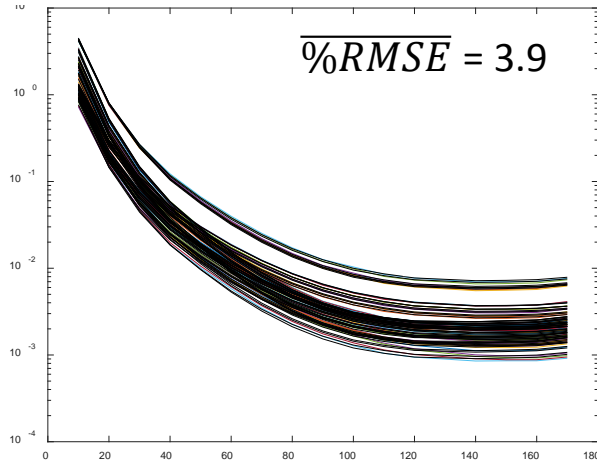
Cluster analysis

After
Moore et al.
(2009, 2014,
2015)

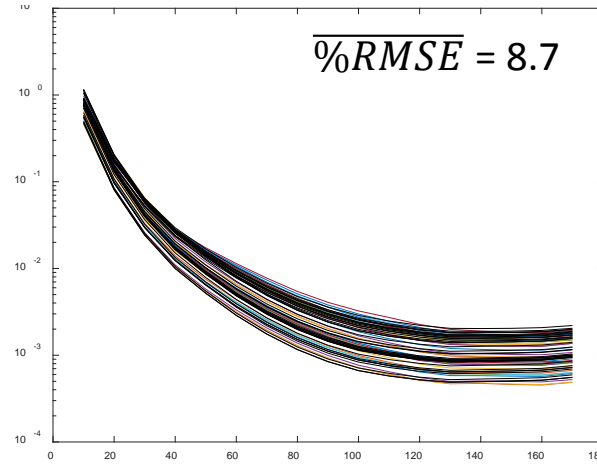


Fitting 2 clusters from NY Bight 11/2007

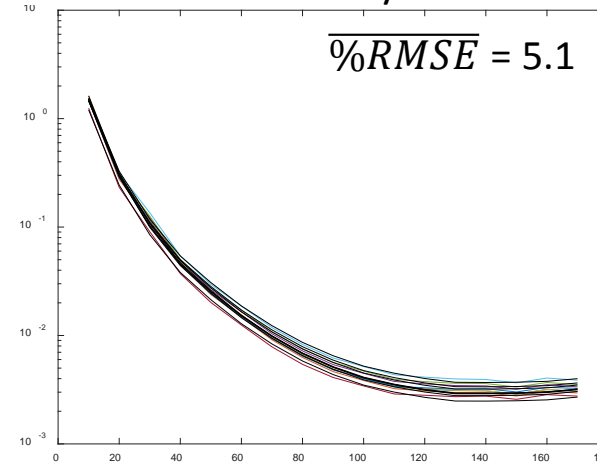
NY Bight 07/2008



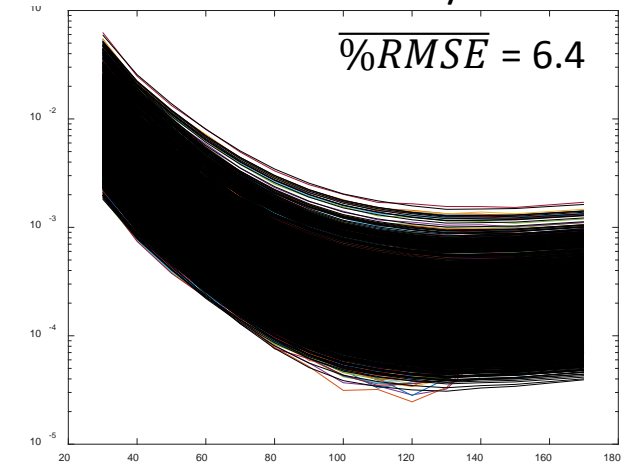
San Diego 01/2008



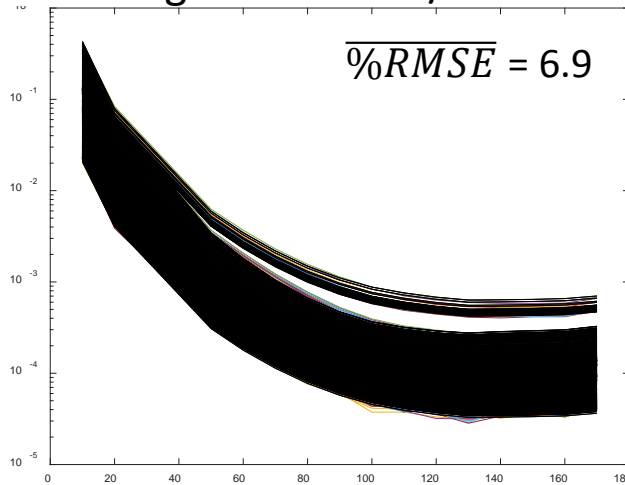
Lake Erie 08/2014



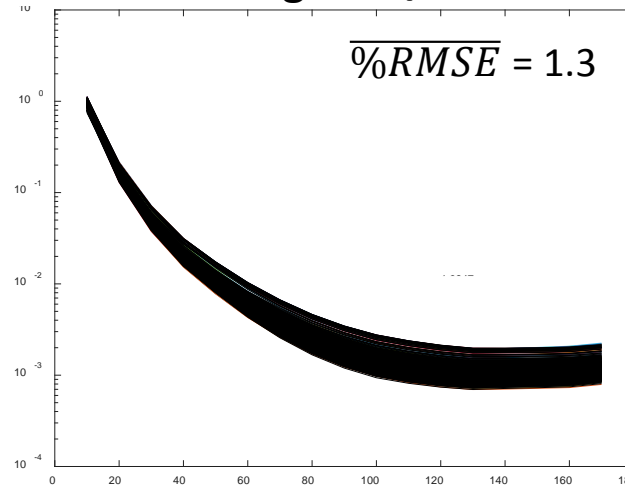
NW Atlantic 08/2014



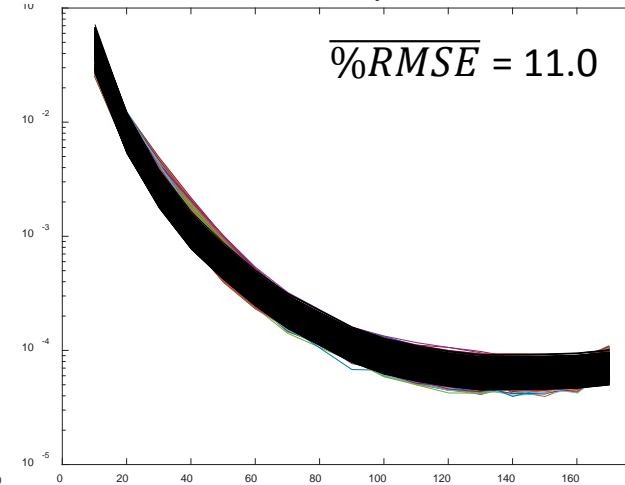
Ligurian Sea 10/2008



NY Bight 11/2007

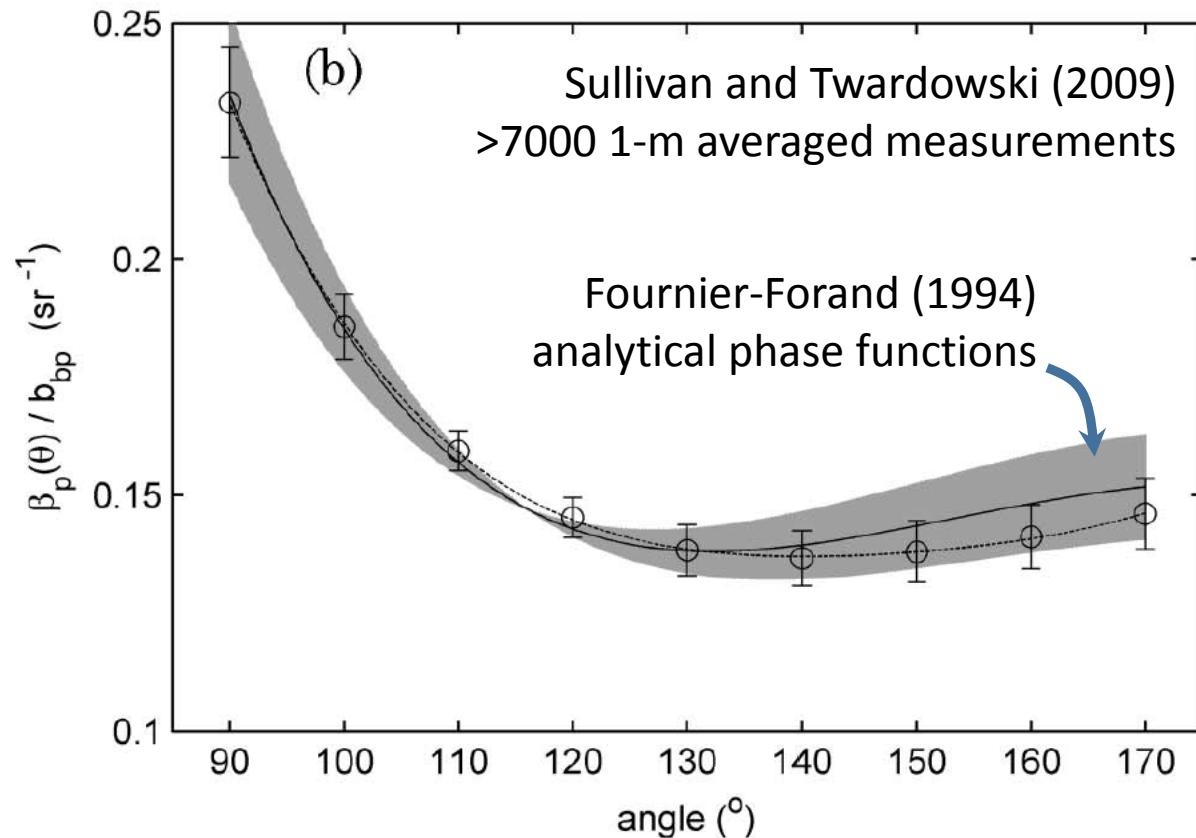


Hawaii 09/2009

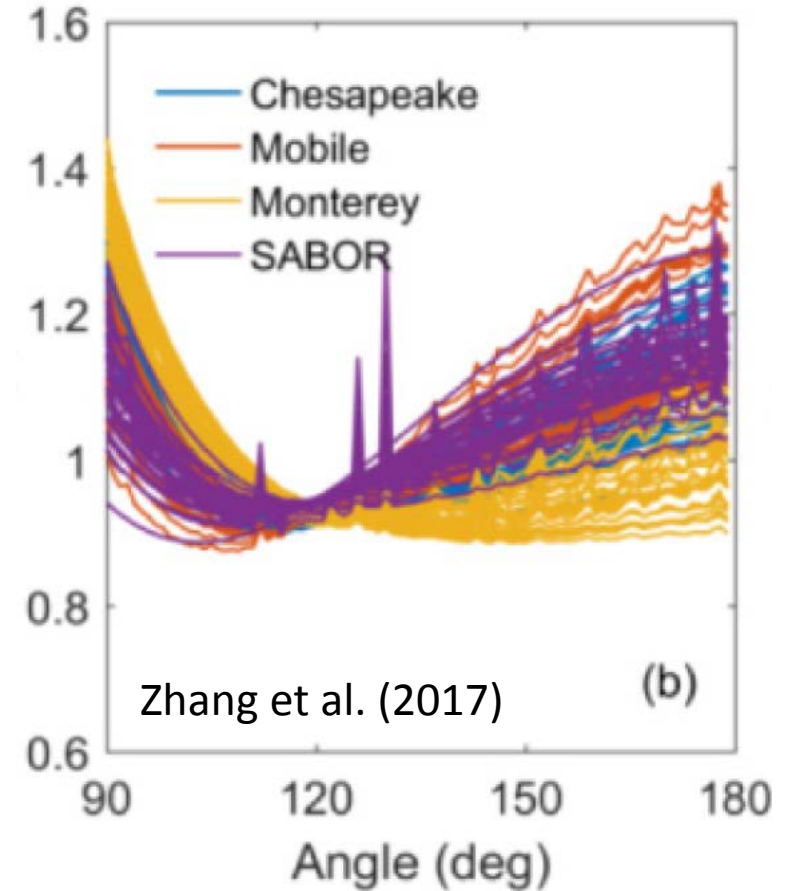


>10 deg only

Backward phase function (i.e., VSF shape)

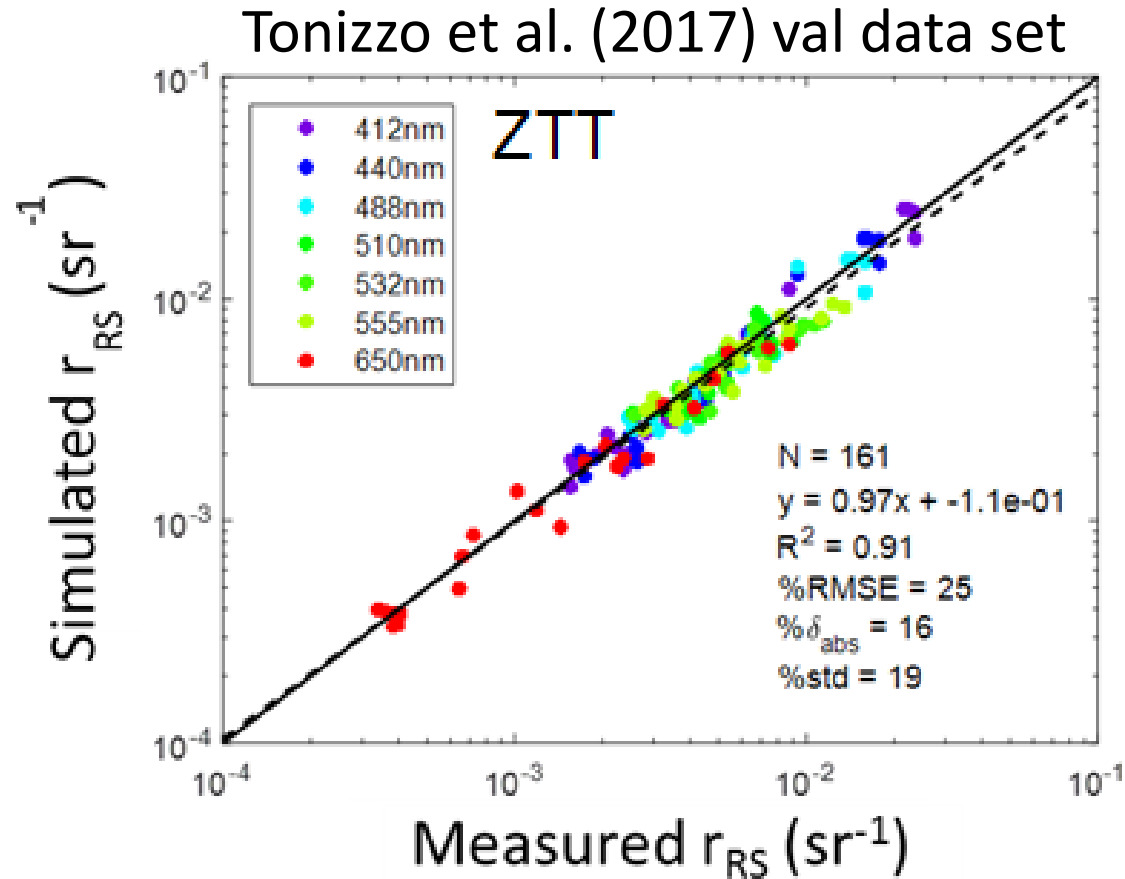


Remarkably consistent shape...
Important implications for ocean color remote sensing



However, some inconsistency
in current literature...

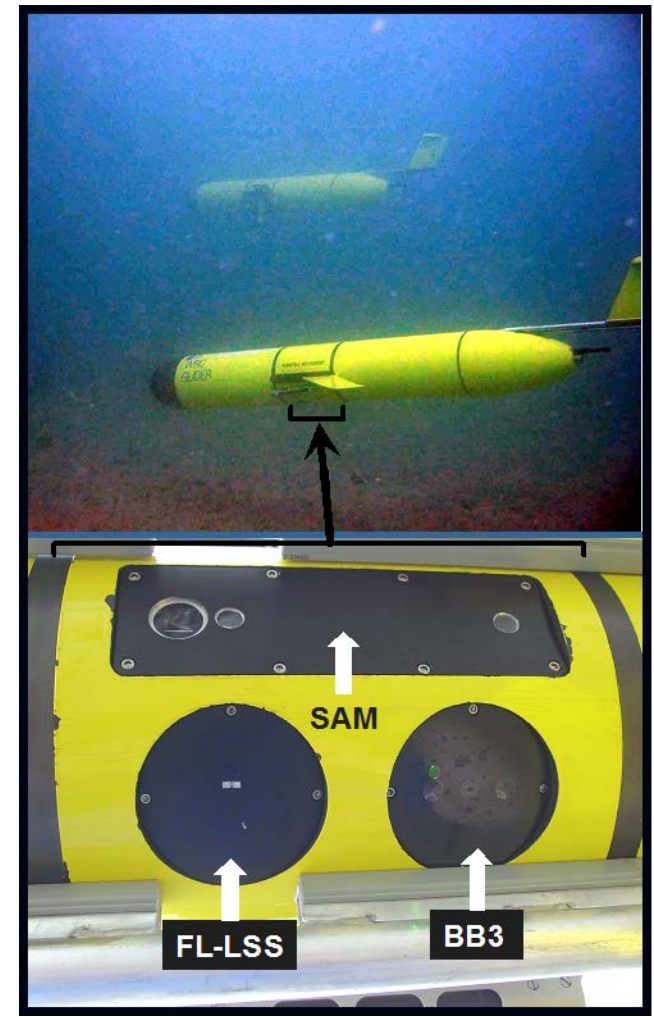
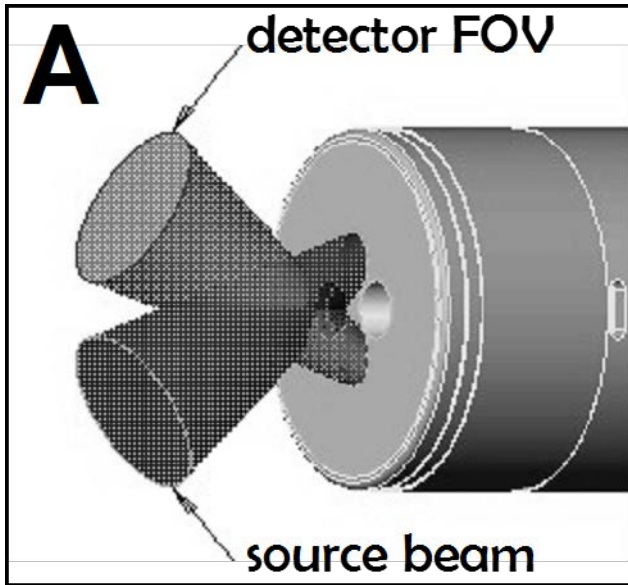
Constant backward VSF shape appears realistic...



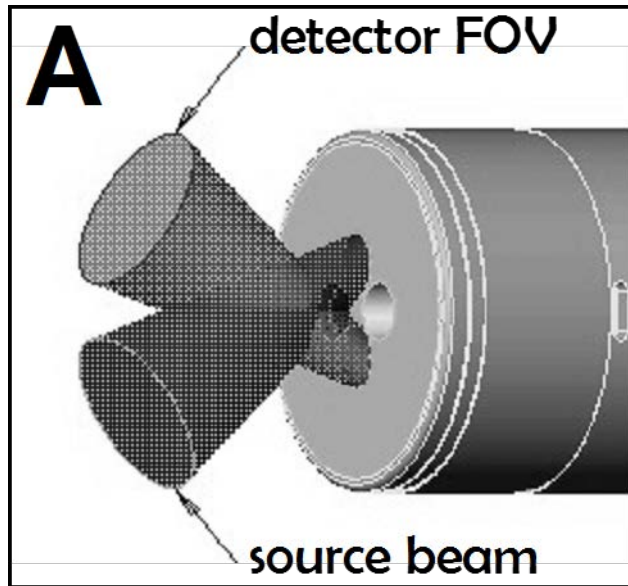
Radiative transfer simulations assuming constant backward VSF shape

Results are equivalent to simulations using measured VSFs

Measuring the VSF: WET Labs ECOs

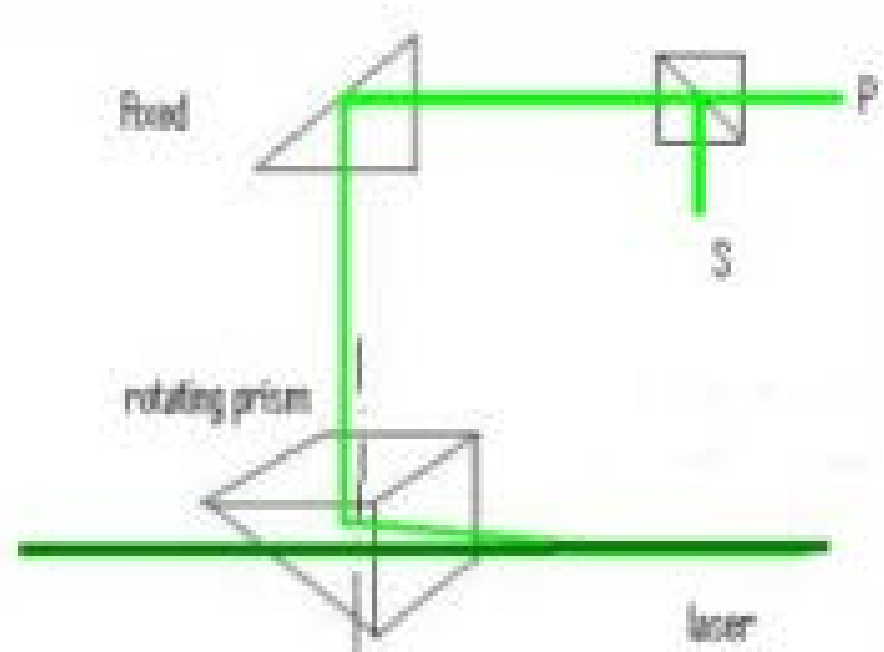


Measuring the VSF: IMO-SC6



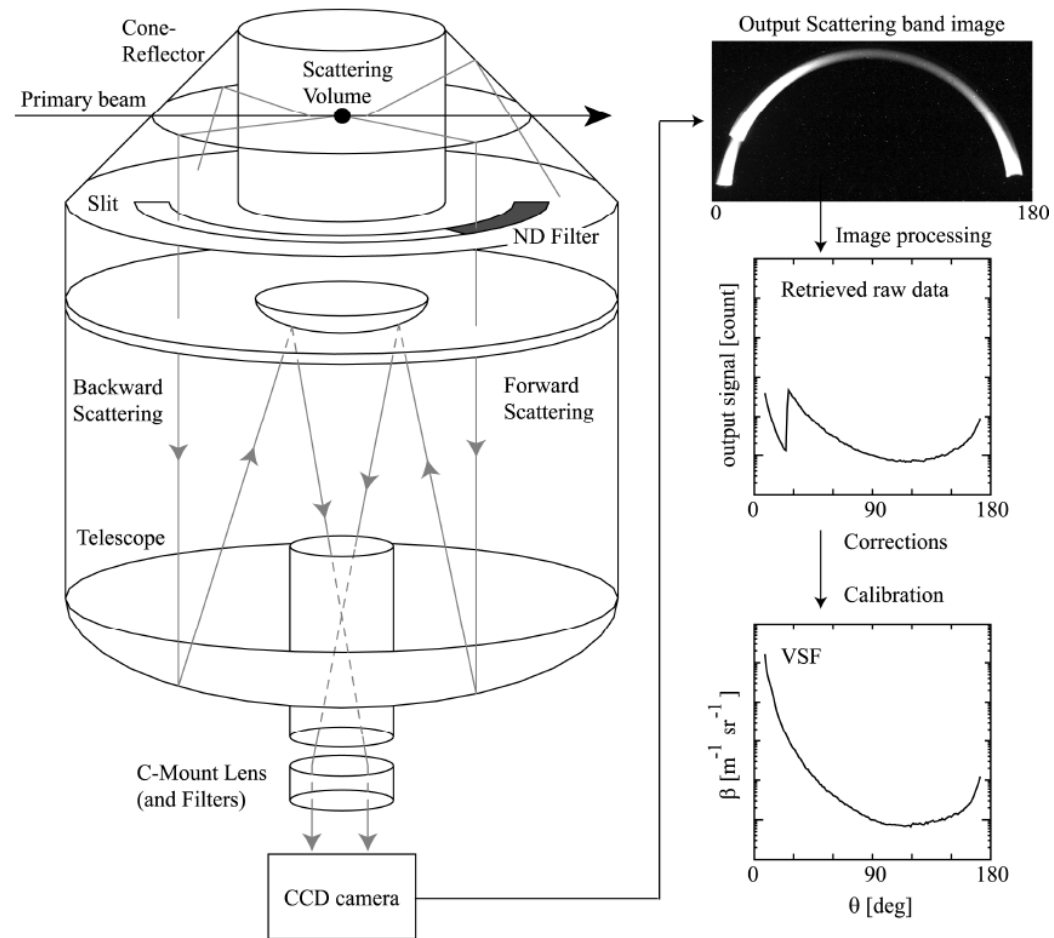
6 wavelengths, centroid angle ~ 120 deg

LISST-VSF (Sequoia)



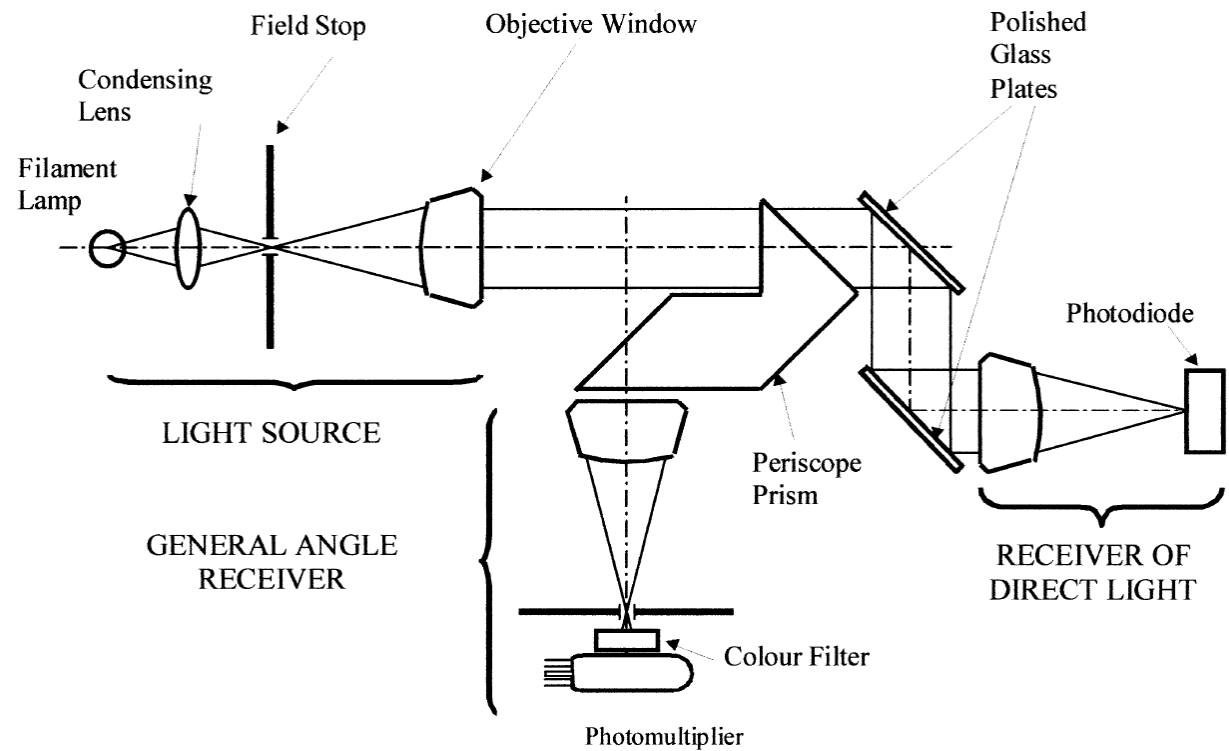
I-VSF

Helmholtz-Zentrum Geesthacht (HZG)

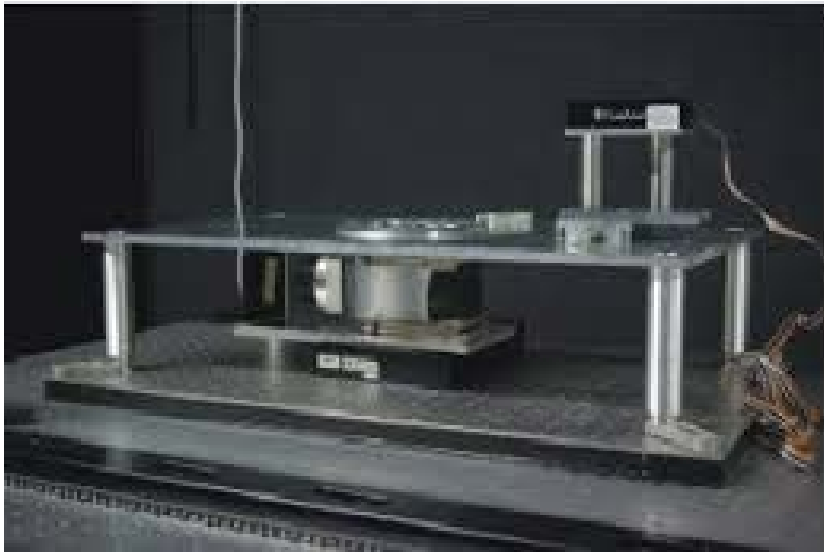


Measuring the VSF: MVSM

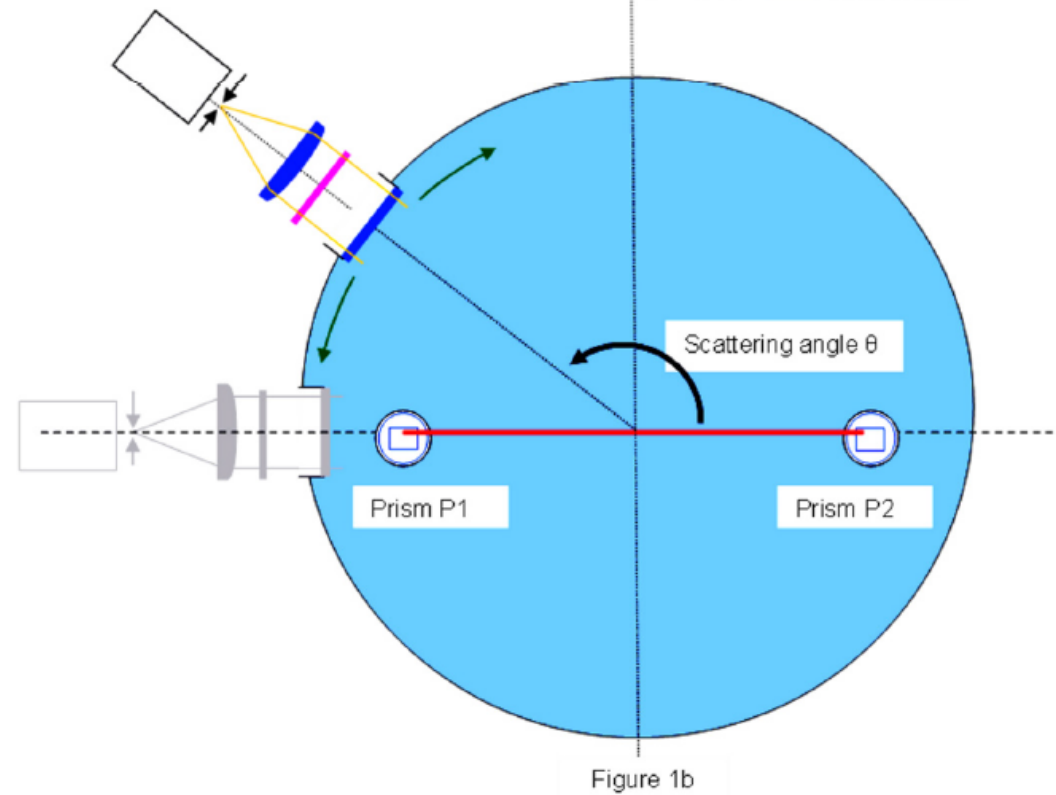
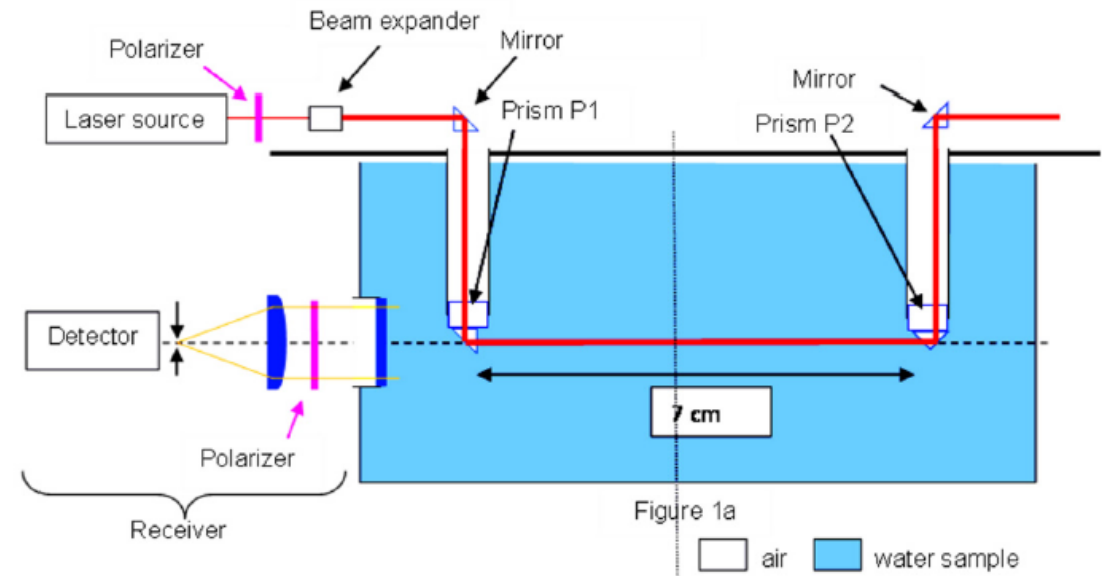
(Marine Hydrophysical Institute, Academy of Sciences of the Ukraine)



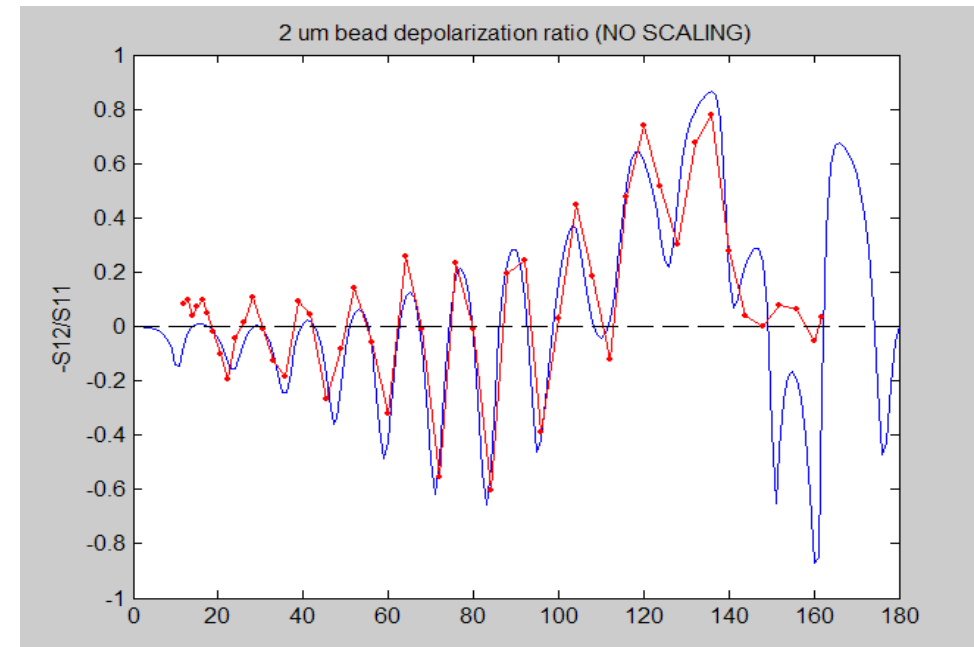
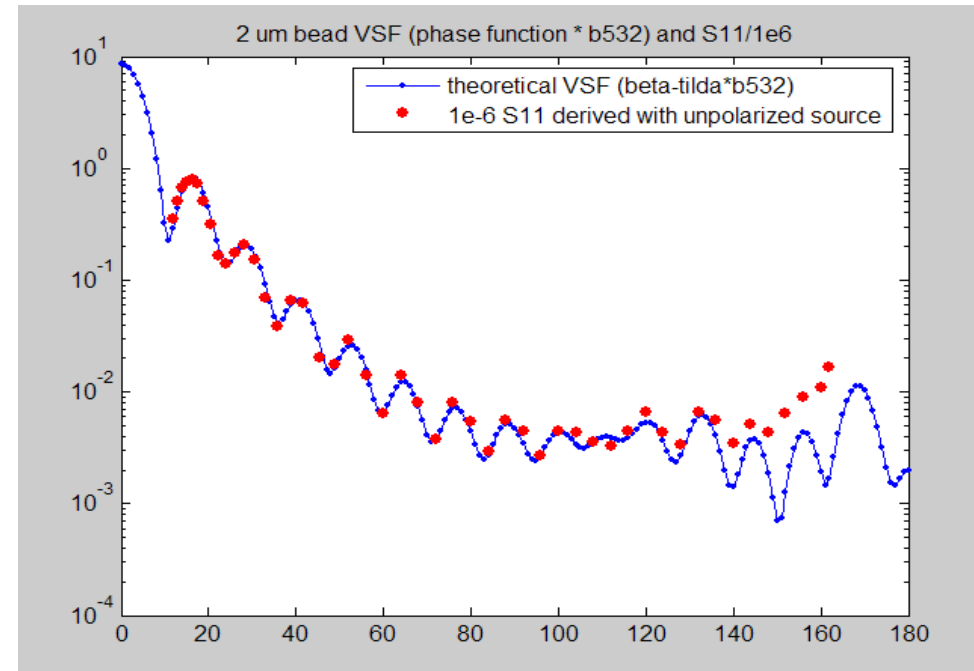
POLVSM (LOV)



Chami et al. (2014)
Harmel et al. (2015)



BI-200 Goniometer (Brookhaven)



Near $\beta(180)$, coherent scattering

Phases interact in a constructive way to enhance scattering near 180 deg

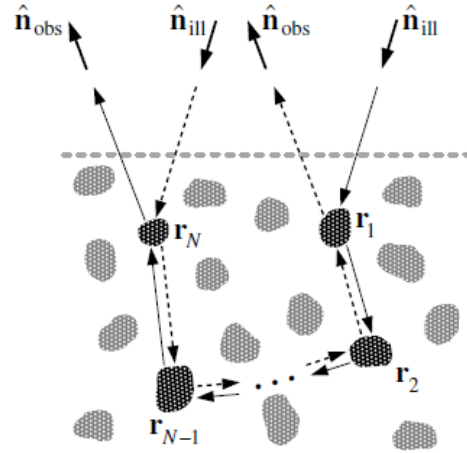


Figure 3.3. Schematic explanation of coherent backscattering.

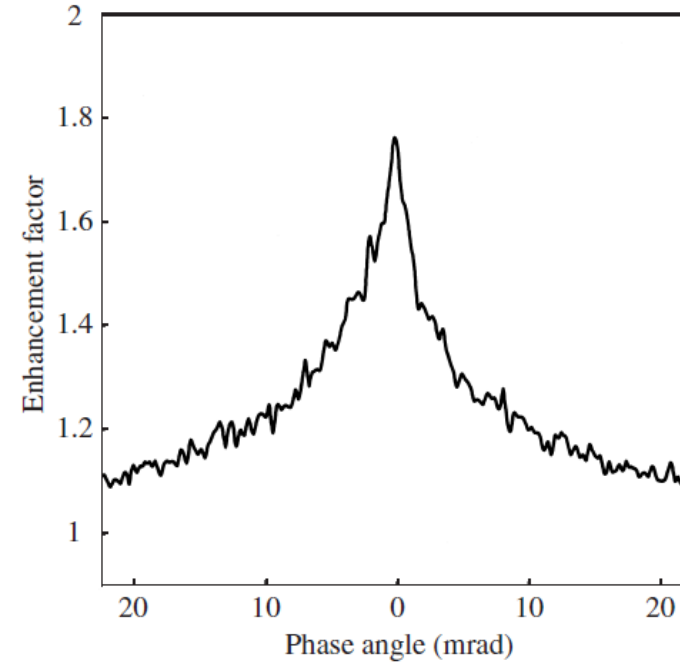
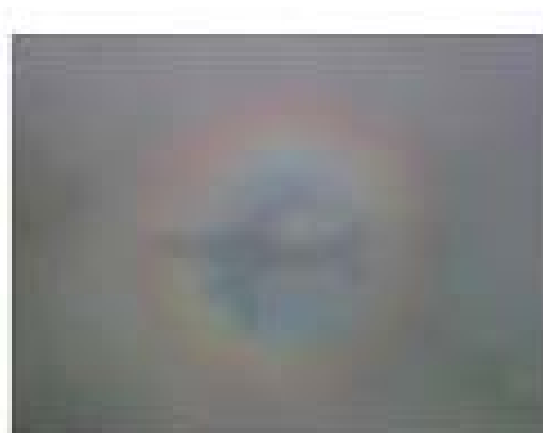


Figure 3.5. Angular profile of the coherent backscattering peak produced by a 1500- μm -thick slab of 9.6 vol% of 0.215- μm -diameter polystyrene spheres suspended in water. The slab was illuminated by a linearly polarized laser beam ($\lambda_1 = 633 \text{ nm}$) incident normally to the slab surface. The scattering plane (i.e., the plane through the vectors $\hat{\mathbf{n}}_{\text{ill}}$ and $\hat{\mathbf{n}}_{\text{obs}}$, Fig. 3.3) was fixed in such a way that the electric vector of the incident beam vibrated in this plane. The detector measured the component of the backscattered intensity polarized parallel to the scattering plane. The curve shows the profile of the backscattered intensity normalized by the intensity of the incoherent background as a function of the phase angle. The latter is defined as the angle between the vectors $\hat{\mathbf{n}}_{\text{obs}}$ and $-\hat{\mathbf{n}}_{\text{ill}}$. (After van Albada *et al.* 1987.)

“Turbidity” ? “NTU” measurements...?

- Typically a measurement of scattering $\sim 90^\circ$ but many sensors use angles $> 90^\circ$
- Spectral characteristics vary (“white light,” 880 nm, etc.)
- Angular weighting ($\Delta\theta$) varies
- Calibrated to formazin particles (phase function looks nothing like that of the real ocean)

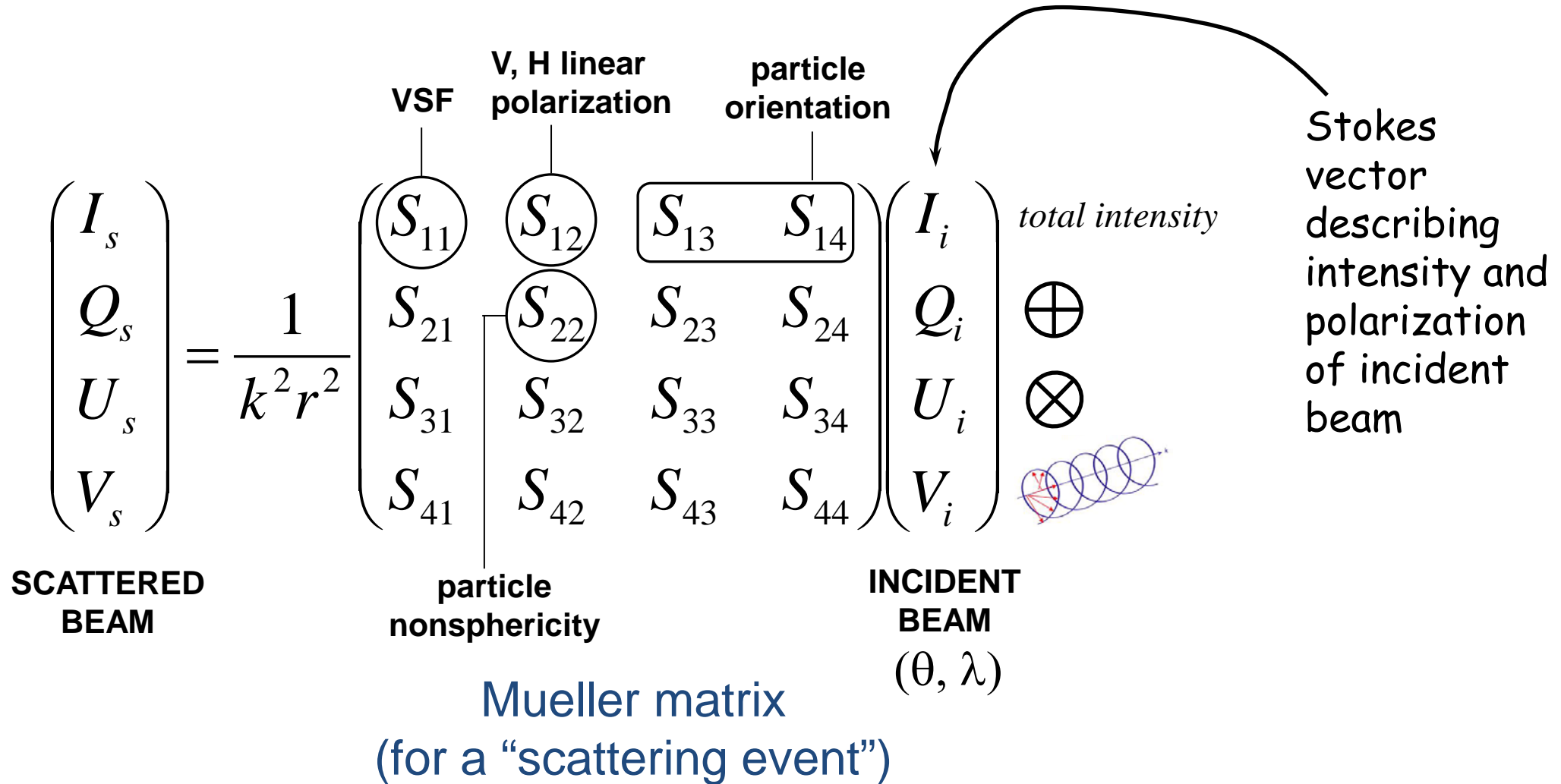
So what does this mean?

Virtually every turbidity measurement, and NTU, is different.

Turbidity is not “water clarity” (c is best for estimating this).

Signal may be correlated with backscattering.

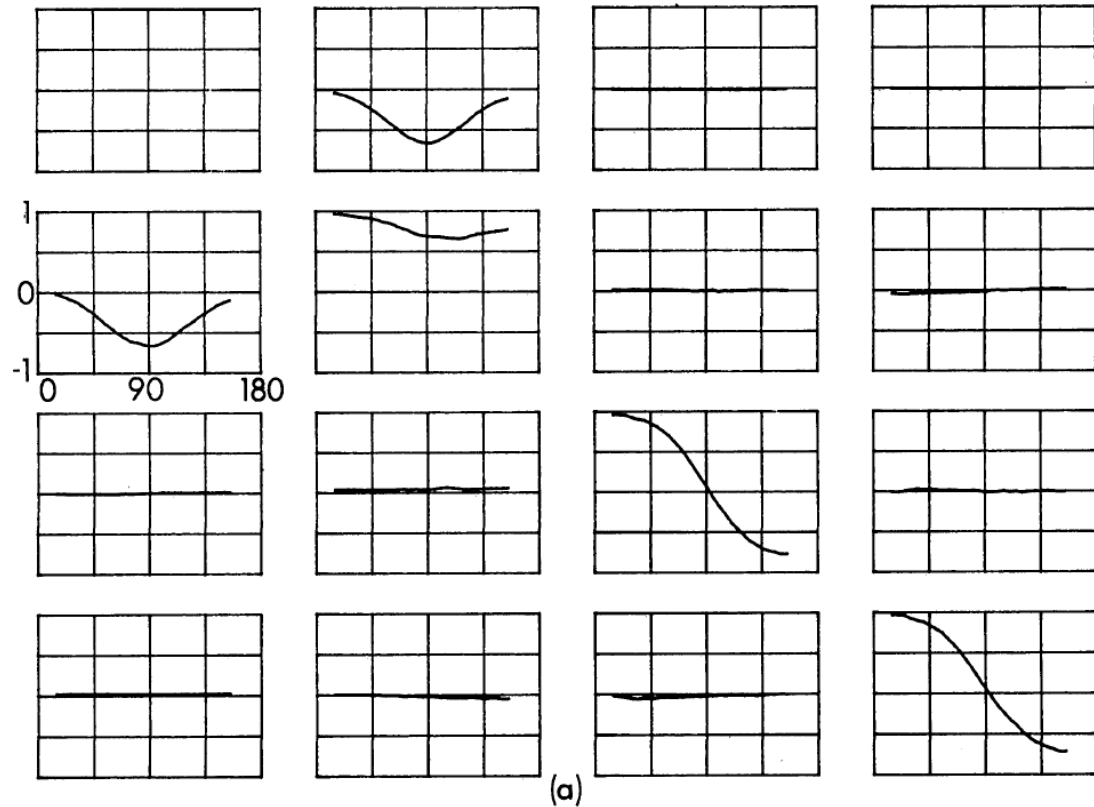
Polarized scattering



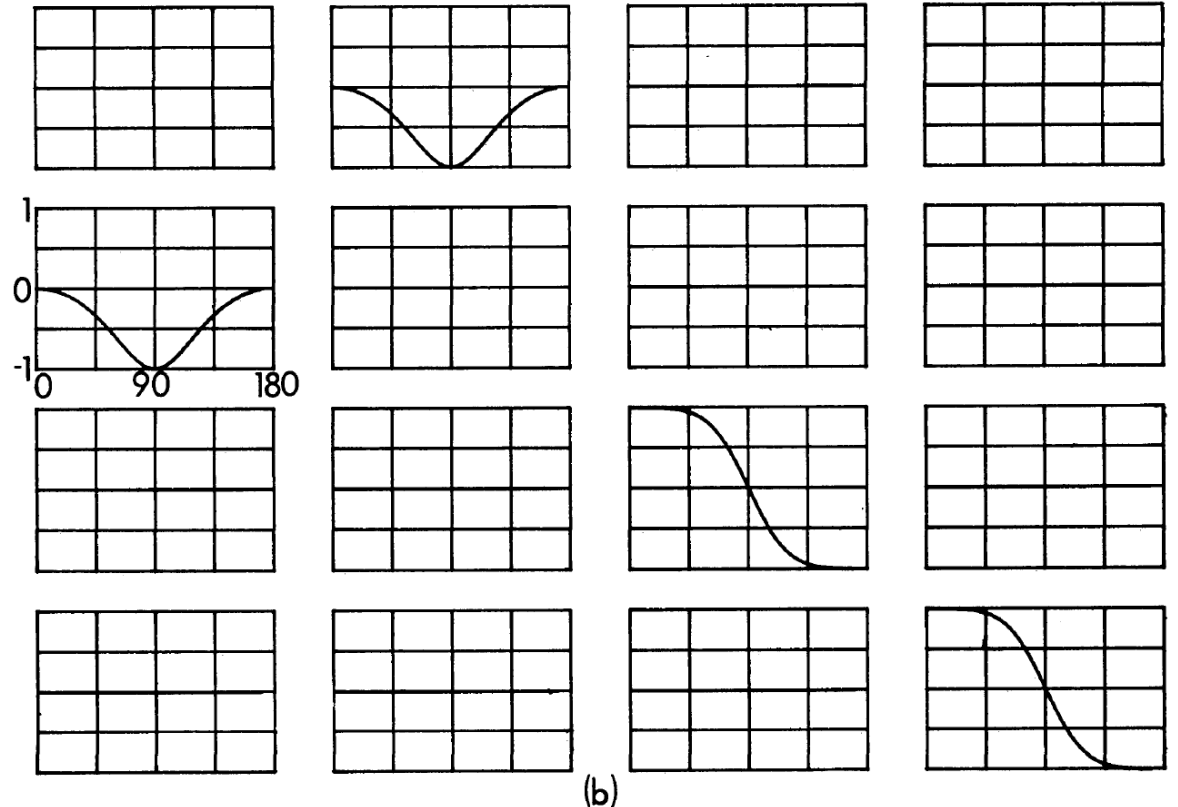
Every element has wavelength and angular dependencies

Mueller matrix: Voss and Fry (1984)

All normalized to S11



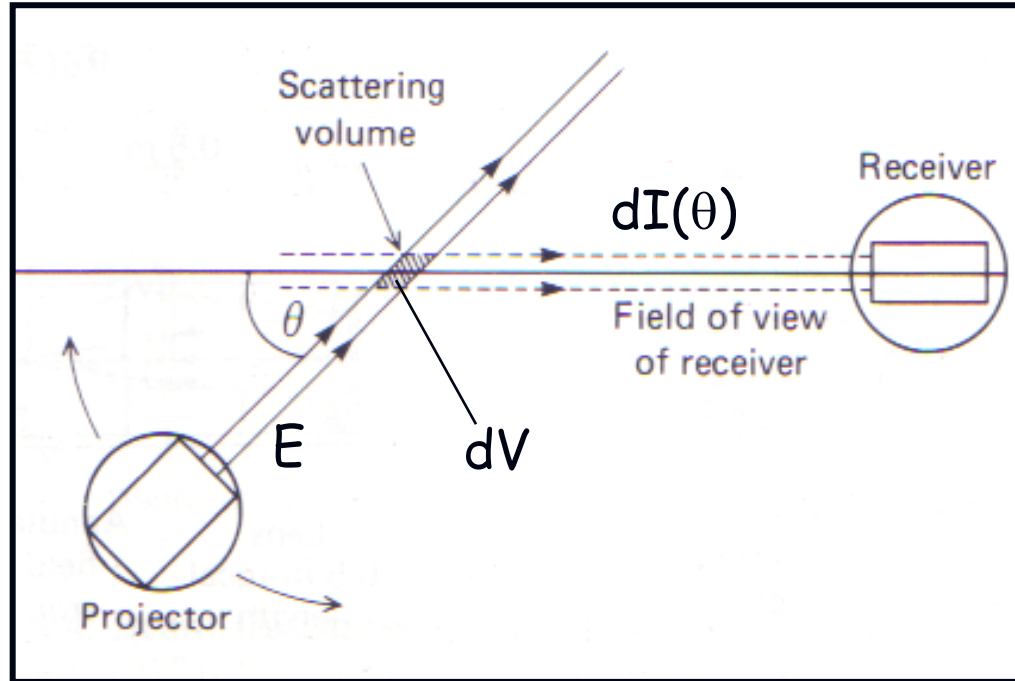
Modeled for very small particles (Rayleigh)



Averaged from Atlantic and Pacific Oceans

> 60 samples

Polarization: Measuring the Mueller matrix



Bohren and Huffman 1983

Table 13.1 Combinations of Scattering Matrix Elements That Result from Measurements with a Polarizer P_i Forward of the Scattering Medium and an Analyzer A_j aft^a

U	U	$\frac{1}{2}(S_{11})$	$\frac{1}{2}(S_{11} + S_{21})$	P_{\perp}	U	$\frac{1}{2}(S_{11} - S_{12})$
U	A_{\parallel}	$\frac{1}{4}(S_{11} + S_{21})$	$\frac{1}{4}(S_{11} + S_{21} + S_{21} + S_{22})$	P_{\perp}	A_{\parallel}	$\frac{1}{4}(S_{11} - S_{12} + S_{21} - S_{22})$
U	A_{\perp}	$\frac{1}{4}(S_{11} - S_{21})$	$\frac{1}{4}(S_{11} + S_{12} - S_{21} - S_{22})$	P_{\perp}	A_{\perp}	$\frac{1}{4}(S_{11} - S_{12} - S_{21} + S_{22})$
U	A_{+}	$\frac{1}{4}(S_{11} + S_{31})$	$\frac{1}{4}(S_{11} + S_{12} + S_{31} + S_{32})$	P_{\perp}	A_{+}	$\frac{1}{4}(S_{11} - S_{12} + S_{31} - S_{32})$
U	A_{-}	$\frac{1}{4}(S_{11} - S_{31})$	$\frac{1}{4}(S_{11} + S_{12} - S_{31} - S_{32})$	P_{\perp}	A_{-}	$\frac{1}{4}(S_{11} - S_{12} - S_{31} + S_{32})$
U	A_R	$\frac{1}{4}(S_{11} - S_{41})$	$\frac{1}{4}(S_{11} + S_{12} - S_{41} - S_{42})$	P_{\perp}	A_R	$\frac{1}{4}(S_{11} - S_{12} - S_{41} + S_{42})$
U	A_L	$\frac{1}{4}(S_{11} + S_{41})$	$\frac{1}{4}(S_{11} + S_{12} + S_{41} + S_{42})$	P_{\perp}	A_L	$\frac{1}{4}(S_{11} - S_{12} + S_{41} - S_{42})$
P_{\parallel}	U	$\frac{1}{2}(S_{11} + S_{12})$	$\frac{1}{2}(S_{11} + S_{13})$	P_{+}	U	$\frac{1}{2}(S_{11} + S_{13})$
P_{\parallel}	A_{\parallel}	$\frac{1}{4}(S_{11} + S_{12} + S_{21} + S_{22})$	$\frac{1}{4}(S_{11} + S_{13} + S_{21} + S_{23})$	P_{+}	A_{\parallel}	$\frac{1}{4}(S_{11} + S_{13} + S_{21} + S_{23})$
P_{\parallel}	A_{\perp}	$\frac{1}{4}(S_{11} + S_{12} - S_{21} - S_{22})$	$\frac{1}{4}(S_{11} + S_{13} - S_{21} - S_{23})$	P_{+}	A_{\perp}	$\frac{1}{4}(S_{11} + S_{13} - S_{21} - S_{23})$
P_{\parallel}	A_{+}	$\frac{1}{4}(S_{11} + S_{12} + S_{31} + S_{32})$	$\frac{1}{4}(S_{11} + S_{13} + S_{31} + S_{33})$	P_{+}	A_{+}	$\frac{1}{4}(S_{11} + S_{13} + S_{31} + S_{33})$
P_{\parallel}	A_{-}	$\frac{1}{4}(S_{11} + S_{12} - S_{31} - S_{32})$	$\frac{1}{4}(S_{11} + S_{13} - S_{31} - S_{33})$	P_{+}	A_{-}	$\frac{1}{4}(S_{11} + S_{13} - S_{31} - S_{33})$
P_{\parallel}	A_R	$\frac{1}{4}(S_{11} + S_{12} - S_{41} - S_{42})$	$\frac{1}{4}(S_{11} + S_{13} - S_{41} - S_{43})$	P_{+}	A_R	$\frac{1}{4}(S_{11} + S_{13} - S_{41} - S_{43})$
P_{\parallel}	A_L	$\frac{1}{4}(S_{11} + S_{12} + S_{41} + S_{42})$	$\frac{1}{4}(S_{11} + S_{13} + S_{41} + S_{43})$	P_{+}	A_L	$\frac{1}{4}(S_{11} + S_{13} + S_{41} + S_{43})$
P_{-}	U	$\frac{1}{2}(S_{11} - S_{13})$	$\frac{1}{2}(S_{11} - S_{14})$	P_L	U	$\frac{1}{2}(S_{11} - S_{14})$
P_{-}	A_{\parallel}	$\frac{1}{4}(S_{11} - S_{13} + S_{21} - S_{23})$	$\frac{1}{4}(S_{11} - S_{14} + S_{21} - S_{24})$	P_L	A_{\parallel}	$\frac{1}{4}(S_{11} - S_{14} + S_{21} - S_{24})$
P_{-}	A_{\perp}	$\frac{1}{4}(S_{11} - S_{13} - S_{21} + S_{23})$	$\frac{1}{4}(S_{11} - S_{14} - S_{21} + S_{24})$	P_L	A_{\perp}	$\frac{1}{4}(S_{11} - S_{14} - S_{21} + S_{24})$
P_{-}	A_{+}	$\frac{1}{4}(S_{11} - S_{13} + S_{31} - S_{33})$	$\frac{1}{4}(S_{11} - S_{14} + S_{31} - S_{34})$	P_L	A_{+}	$\frac{1}{4}(S_{11} - S_{14} + S_{31} - S_{34})$
P_{-}	A_{-}	$\frac{1}{4}(S_{11} - S_{13} - S_{31} + S_{33})$	$\frac{1}{4}(S_{11} - S_{14} - S_{31} + S_{34})$	P_L	A_{-}	$\frac{1}{4}(S_{11} - S_{14} - S_{31} + S_{34})$
P_{-}	A_R	$\frac{1}{4}(S_{11} - S_{13} - S_{41} + S_{43})$	$\frac{1}{4}(S_{11} - S_{14} - S_{41} + S_{44})$	P_L	A_R	$\frac{1}{4}(S_{11} - S_{14} - S_{41} + S_{44})$
P_{-}	A_L	$\frac{1}{4}(S_{11} - S_{13} + S_{41} - S_{43})$	$\frac{1}{4}(S_{11} - S_{14} + S_{41} - S_{44})$	P_L	A_L	$\frac{1}{4}(S_{11} - S_{14} + S_{41} - S_{44})$
P_R	U	$\frac{1}{2}(S_{11} + S_{14})$	$\frac{1}{2}(S_{11} + S_{14})$			
P_R	A_{\parallel}	$\frac{1}{4}(S_{11} + S_{14} + S_{21} + S_{24})$				
P_R	A_{\perp}	$\frac{1}{4}(S_{11} + S_{14} - S_{21} - S_{24})$				
P_R	A_{+}	$\frac{1}{4}(S_{11} + S_{14} + S_{31} + S_{34})$				
P_R	A_{-}	$\frac{1}{4}(S_{11} + S_{14} - S_{31} - S_{34})$				
P_R	A_R	$\frac{1}{4}(S_{11} + S_{14} - S_{41} - S_{44})$				
P_R	A_L	$\frac{1}{4}(S_{11} + S_{14} + S_{41} + S_{44})$				

$\frac{S_{12}}{S_{11}}$ degree of linear polar.

$S_{21} = S_{12}$ for sphere
 $S_{11} = S_{22}$ for goniometer

See p. 65 and p. 112

^a U indicates the absence of a polarizer or analyzer.

Voss and Fry (1984) PDM model

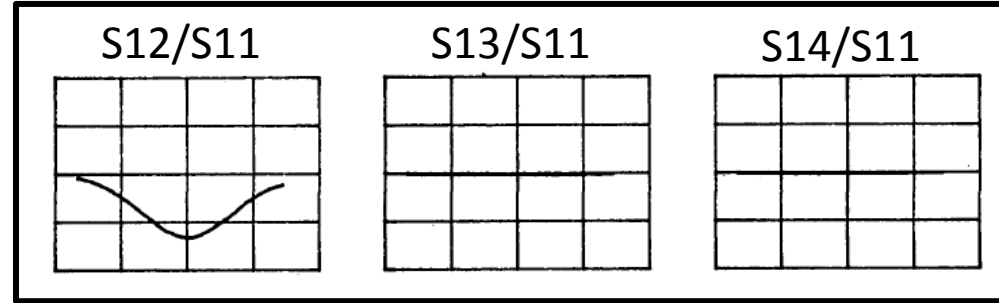
Degree of Linear Polarization

$$\text{DoLP} = -S_{12} / S_{11}$$

$$= -(H-V)/(H+V)$$

$$H = \frac{1}{2}(S_{11} + S_{12})$$

$$V = \frac{1}{2}(S_{11} - S_{12})$$



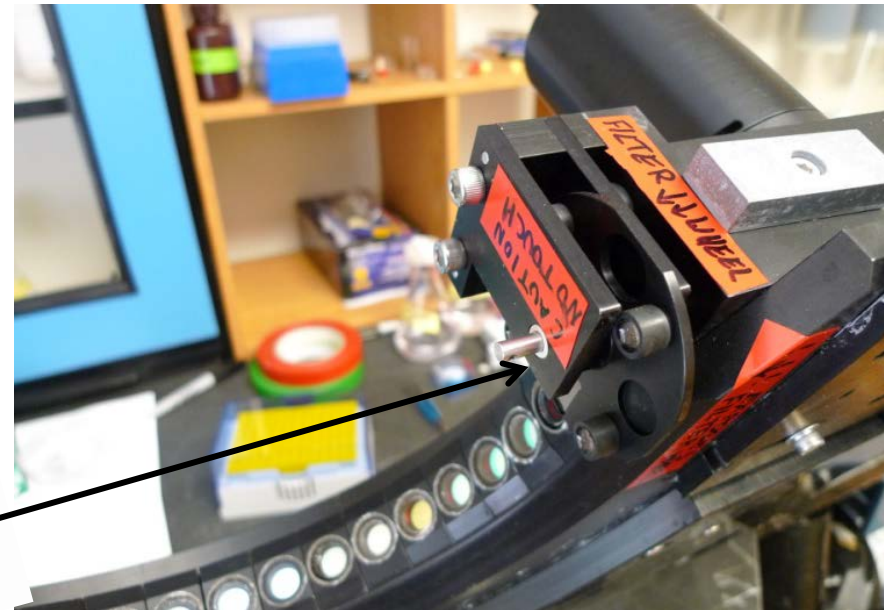
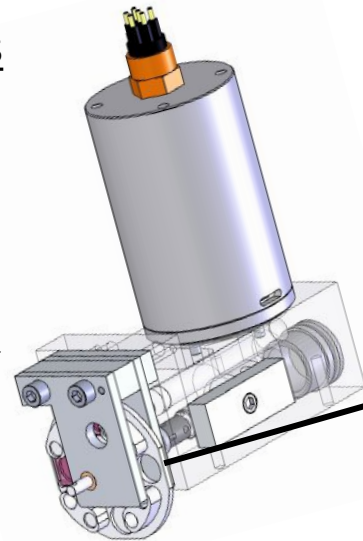
4 positions

1 - OPEN

2 - DARK

3 - H \longleftrightarrow

4 - V \updownarrow



Measuring polarization

linear

Measuring S12

$$H = \frac{1}{2}(S_{11} + S_{12})$$

$$V = \frac{1}{2}(S_{11} - S_{12})$$

oblique linear

Measuring S13

$$O_+ = \frac{1}{2}(S_{11} + S_{13})$$

$$O_- = \frac{1}{2}(S_{11} - S_{13})$$

circular

Measuring S14

$$R = \frac{1}{2}(S_{11} + S_{14})$$

$$L = \frac{1}{2}(S_{11} - S_{14})$$

$$-S_{12} / S_{11} = -(H-V)/(H+V)$$

$$-S_{13} / S_{11} = \frac{-(O_+ - O_-)}{(O_+ + O_-)}$$

$$-S_{14} / S_{11} = -(R-L)/(R+L)$$

$$S_{12} = H-V \text{ and} \\ S_{11} = H+V$$

$$S_{13} = O_+ - O_- \text{ and} \\ S_{11} = O_+ + O_-$$

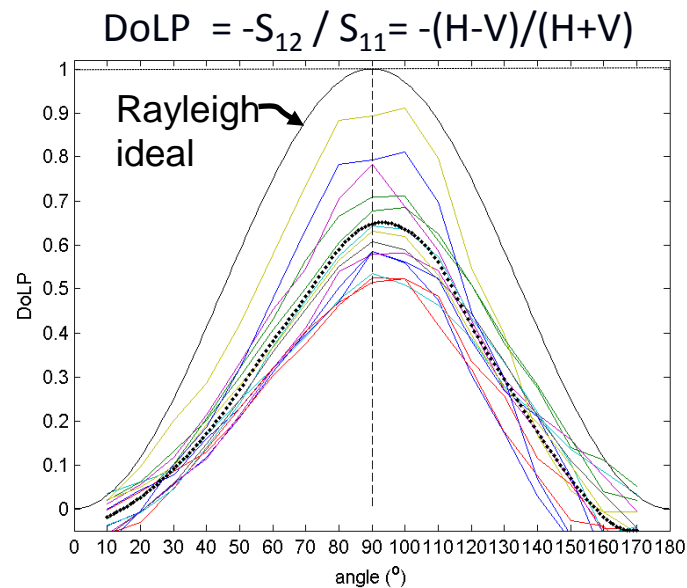
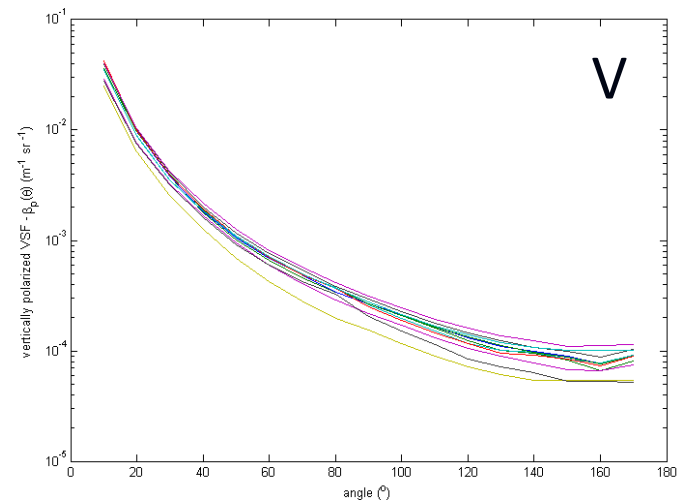
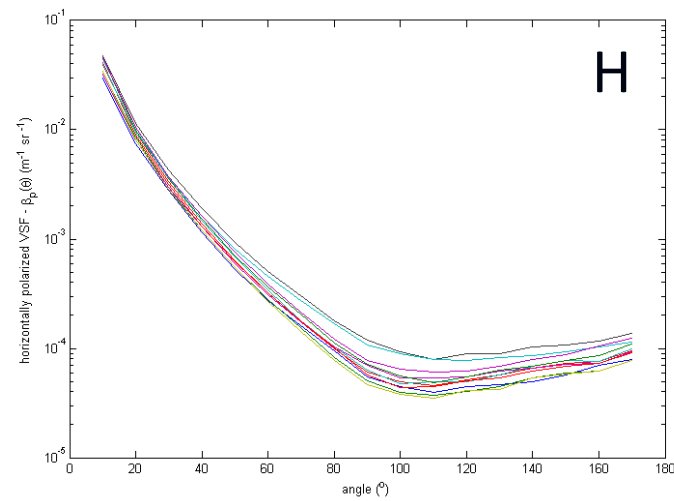
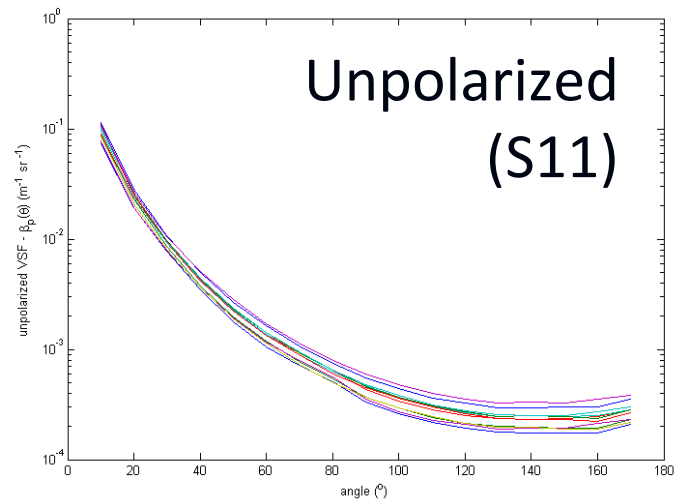
$$S_{14} = R-L \text{ and} \\ S_{11} = R+L$$

- *however, there are transmission losses due to the filters (~90% T)*
- *radiometric values are fine, as transmission factors cancel*

“true” $S_{11} = (H + V)/T$ (where $T = 0.9$)

S11 can be validated with direct open path measurement

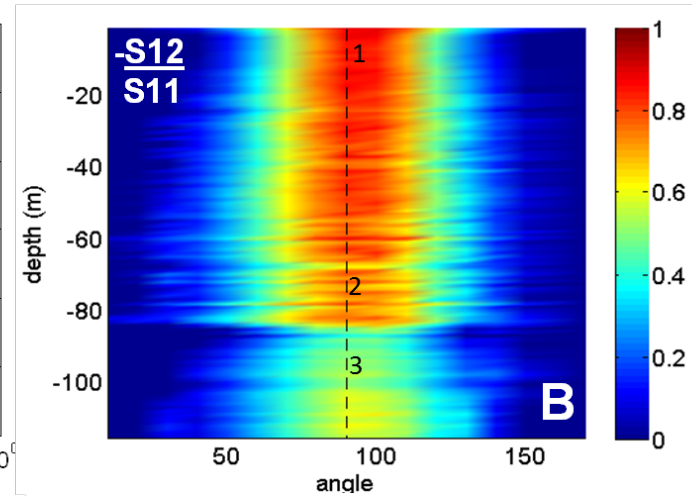
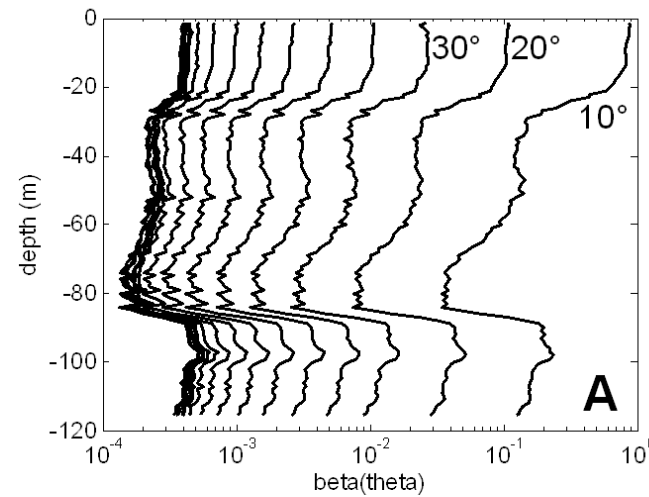
Curaçao, 2012: single vertical profile



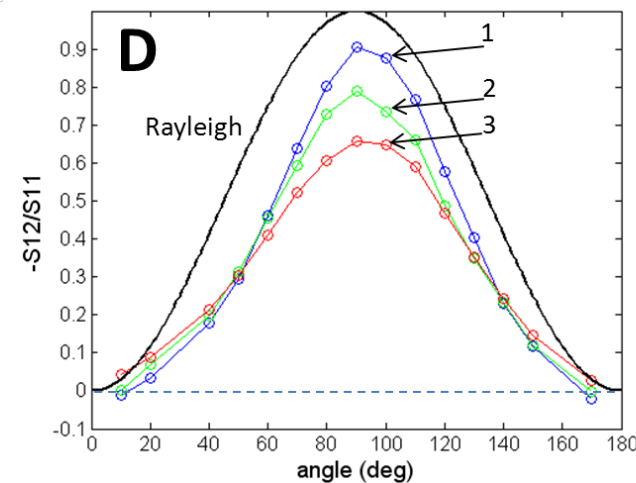
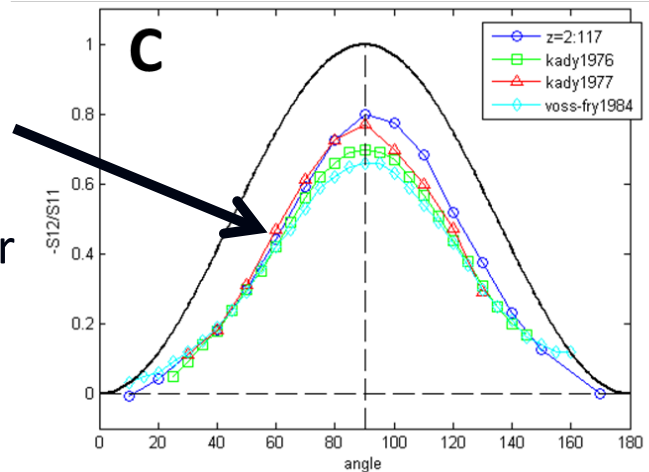
Cruise locations with MASCOT polarization measurements (since 2008)

- Ligurian Sea (S13 and S14 also)
- NY bight
- Santa Barbara Channel
- Gulf of Mexico
- Port Aransas, TX
- Florida Keys (2X)
- Curacao
- East Sound, WA
- Florida, Indian lagoon
- N. Lake Michigan

Polarized scattering measurements




There are only 3 other measurements of S_{12}/S_{11} for ocean water in the literature!

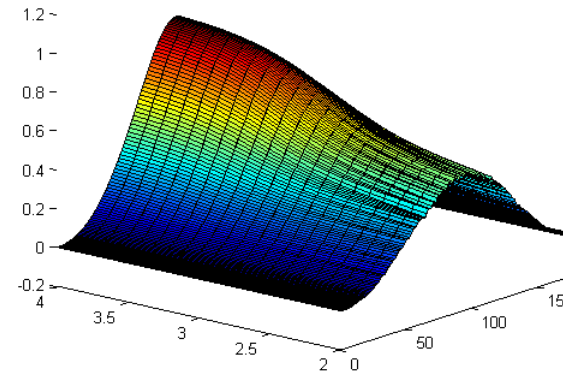
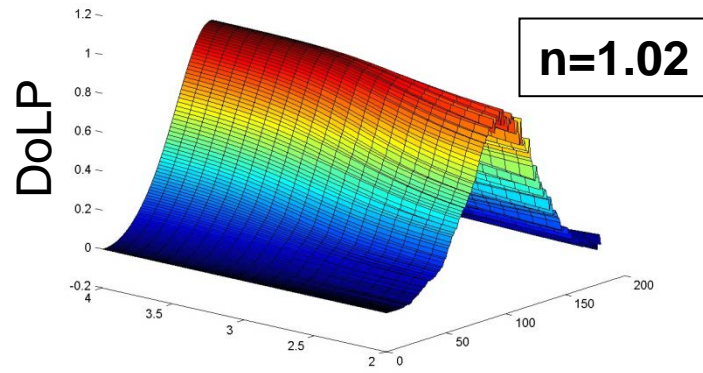


S_{12}/S_{11} :
degree of
linear polarization

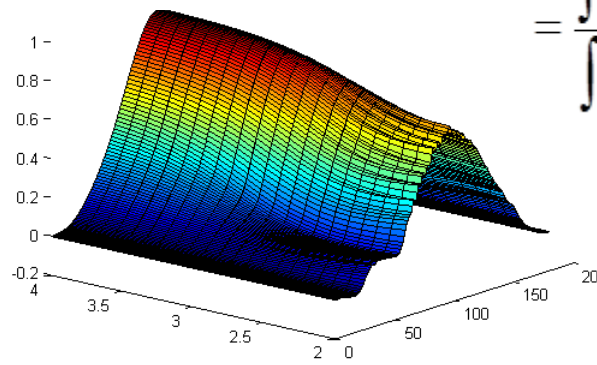
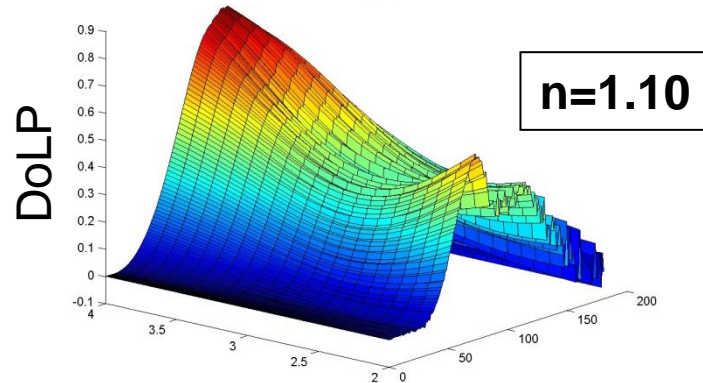
Santa Barbara Channel, September 2008

Lorenz-Mie ()

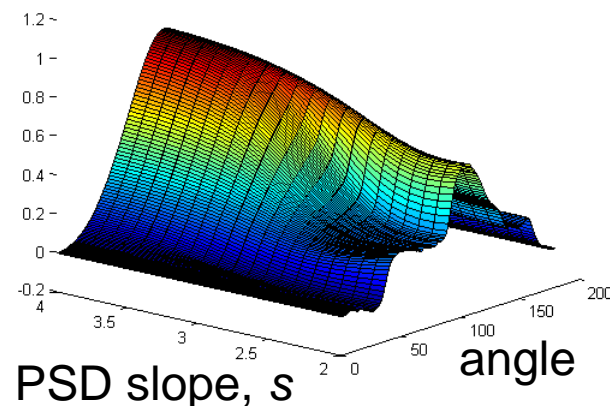
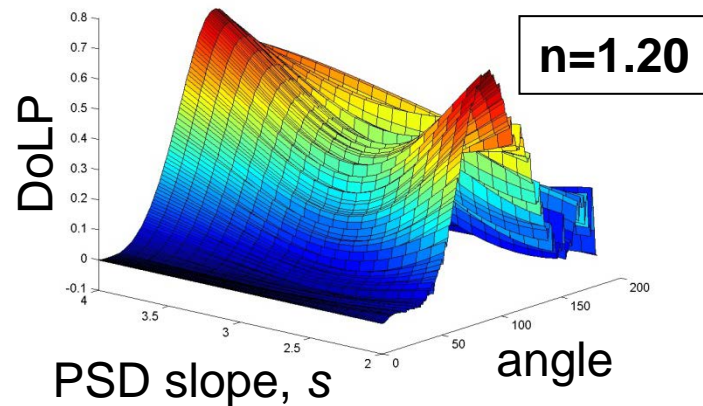
asymmetric hexahedra ()



$$DoLP_{pop} = \frac{\overline{S12(\theta)}}{\overline{S11(\theta)}}$$

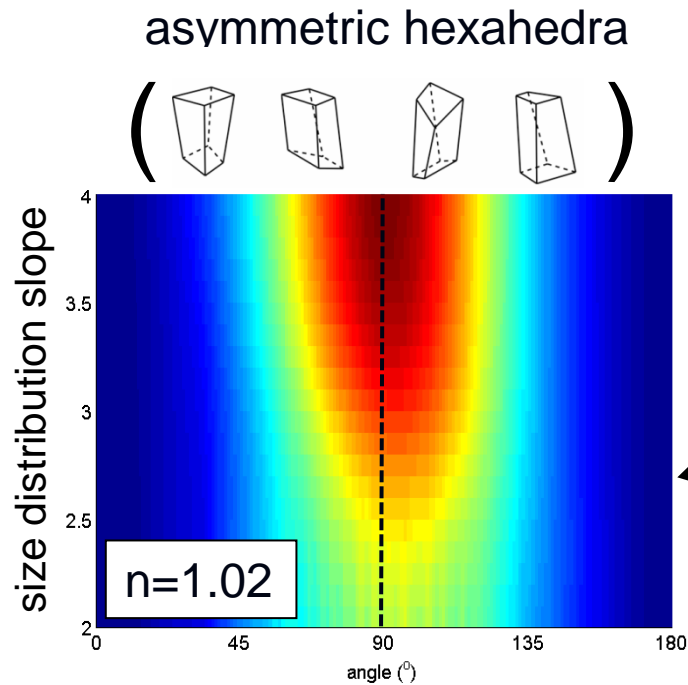


$$= \frac{\int S12(D, n, \theta, \lambda) F(D) dD}{\int S11(D, n, \theta, \lambda) F(D) dD}$$

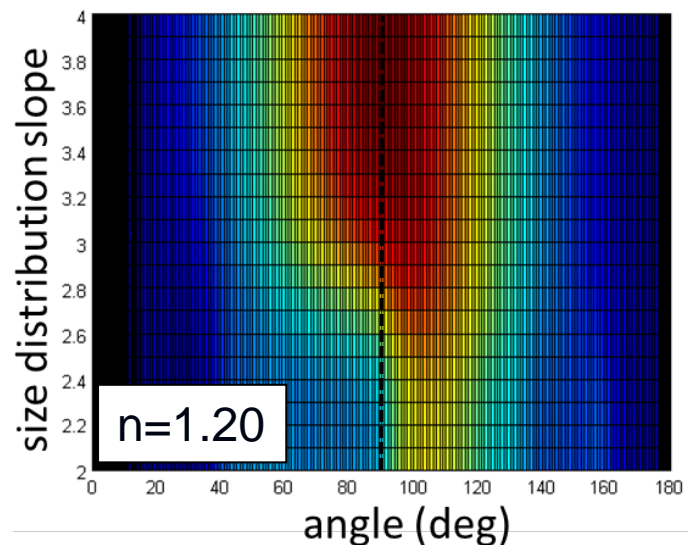
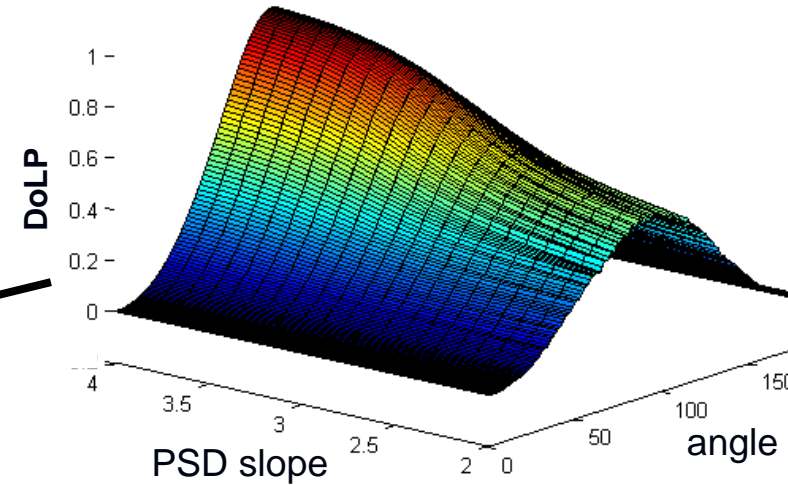


$$F(D) = \frac{dN}{dD} = AD^{-s}$$

Degree of Linear Polarization



another view



- **Increasing nonsphericity** lowers DoLP and shifts the DoLP peak to larger angles
- **Increasing refractive index** lowers DoLP, particularly for populations with relatively flat size distributions
- **As size distributions become increasingly flat**, the DoLP decreases and the maximum shifts to larger angles

Polarized scattering

phytoplankton species

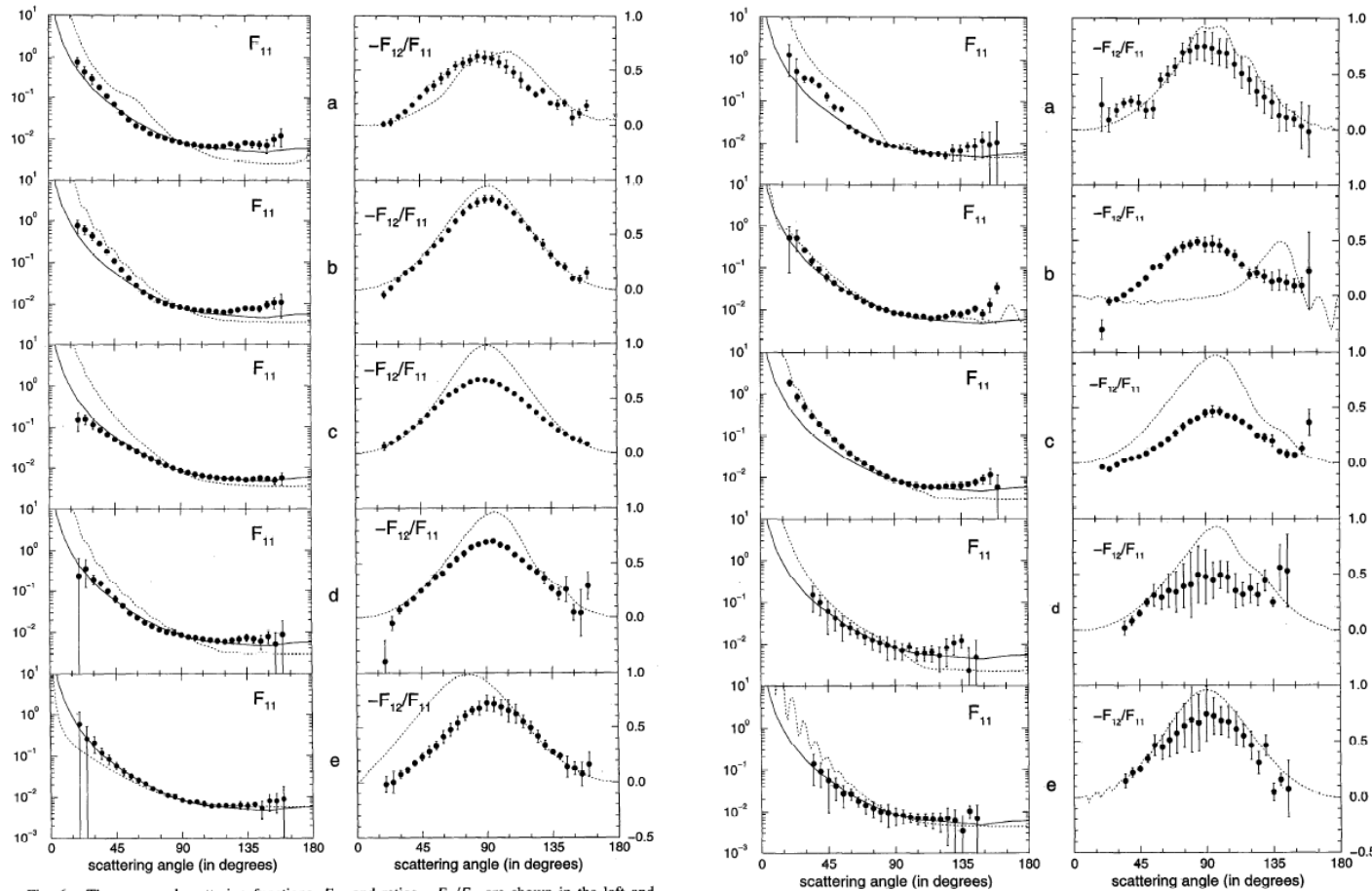


Fig. 6. The measured scattering functions, F_{11} , and ratios $-F_{12}/F_{11}$ are shown in the left and right panels, respectively (filled circles) for (a) *Microcystis aeruginosa* without gas vacuoles, (b) *Microcystis aeruginosa* with gas vacuoles, (c) *Microcystis* sp., (d) *Phaeocystis*, and (e) *Volvox aureus*. Also plotted are the scattering function for San Diego Harbor (solid, left panels) and the results of Mie calculations (dashed, left and right panels). The $F_{11}(\theta)$ functions are scaled at 90° to the scattering function of San Diego Harbor. Errors are smaller than symbols if no error bar is indicated.

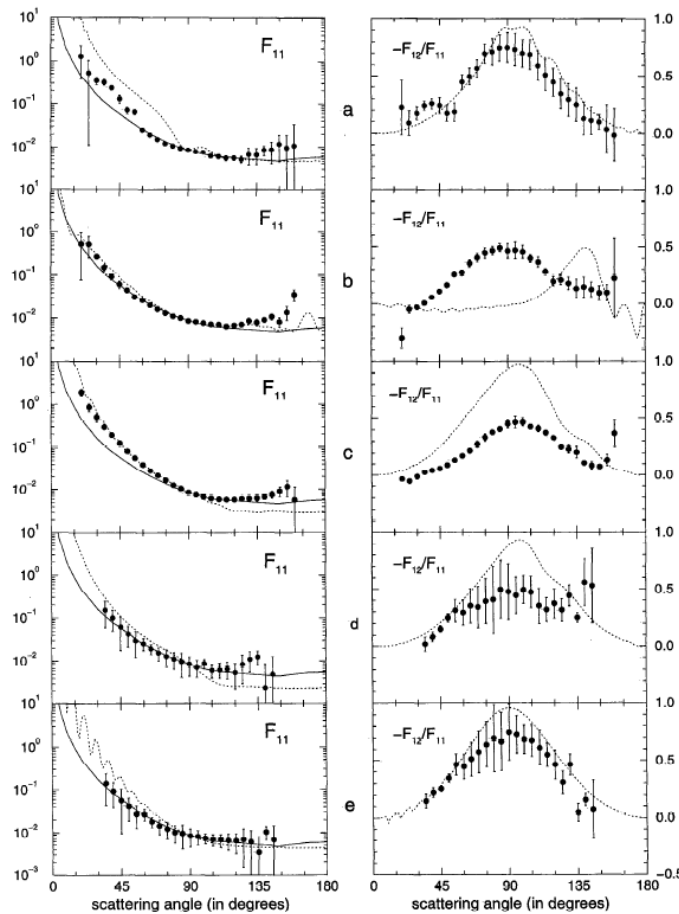


Fig. 8. Same as Fig. 6 for (a) *Astrionella formosa*, (b) *Selenastrum capricornutum*, (c) *Phaeodactylum*, (d) *Emiliana huxleyi* with cocoliths, and (e) *Emiliana huxleyi* without cocoliths.

sediment samples

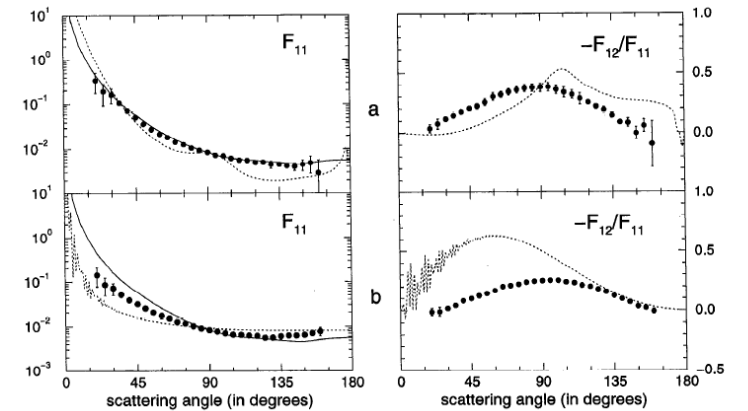


Fig. 9. Same as Fig. 6 for (a) Westerschelde silt with diameters ranging between 3 and 5 μm , and (b) Westerschelde silt with diameters ranging between 5 and 12 μm .

*Included reflection
corrections*

Interpreting polarized scattering

The angular and spectral characteristics of the Mueller scattering matrix parameters are a function of several properties of the particle population, including:

- Refractive index composition
- Size distribution
- Particle shape
- Particle orientation

Much to be done!

Scattering components

- Pure seawater (molecular)
- Turbulence (i.e., refractive index discontinuities)
- Particles
- Bubbles

Scattering by pure seawater – most literature pre~2006

VSF of water using Morel's model

$$\beta_w(\theta, \lambda, S, T=20^\circ\text{C}) = 1.38(\lambda/500\text{nm})^{-4.32} (1+0.3S/37)10^{-4} (1+\cos^2\theta(1-\delta)/(1+\delta))$$

(where depolarization ratio $\delta = 0.09$)

- Computed from Mie and Rayleigh-Mishchenko theory
- The term $1.38(\lambda/500\text{nm})^{-4.32}$ describes $\beta(90)$ and was obtained by a fit to Morel's computed results
- The term $(1+0.3S/37)$ is from Morel's experimental data with 37 ppt seawater

NOT THE BEST VALUES

Scattering by pure seawater, literature ~2007-2008

VSF of water using Buiteveld et al. (1994) and
Morel's salinity term:
(reviewed in Twardowski et al. (2004))

- Also uses Einstein-Smoluchowsky theory, but uses updated constants, mostly derived from experimental data from the 1970s
- The "famous" -4.32 exponent for scattering of water is now -4.14 because of a reformulation of the refractive index of water and the isothermal compressibility of water
- The depolarization ratio is now 0.51 after Farinato and Rowell (1974)
 - ❖ this is a critical uncertainty – needs further work

NOT THE BEST VALUES

Scattering by pure seawater (current)

Zhang and Hu (2009); Zhang et al. (2009)

Review: Zhang (2012)

-Also uses Einstein-Smoluchowsky theory, but uses density derivative for refractive index fluctuations with updated constants – more accurate than approximation with pressure derivative

-The depolarization ratio used is 0.039, also after Farinato and Rowell (1974)

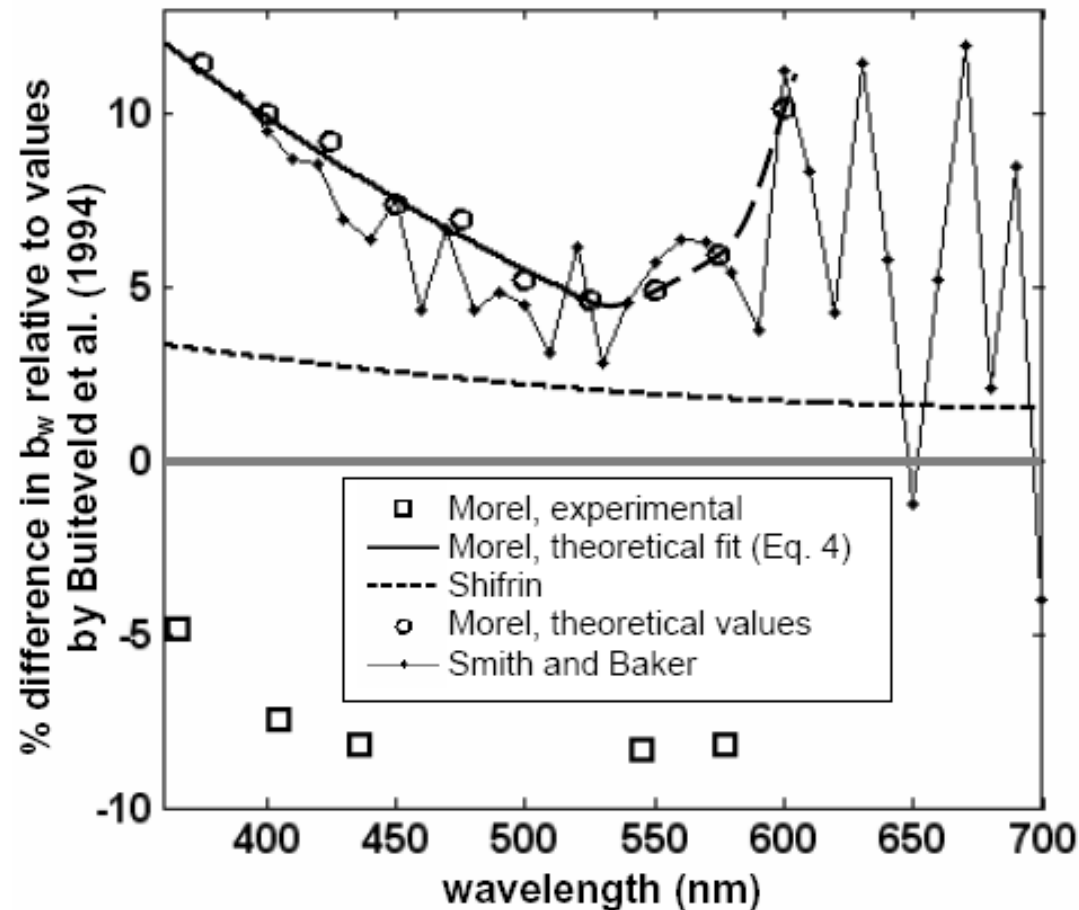
❖ this is a critical area of uncertainty – needs further work

These are currently considered the most accurate values (probably $\pm 2-4\%$) but rigorous experimental verification is still needed

Agrees well with experimental work of Morel (1968)

For backscattering by seawater, divide b_w by 2.

Scattering by pure seawater

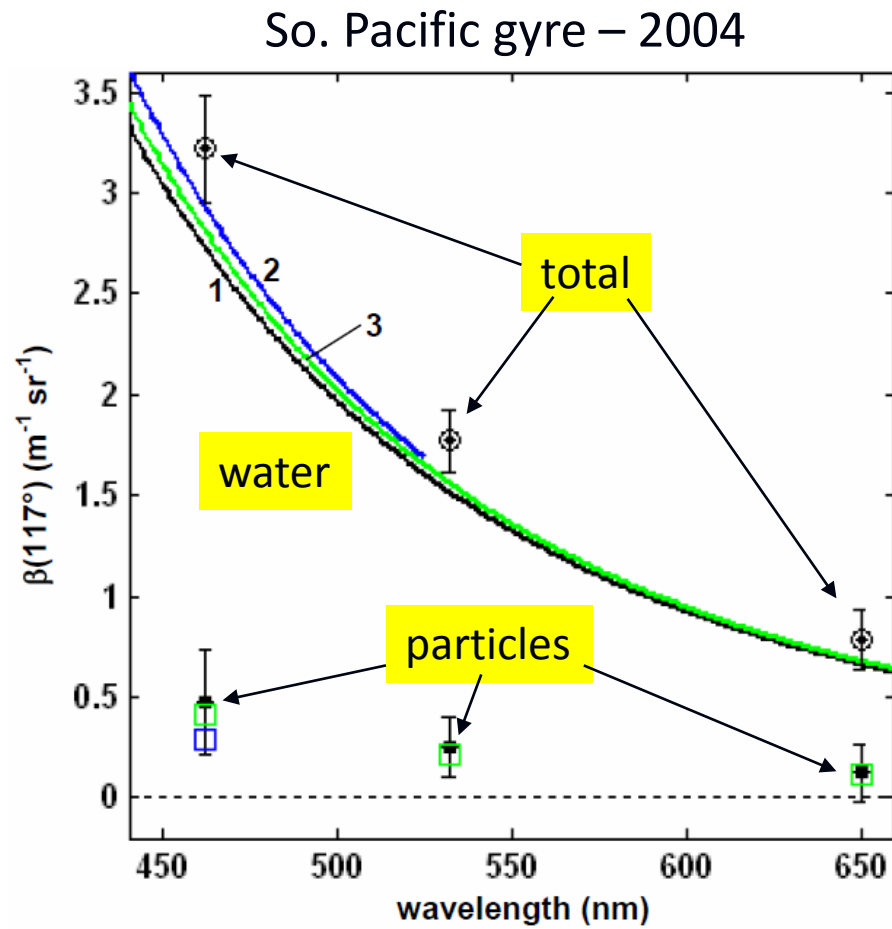


Backscattering by seawater can be 90+% of total b_b in the very clear ocean.
Accuracy is very important if we are interested in b_{bp}

$$\text{Morel : } b_w = 3.50 \left(\frac{\lambda}{450} \right)^{-4.32} 10^{-3} \text{ m}^{-1},$$

$$\text{Shifrin : } b_w = 1.49 \left(\frac{\lambda}{546} \right)^{-4.17} 10^{-3} \text{ m}^{-1}$$

Scattering by pure seawater

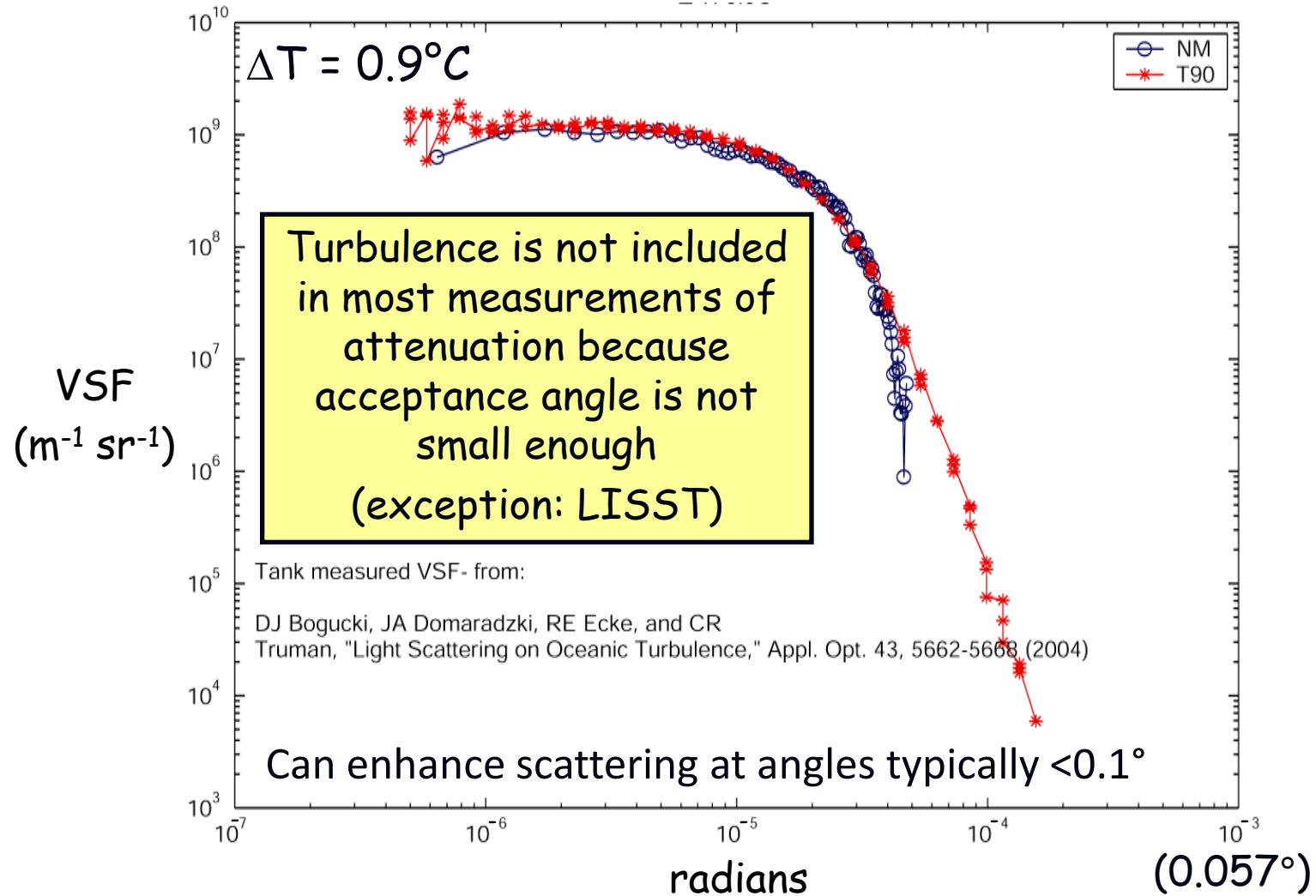


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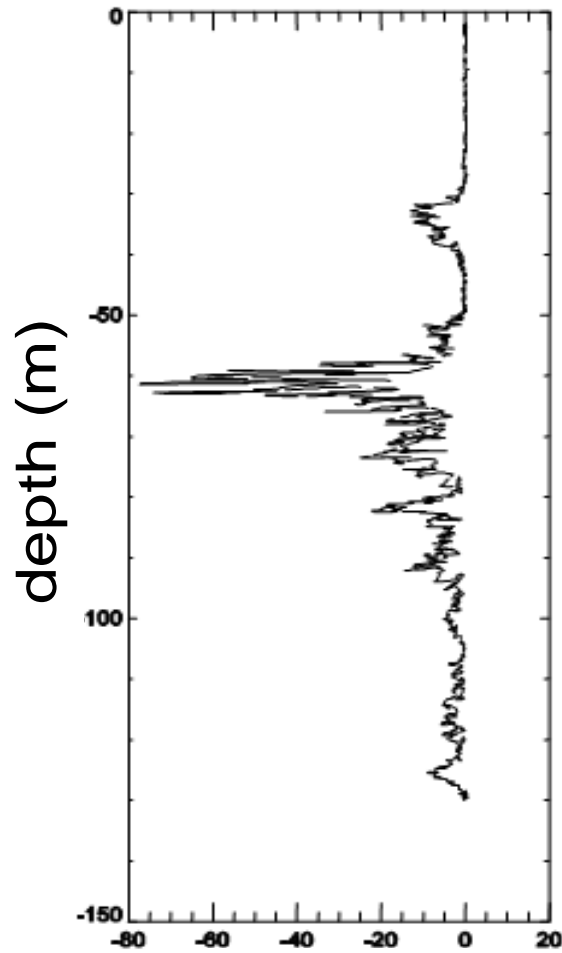
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$$\text{Shifrin : } b_w = 1.49 \left(\frac{\lambda}{546} \right)^{-4.17} 10^{-3} \text{ m}^{-1}$$

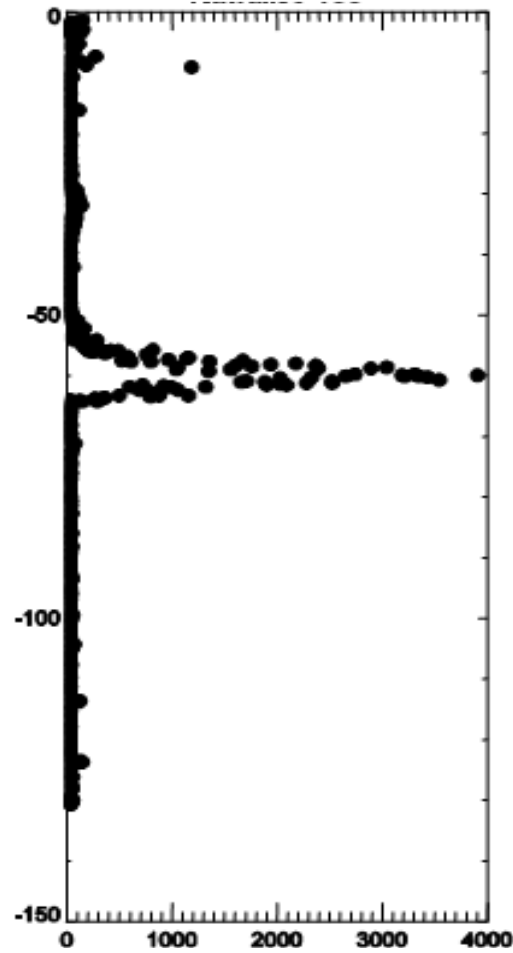
Turbulence (refractive index discontinuities)



Turbulence measurement with LISST-100X

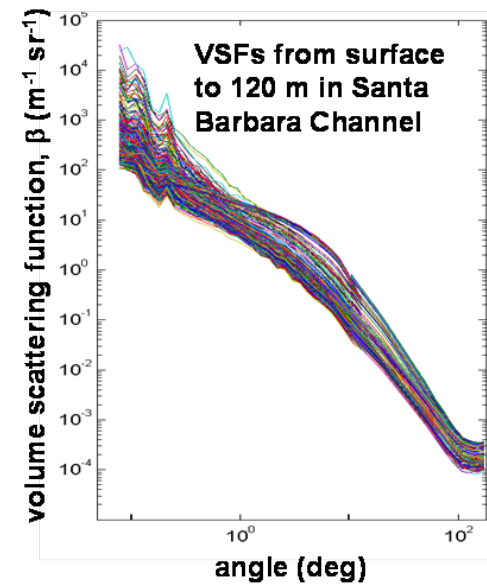
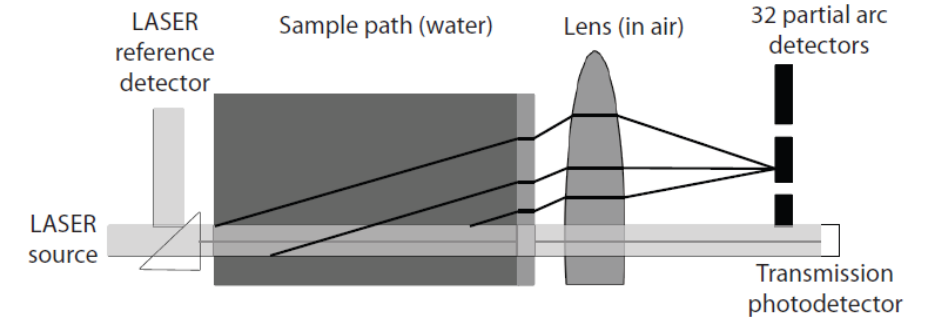


dn/dt
from T&S

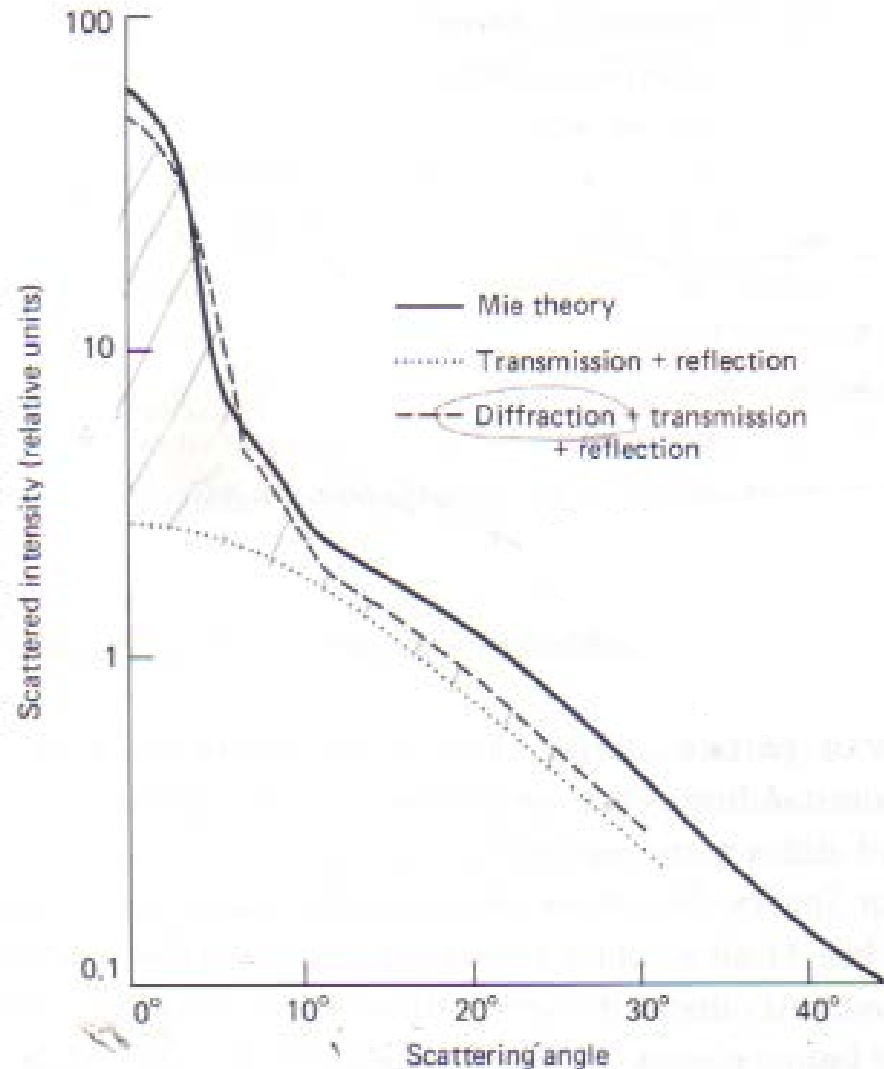
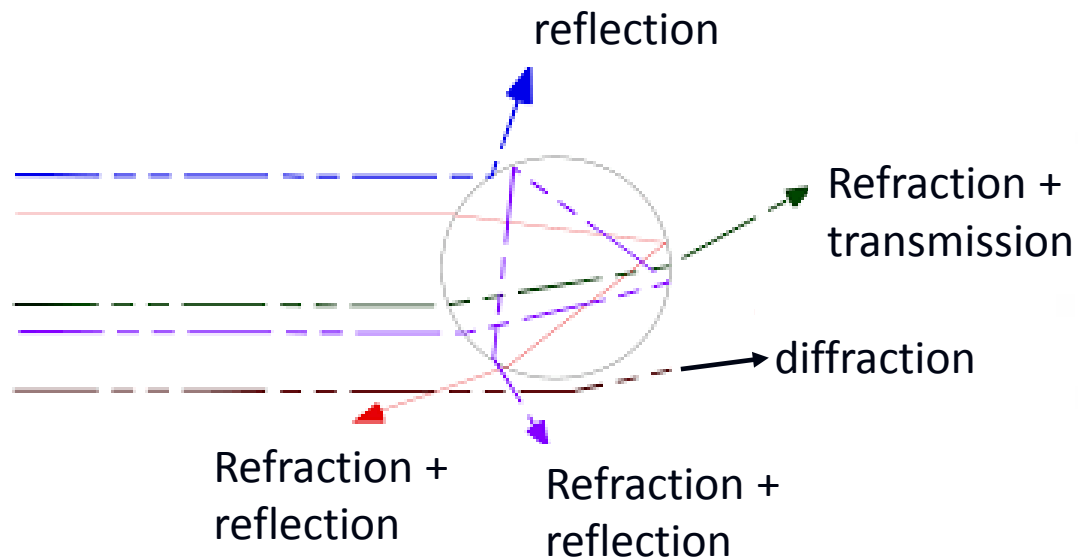


turbulence indicator
from LISST VSF

Hawaii
09/2009



Particle scattering



Kirk 1994

Fig. 4.1. Angular distribution of scattered intensity from transparent spheres calculated from Mie theory (Ashley & Cobb, 1958) or on the basis of transmission and reflection, or diffraction, transmission and reflection (Hodkinson & Greenleaves, 1963). The particles have a refractive index (relative to the surrounding medium) of 1.20, and have diameters 5–12 times the wavelength of the light. After Hodkinson & Greenleaves (1963).

“...our present-day interpretation and detailed understanding of major sources of backscattering and its variability in the ocean are uncertain and controversial.”

Stramski, D., E. Boss, D. Bogucki, and K. J. Voss, 2004. The role of seawater constituents in light backscattering in the ocean. *Progress in Oceanography*, 61(1), 27-55.

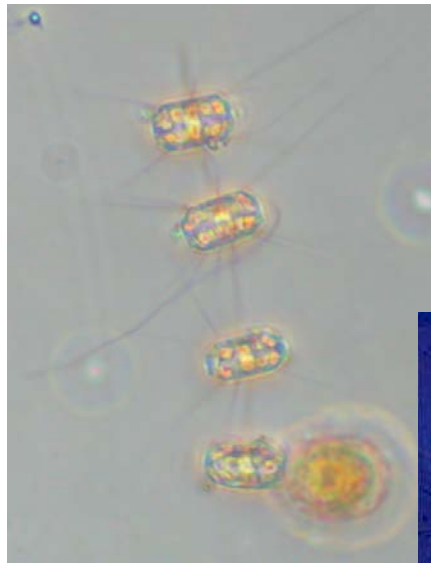
The Enigma of Phytoplankton Backscattering...

Modeling phytoplankton as homogeneous spheres results in backscattering levels too low (only a few percent contribution) to be consistent with their influence on remote sensing reflectance (R_{RS}).

Stramski and Kiefer 1991; Stramski et al. 2001

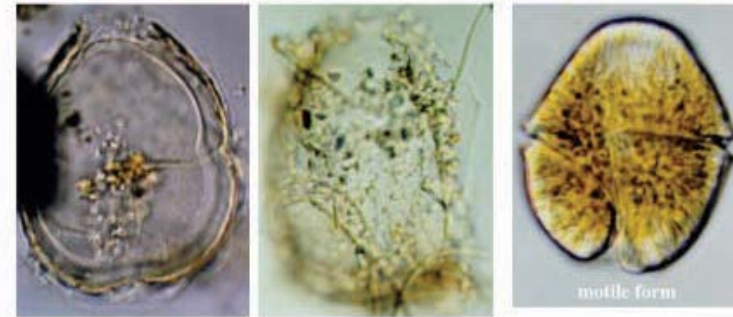
Testing the “Complex Particle” Hypothesis

Thalassiosira weissflogii



~25 μm diameter

Gyrodinium instriatum



photomicrographs by K. Matsuoka and Y. Fukuyo

~50 mm diameter



Chaetoceros socialis
© Jan Rines

Chaetoceros socialis

~10 μm cell diameter
Up to 1 mm colonies

The background in cultures is important

Background (<10 μm fraction) in culture experiments

	<u>Thalassiosira</u>	<u>C. socialis</u>	<u>Gyrodinium</u>
Fraction bbp	41%	53%	73%
bbp/bp	0.004	0.035	0.034

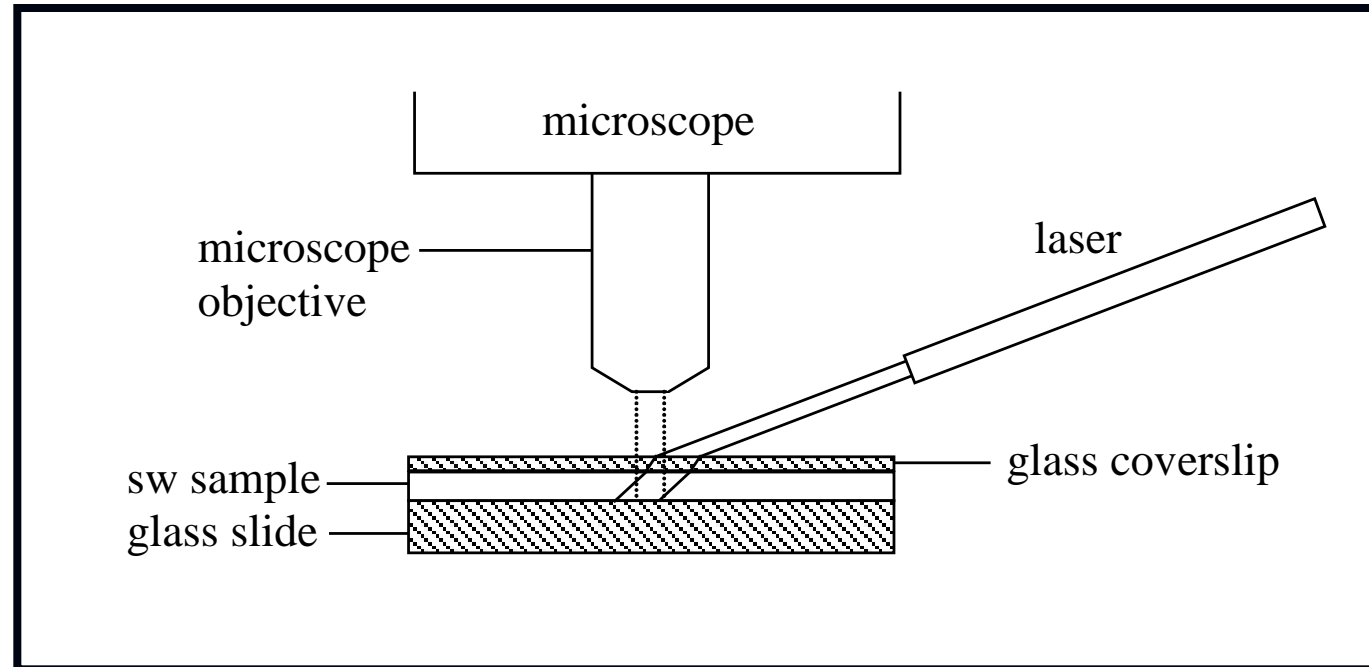
Background is usually not considered in scattering measurements in phytoplankton cultures

Phytoplankton scattering: measurements and modeling

$$b_{bp}/b_p$$

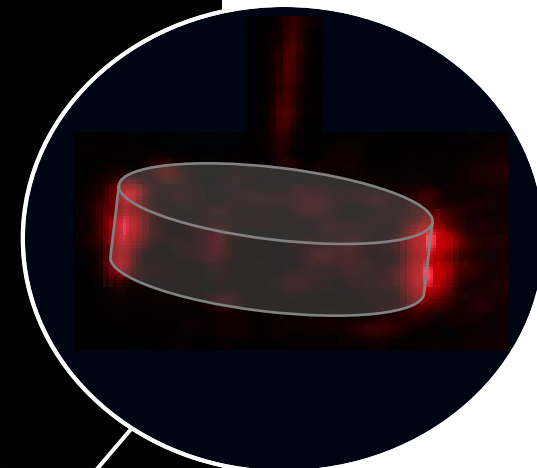
	Measured	Mie theory	Coated Mie theory
<i>Thalassiosira</i> cells	0.013	0.006	0.013
<i>Gyrodinium</i> cells	0.006	0.003	0.007
<i>C. socialis</i> cells	0.004	0.0006	0.0237
<i>C. socialis</i> ¹ cell Q_{bb} ² colony Q_b	0.004	0.004	

Imaging Particle Backscattering



Backscattering imaged at $\sim 140^\circ$

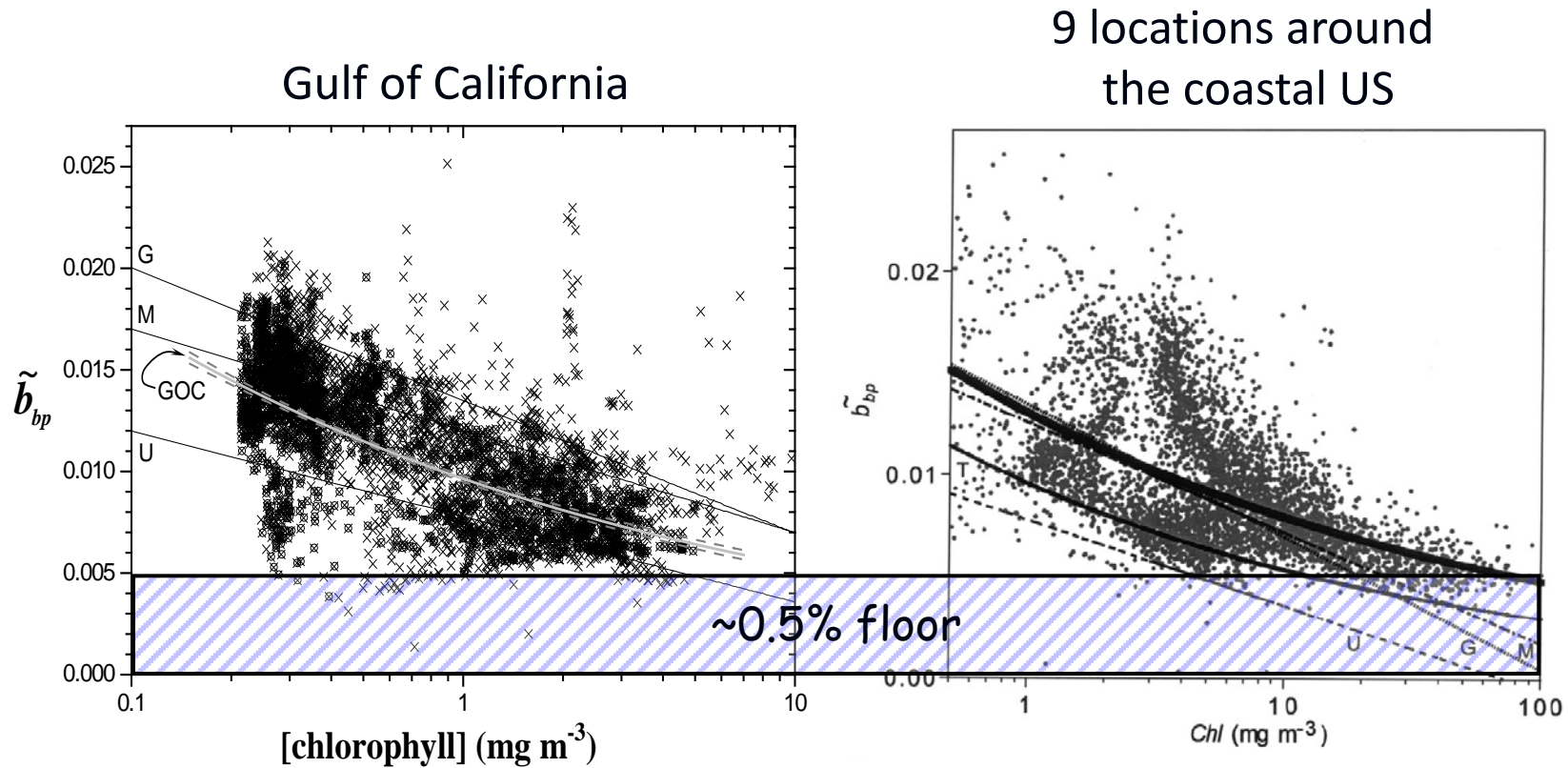
Imaging Particle Backscattering



Need hi
refractive
index
difference
 $(n_p - n_m)$

er direction
g image

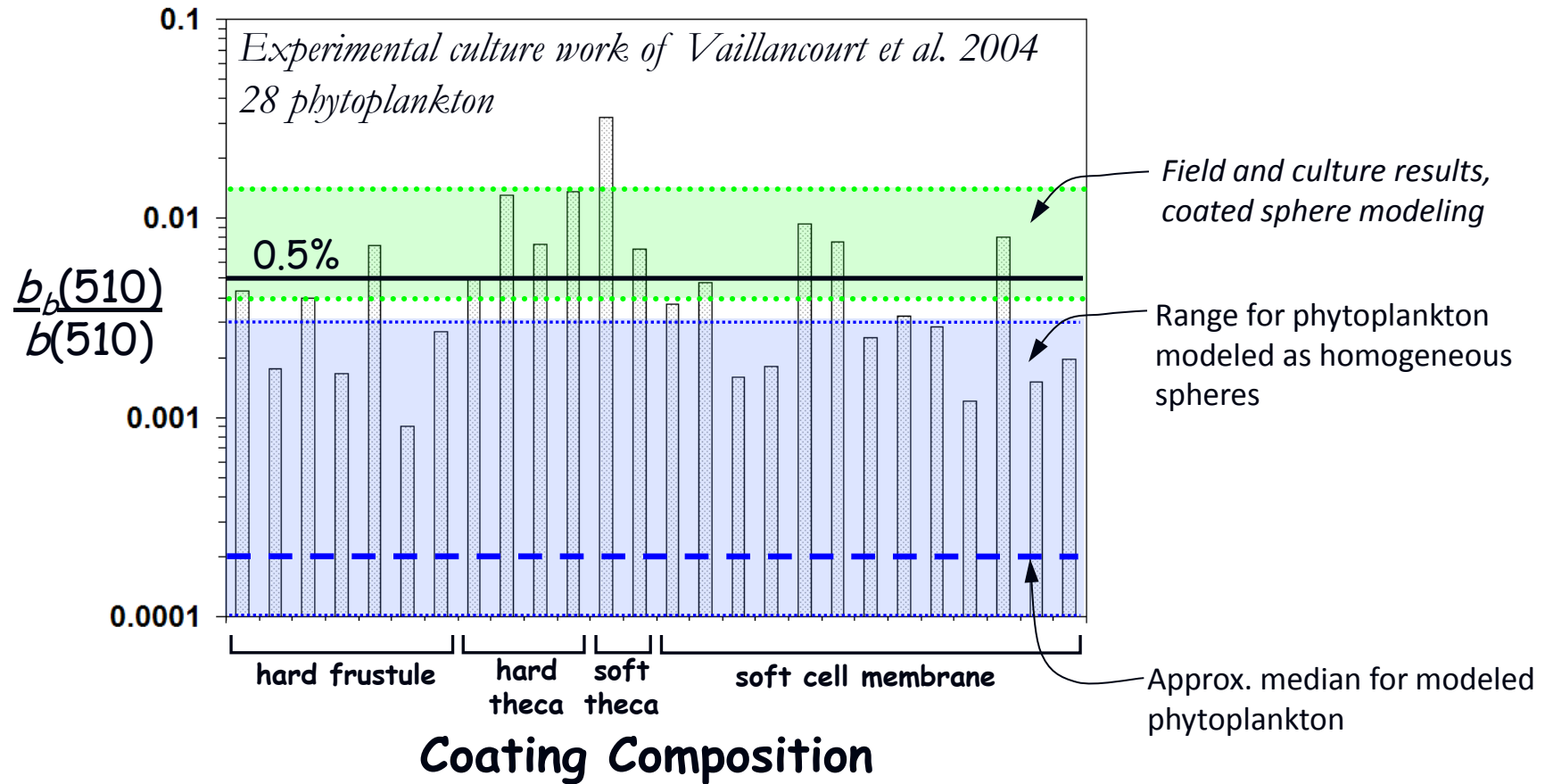
Backscattering ratio and chlorophyll



Twardowski et al. 2001

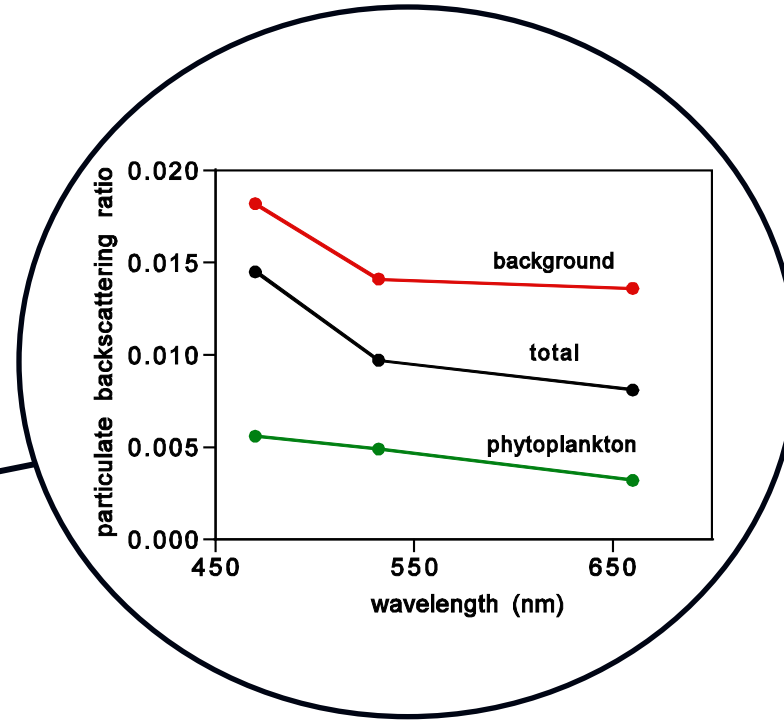
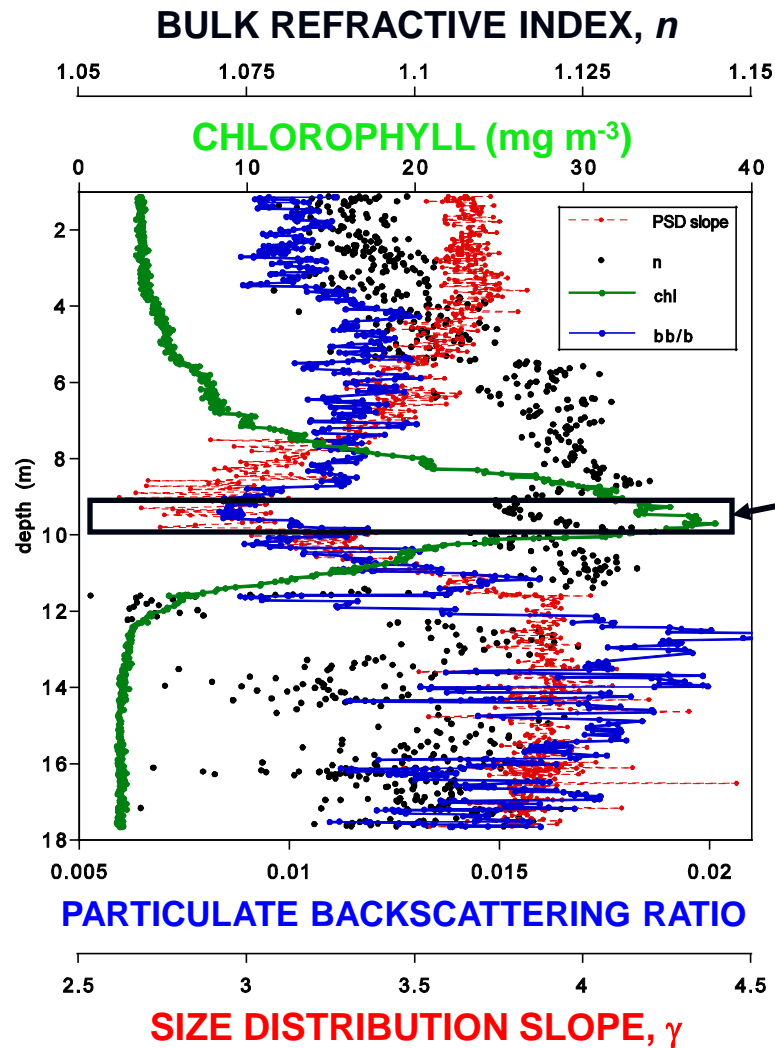
Sullivan et al. 2005

Phytoplankton b_b/b



Phytoplankton likely do make a significant direct contribution to b_{bp}

Akashiwo Layer in Monterey Bay



Akashiwo et al.

$$b_{bp}(532) / b_p(532) \approx \underline{0.005}$$

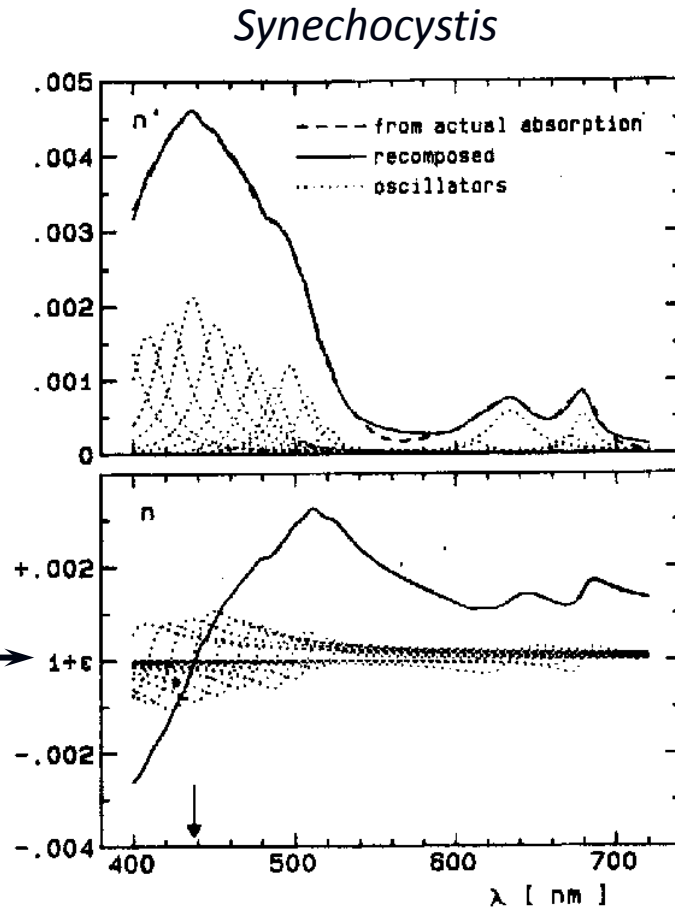
$\sim \underline{20\%}$ of $b_{bp}(532)$

Anomalous dispersion

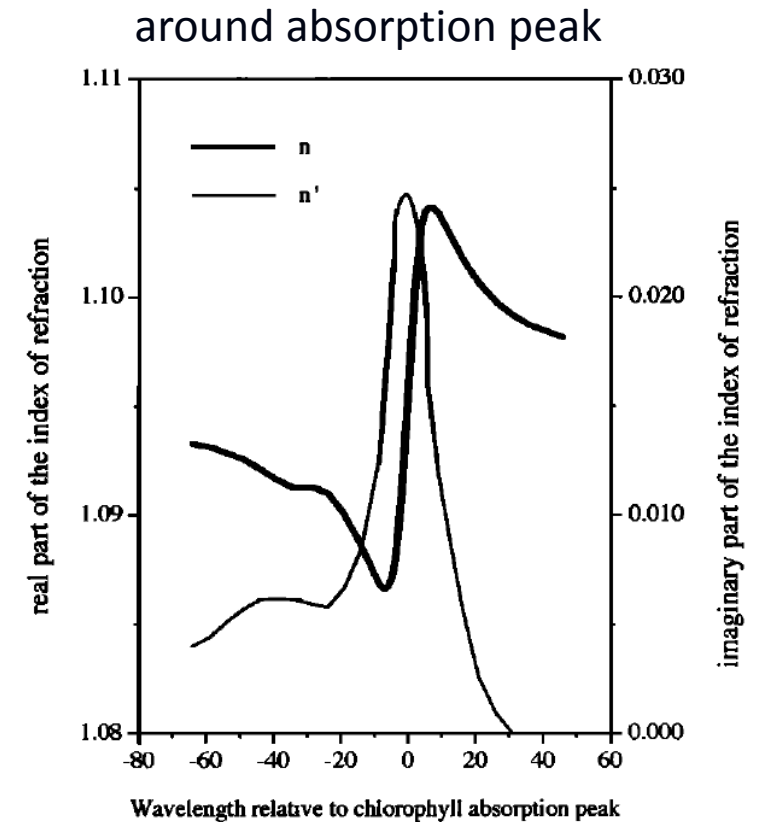
Spectral and angular scattering intensity of a particle is principally dependent on:

- size relative to λ
- complex refractive index relative to the medium ($n - in'$)

Anomalous dispersion describes how particle absorption alters the refractive index spectrum, i.e., if you change a_p , you will change b_p, b_{bp}

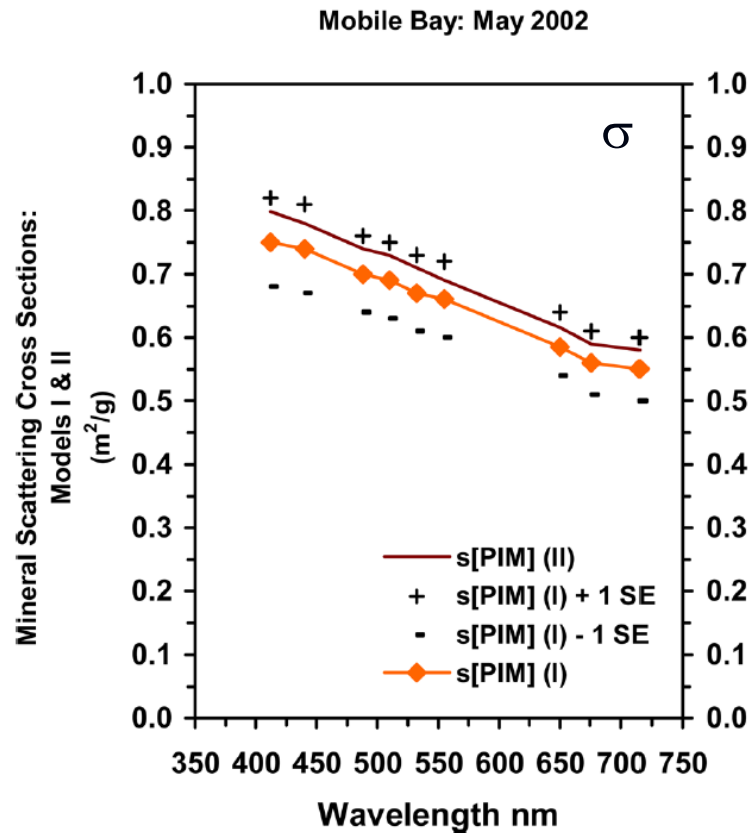


Stramski et al. 1988

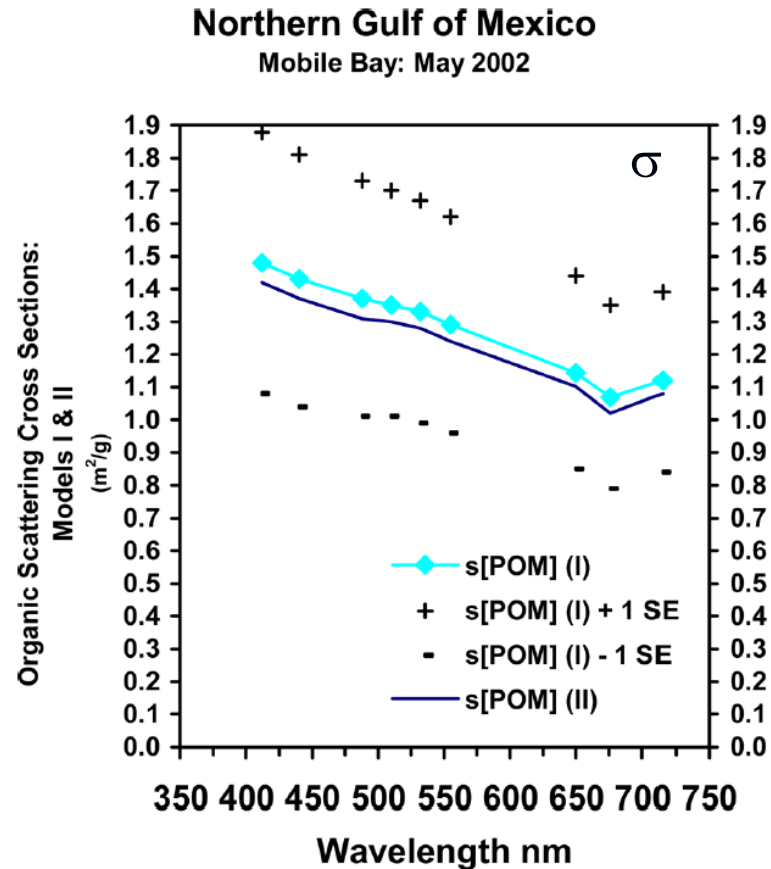


Zaneveld and Kitchen 1995

Spectral scattering by particles



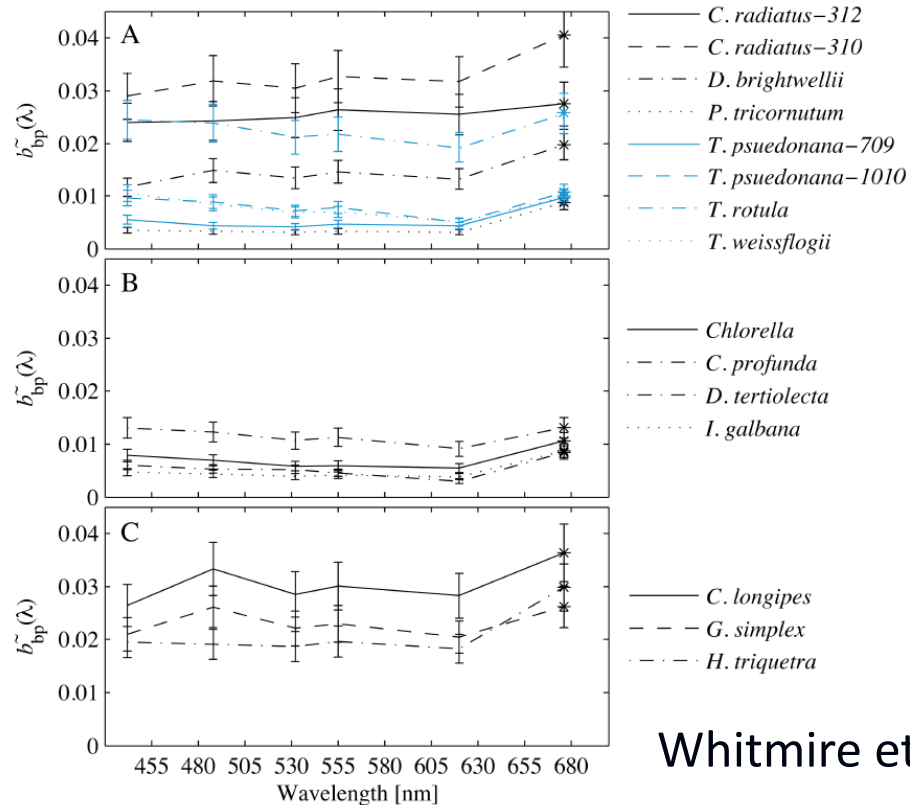
$$b_p = \sigma \text{ PIM}$$



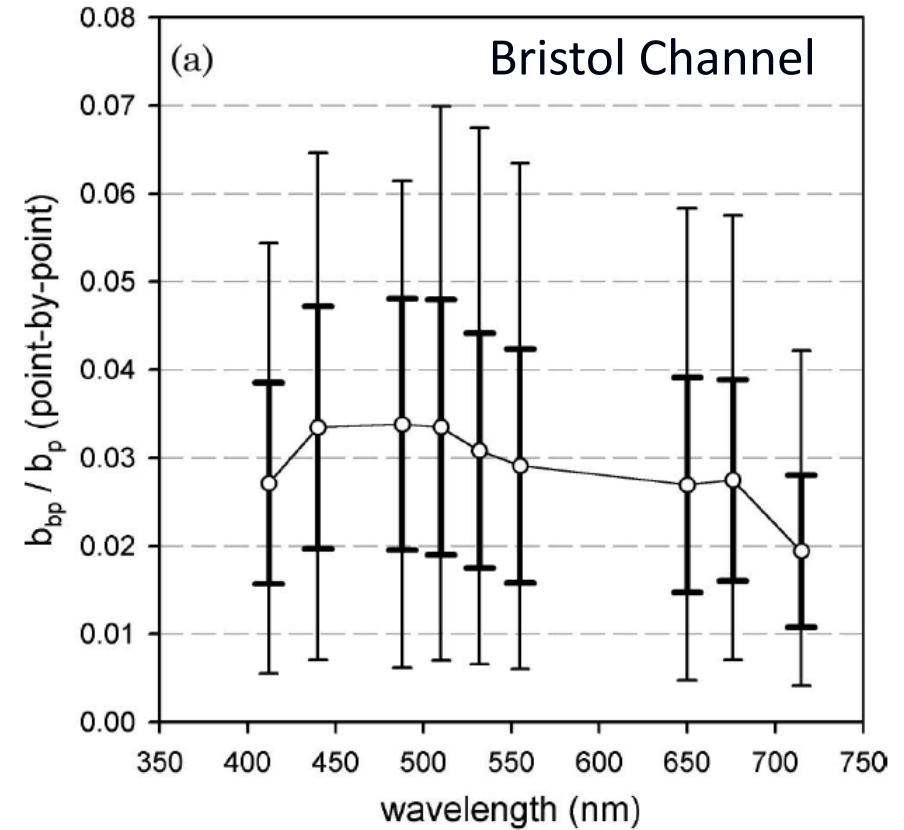
$$b_p = \sigma \text{ POM}$$

Spectral backscattering ratio by particles

For size distribution described by power law,
with relatively low absorption, theory predicts
spectrally independent b_{bp}/b_p
(e.g. Twardowski et al. 2001)



Whitmire et al. 2009



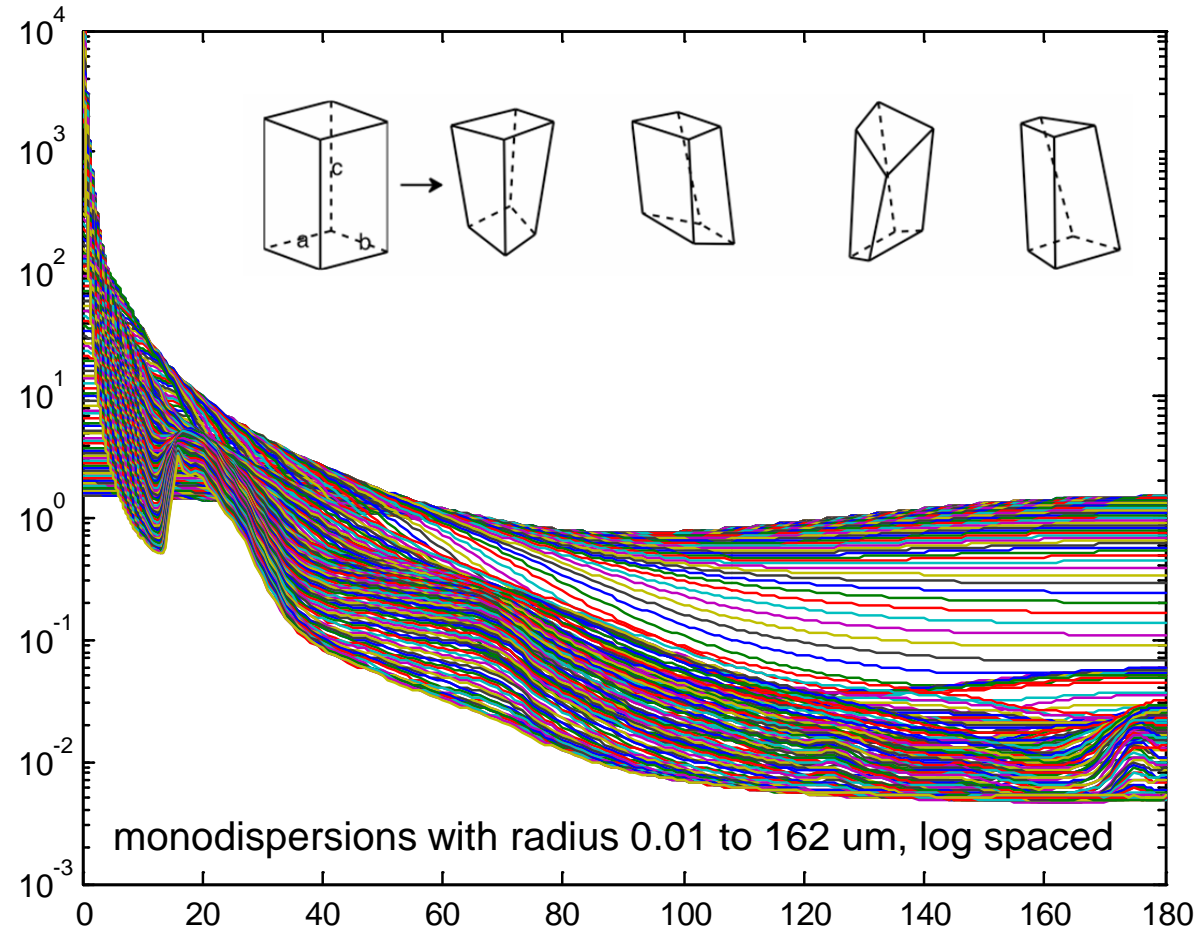
McKee et al. 2009

Models for computing particle scattering

- Rayleigh
- Lorenz-Mie (coated sphere, multi-layer sphere)
- van de Hulst anomalous diffraction approximation
- Geometric optics (IGOM, RBR)
- Discrete dipole approximation (DDA)
- Finite difference, time-domain (FDTD)
- Pseudo-spectral time-domain (PSTD)
- T-matrix (invariant imbedding, multiple sphere, extended boundary condition, many body iterative...)

Each has restrictions: size ranges, n , shape and symmetries

Phase functions of randomly oriented asymmetric hexahedra (mineral-mimicking)

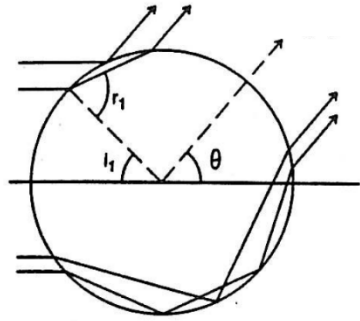


Discrete Dipole
Approx
(DDA)

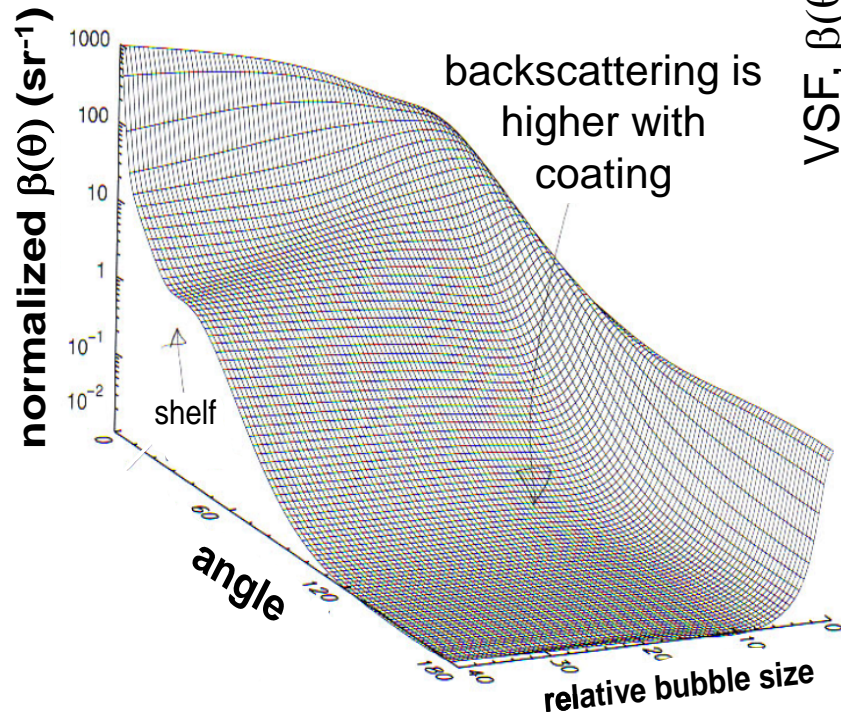
and

Improved
Geometrical
Optics Model
(IGOM)

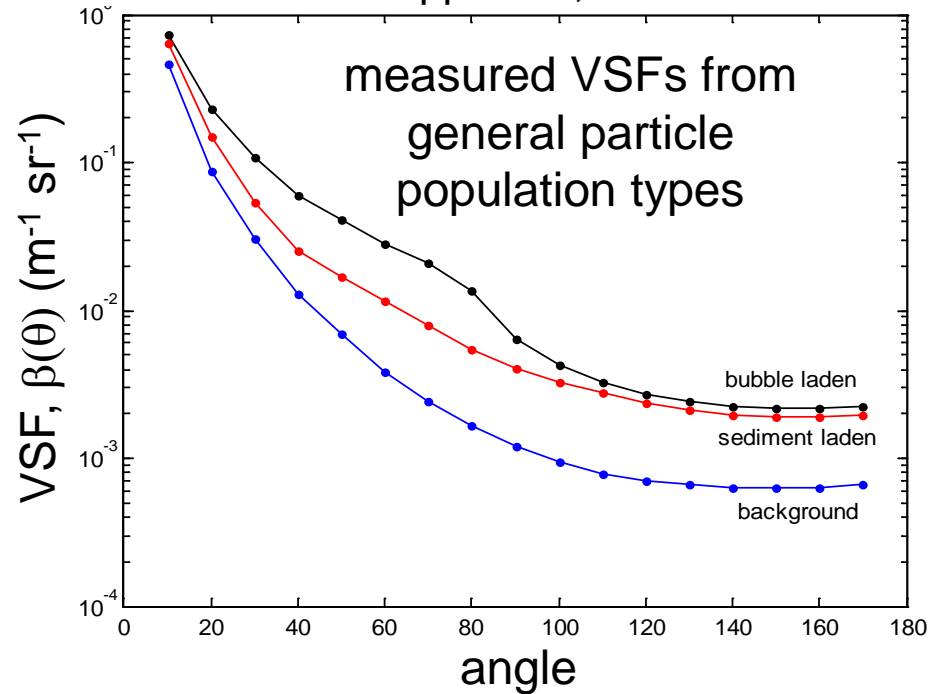
Bubbles



single bubble theory

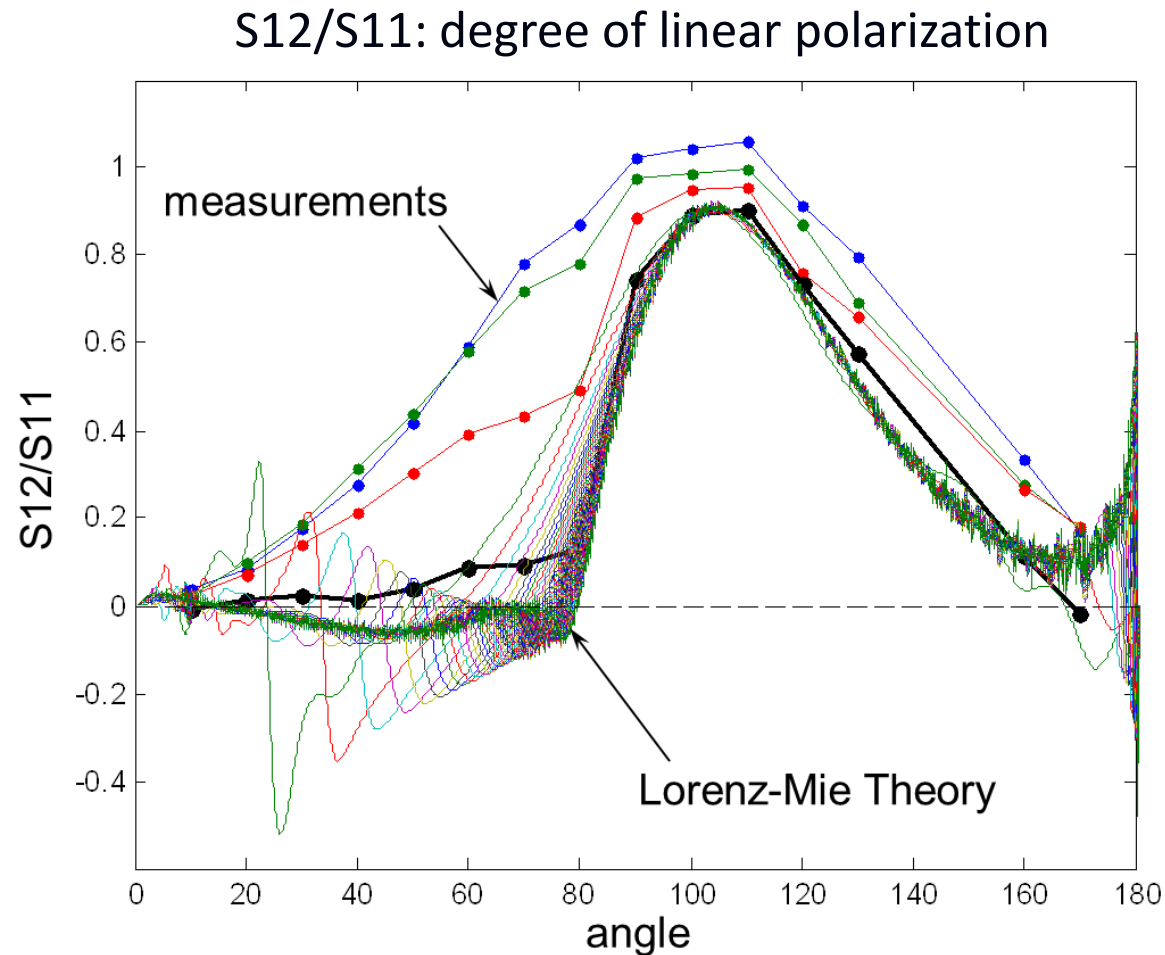


Scripps Pier, 2008



- Different particle populations exhibit different VSF shapes
- Theoretical bubble VSFs verified with *in situ* measurements
- Currently scattering is the only method of resolving small bubbles in seawater

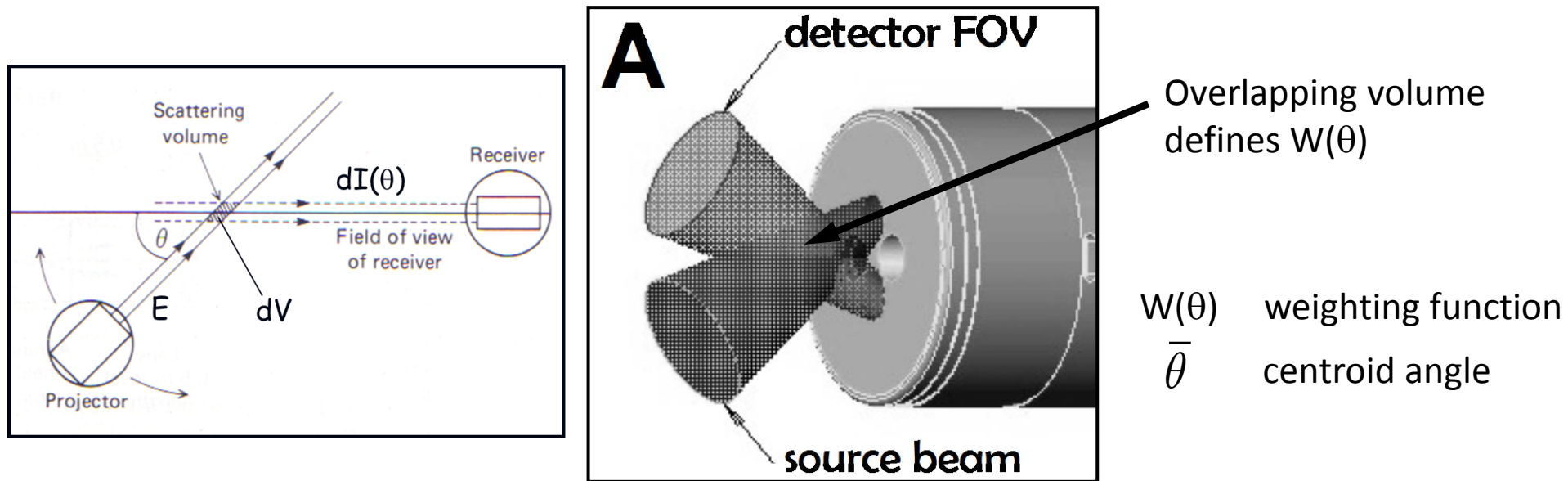
Polarized scattering: effects of bubbles



VSF measurement detail

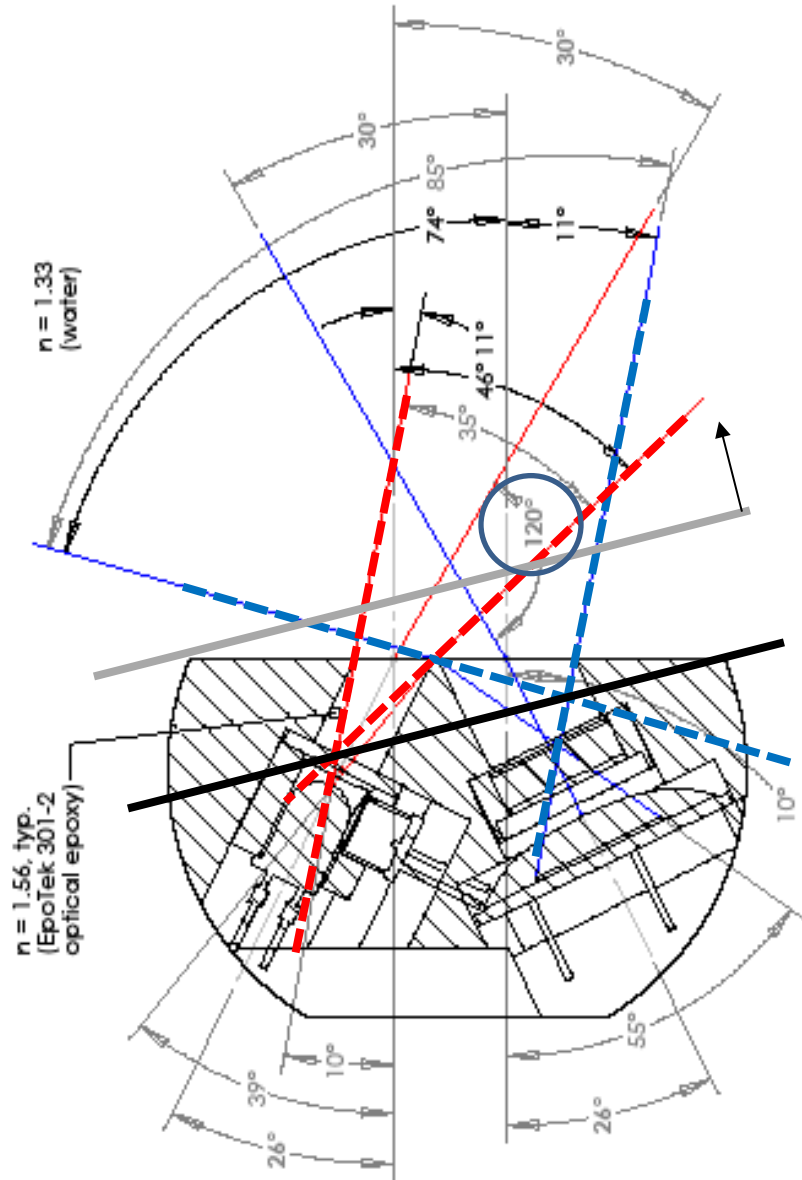
VSF measurement detail

$\beta(\theta)$ measurements are always resolved over a range of angles



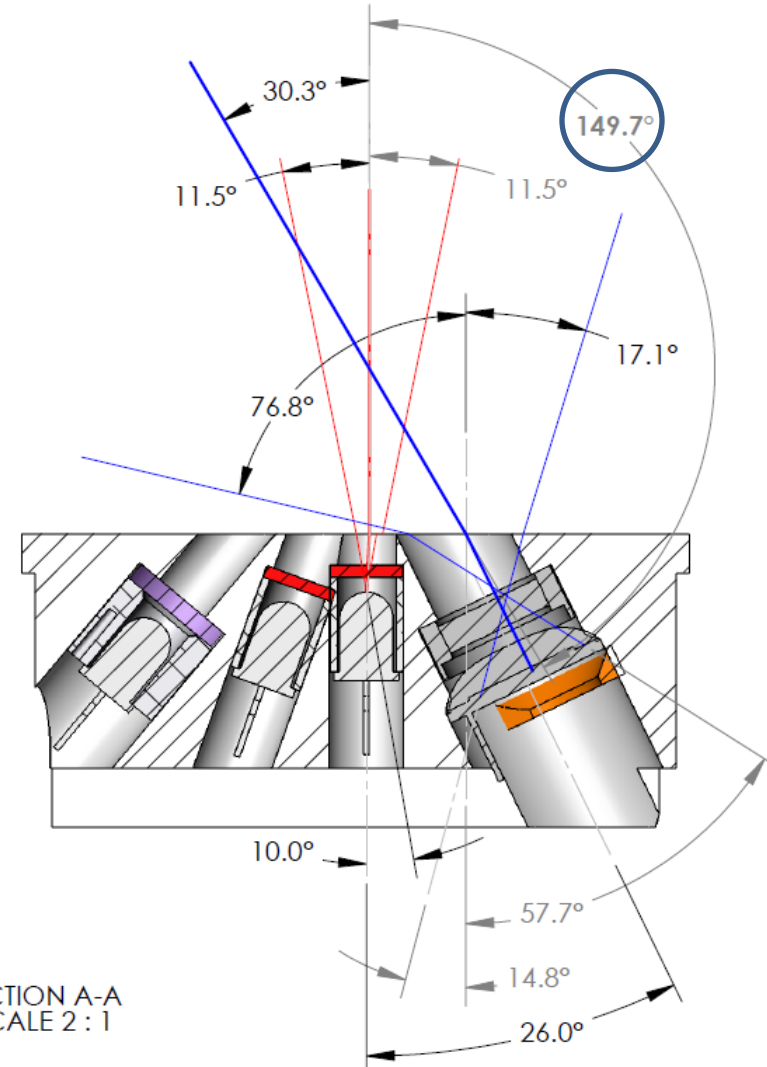
$$\bar{\beta}(\bar{\theta}, \Delta\theta) = \int_0^{\pi} \beta(\theta) W(\theta) d\theta$$

Example of WET Labs ECO geometries



ECO-BB geometry

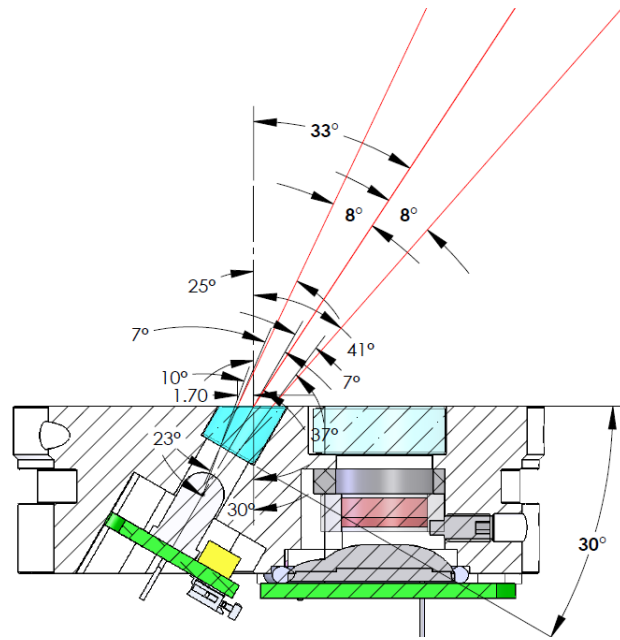
SECTION A-A
SCALE 2 : 1



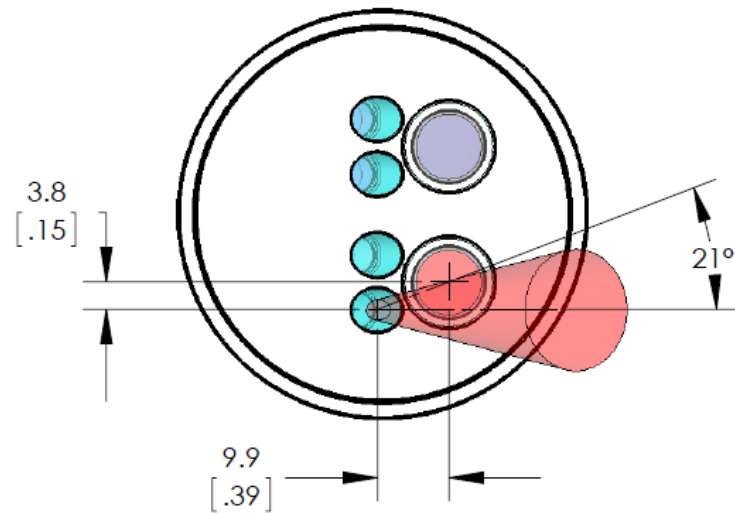
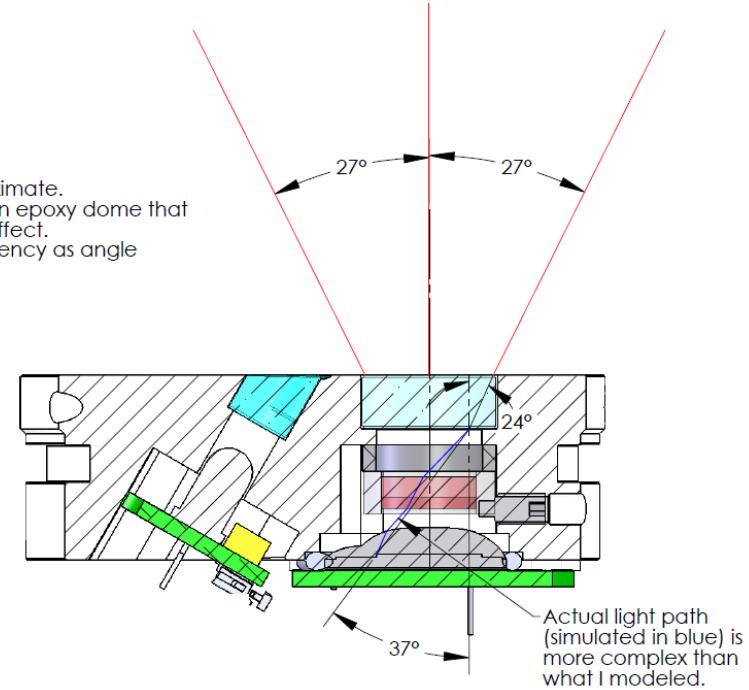
ECO-VSF geometry
(150°)

SECTION A-A
SCALE 2 : 1

WET Labs MCOMS



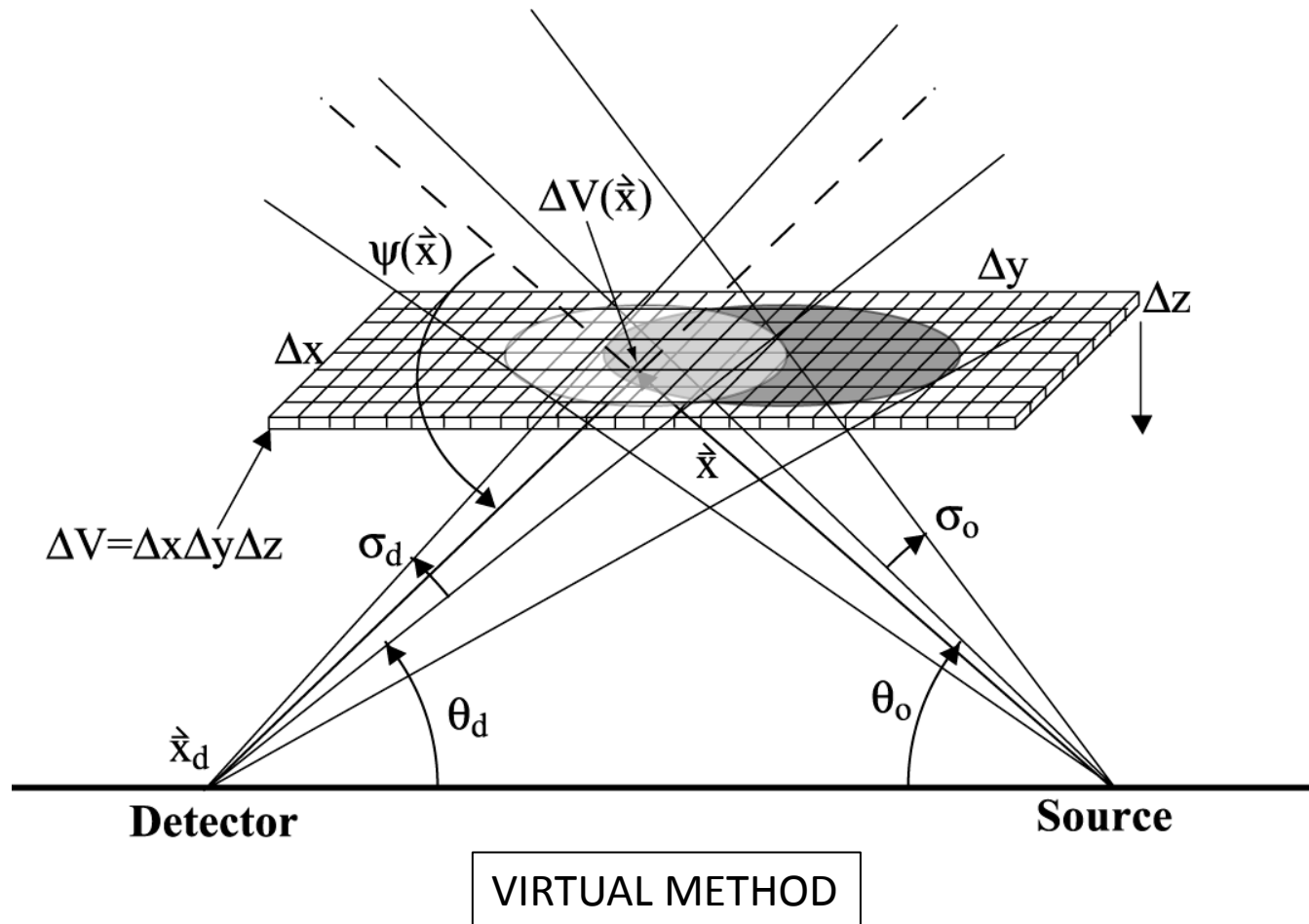
- These angles are approximate.
- The detector has an epoxy dome that has some lensing effect.
 - The filter loses efficiency as angle increases.



Determining $W(\theta)$

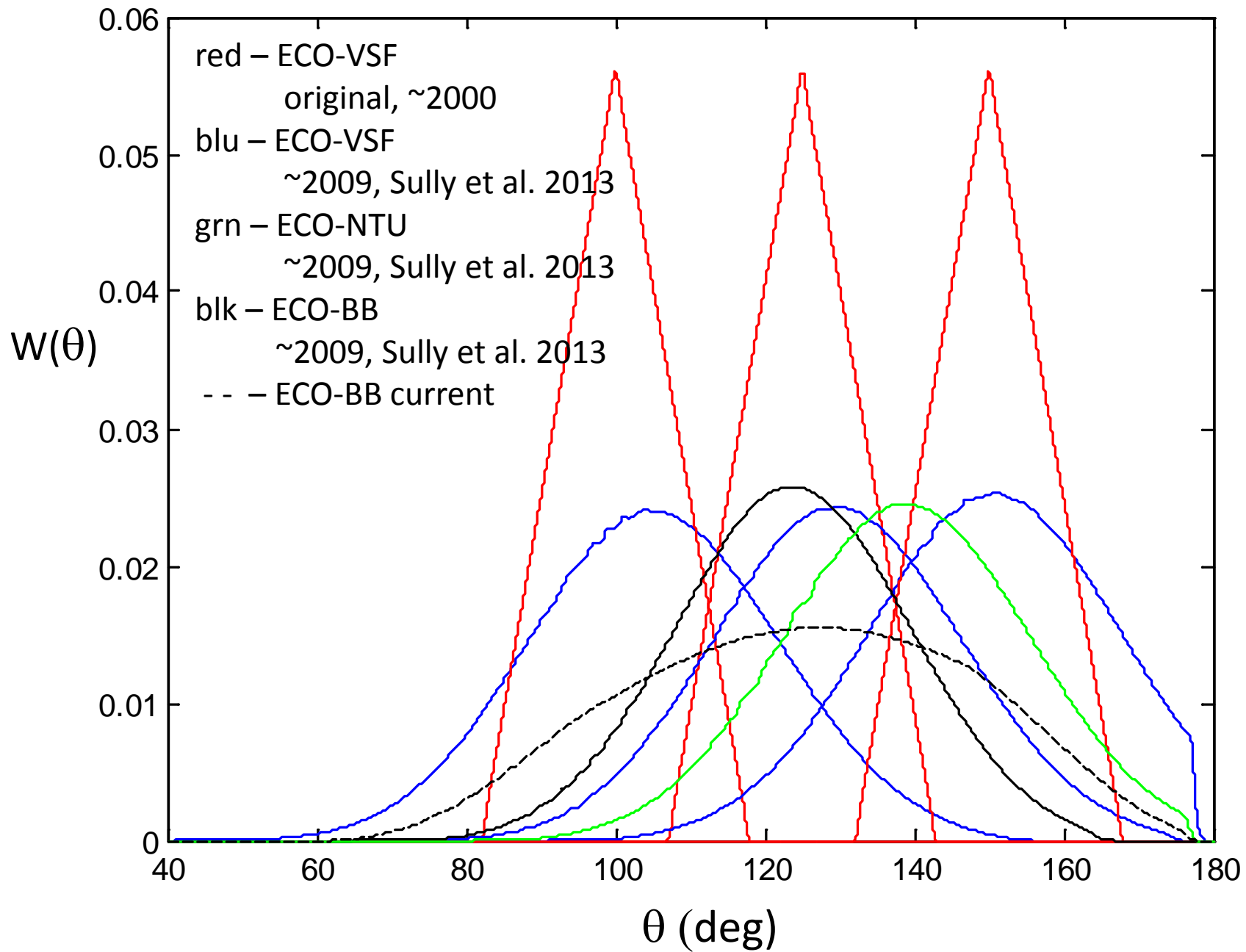
Experimentally (Maffione and Dana 1997) – the plaque method

Analytically (Sullivan et al. 2013) – the “virtual plaque” method



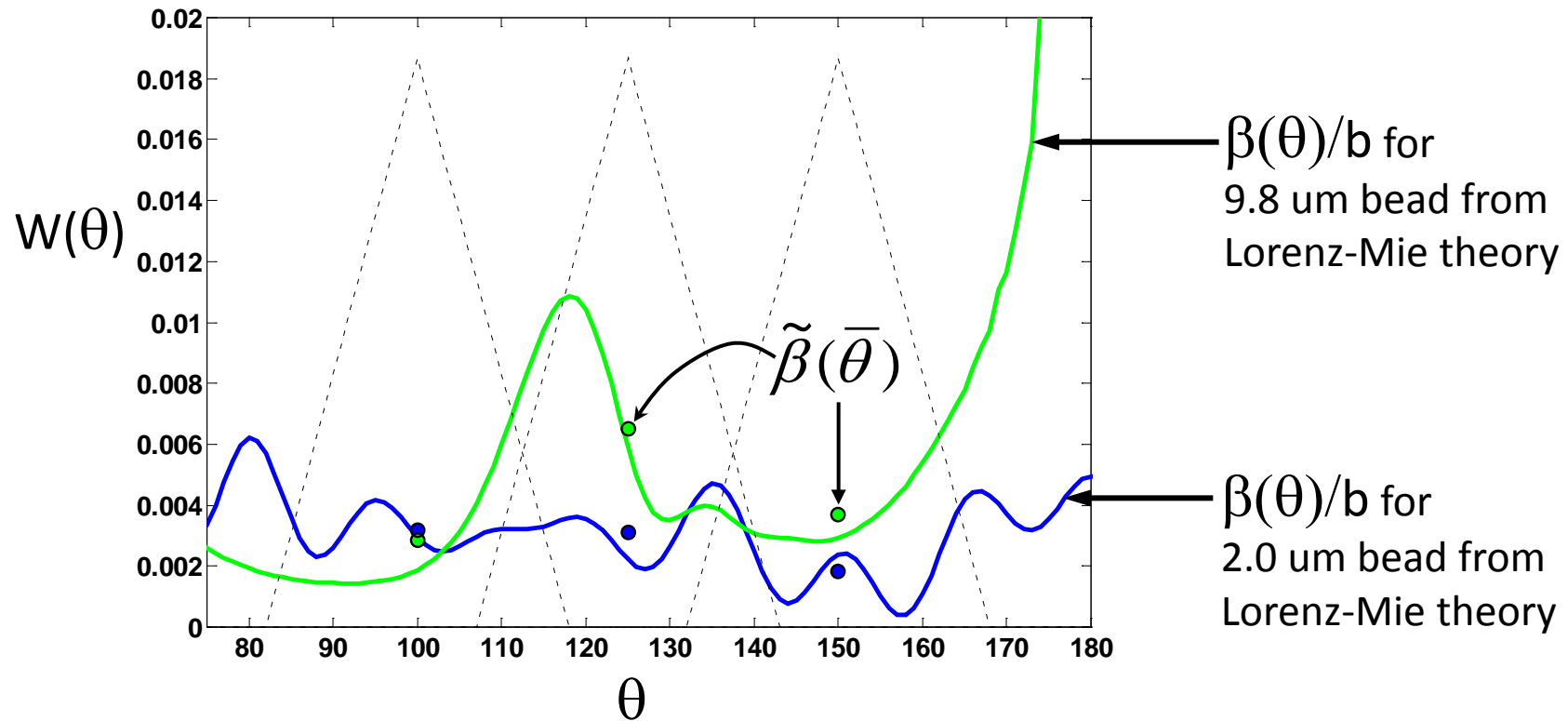
- Step virtual plaque through sample volume
- Determine area where source and detector beam images overlap for each z step
- Calculate power returned to detector at each dV in the overlapping area (note there is no consideration of VSF in doing this)
- Assign θ to each dV
- Compile results (i.e., fill θ bins) to derive weighting function

ECO weighting function history



Calibration: Step 1

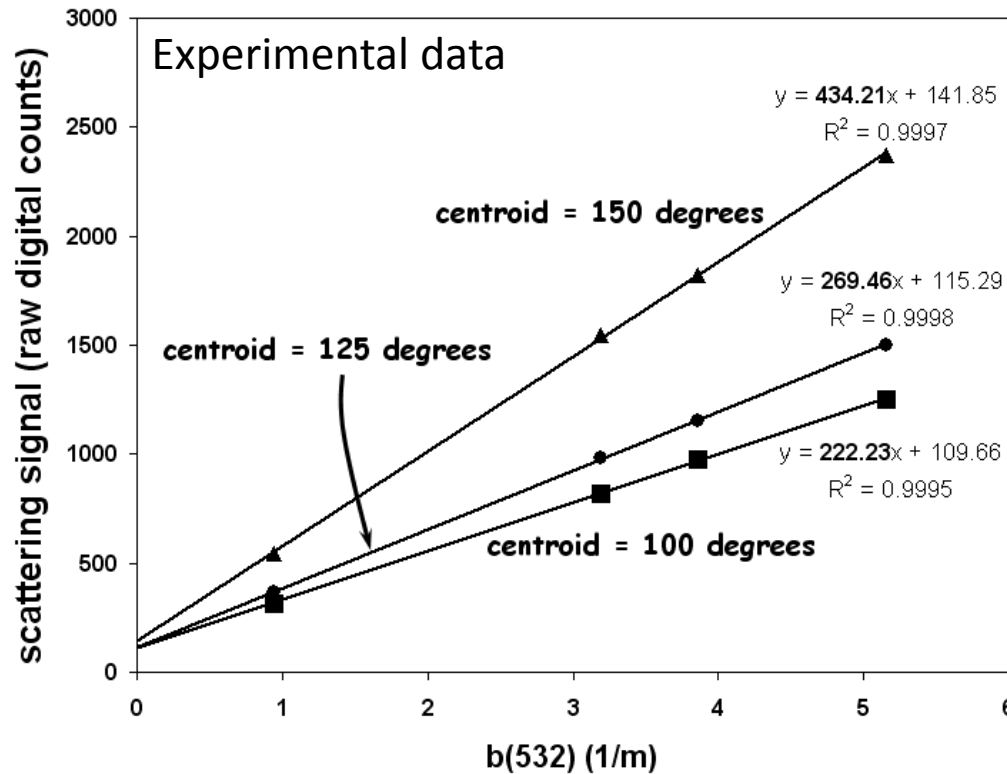
Compute phase function of easily modeled particle solution (e.g., microspherical beads) and convolve with $W(\theta)$



*use a Rayleigh scatterer ($d < \lambda$) for best results

Calibration: Step 2

Place sensor in the solution with known phase function and measure raw digital counts and b (with ac9)



Intercepts are nonzero because

- 1) scattering sensor dark counts
- 2) ac9 is not calibrated precisely
- 3) insufficient water purity

these do not matter because the slope is what you care about, i.e., the change in counts per change in b

Calibration: Step 3

Compute scaling factor, SF

$$SF = \frac{\beta(\bar{\theta})}{b} \frac{\overset{\text{experimental}}{\downarrow} b}{counts} = \frac{\beta(\bar{\theta})}{counts}$$

↑
theory

Calibration: Step 4

Determine dark offset, DO



- black tape over detector only
- put in water to match refractive index
- average time record (~30 s)

Applying the calibration

$$\beta(\bar{\theta}) = \text{scaling factor} \left(\text{raw counts} - \text{dark offset} \right)$$

Important...

- All $\beta(\theta)$ measurements are not equal due to instrument-specific $W(\theta)$
- Measurements of $\beta(\theta)$ in the field will include water. Water from highest quality purification systems is not close to being clean enough for calibrations (pure water itself is several counts of signal)
- Ambient light rejection circuitry important for backscattering measurements

Correction for attenuation

Sometimes required because light is attenuated on its way to and from the sample volume

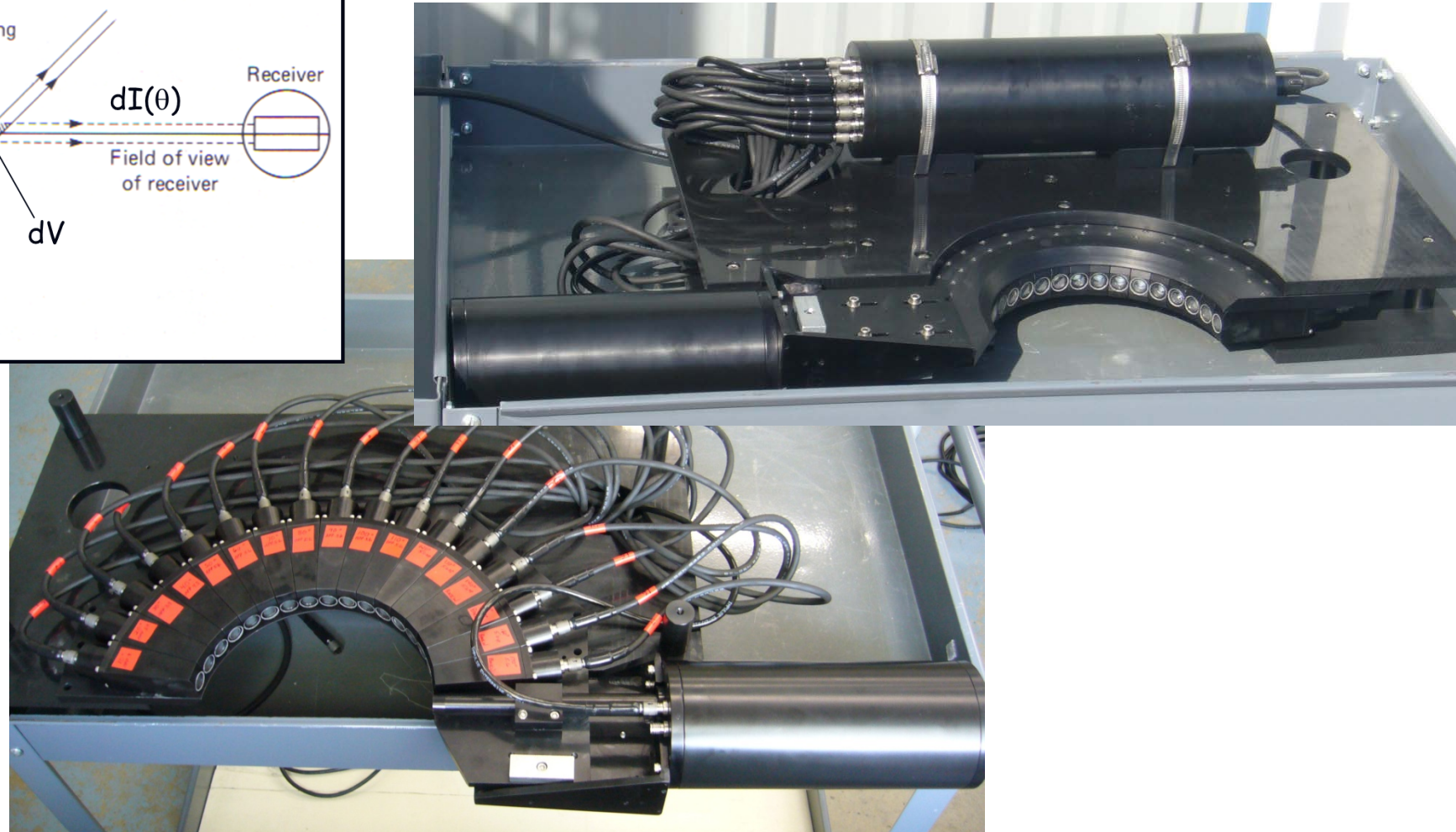
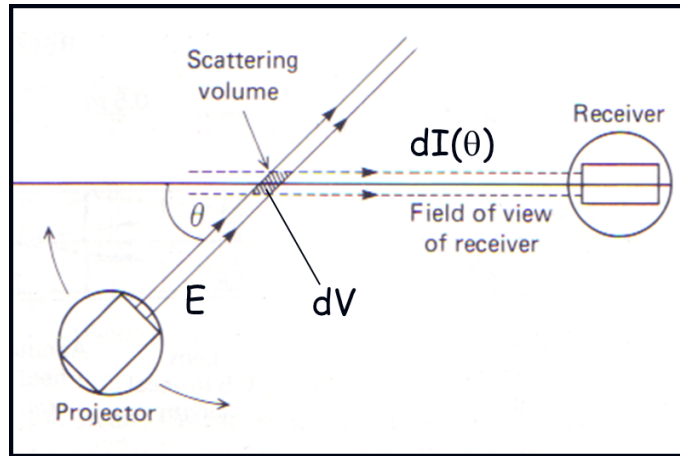
For bead calibration, scattering portion of attenuation is inherently corrected
(close enough for ECOs...)

only need to correct for absorption when it is very high (> ~2 1/m)

$$\beta_{\text{corr}} = \beta_{\text{meas}} \exp(aL)$$

This is an approximation, valid when pathlength L is small

When pathlength is not small: MASCOT (Multi-Angle SCattering Optical Tool)

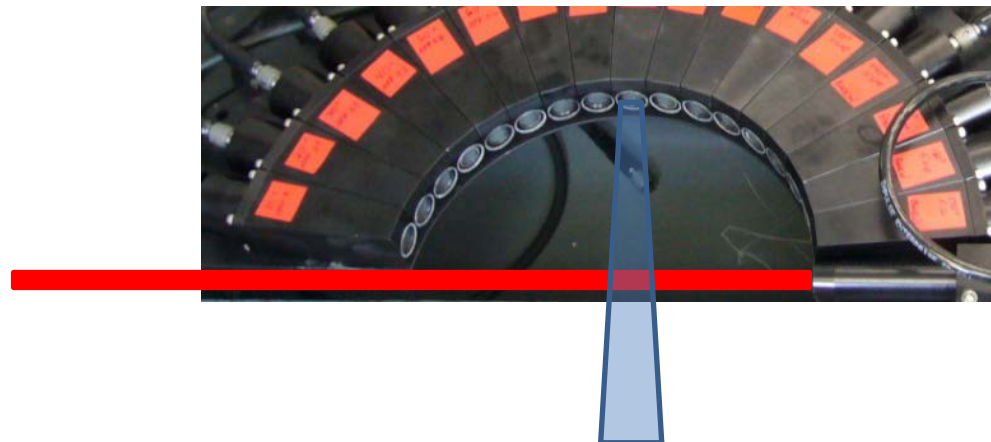


Full correction for attenuation

$$\beta(\bar{\theta}_i) = \frac{R_{cal}}{R_m} [\Phi_i - D_i] f_i e^{L[b_p \varepsilon + a_{pg} + a_w]}$$

R – source references

ε – fraction of scattering that is not included in the measurement



$L \sim 20$ cm

See Twardowski et al. (2012) for full details

Obtaining backscattering coefficients with β at limited θ

With a single $\beta(\theta)$ in the backward hemisphere

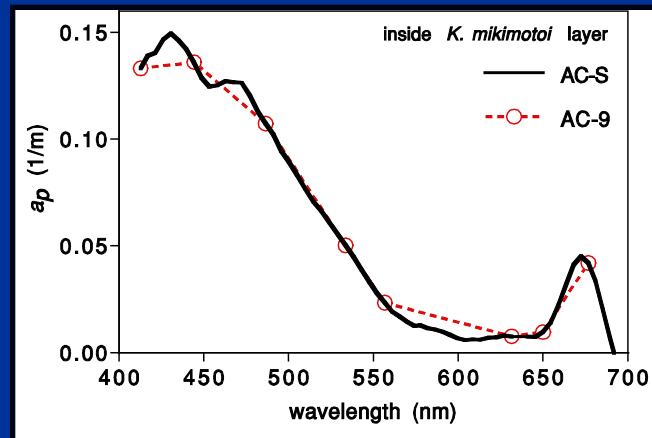
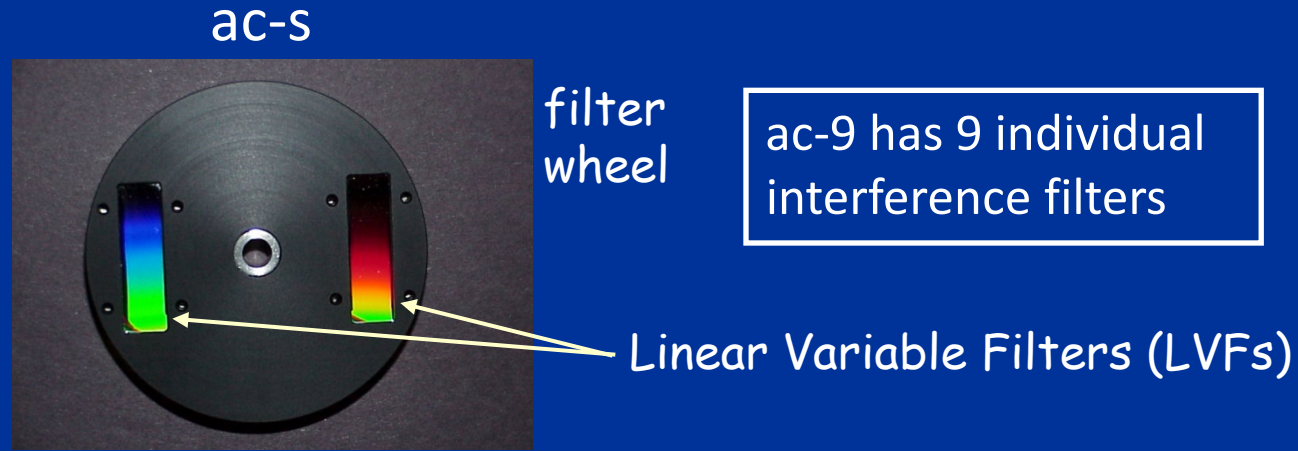
$$b_{bp} = \chi(\theta)2\pi\beta_p(\theta)$$

Much discussion over which θ and which χ to use:

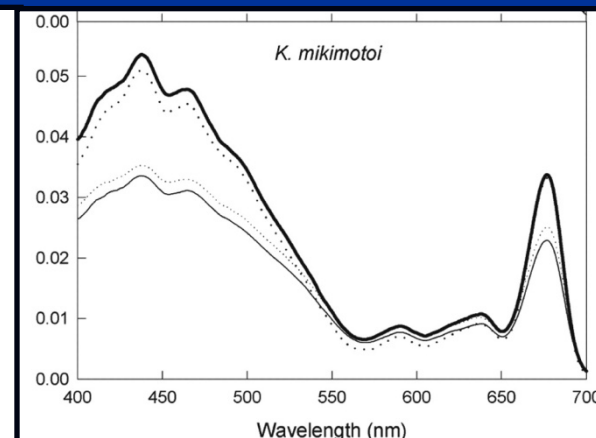
- Oishi (1990): **120°**
- Maffione and Dana (1997): **140°**
- Boss and Pegau (2001): **117°**
- Sullivan and Twardowski (2009): **118°**

For most accurate current protocol, see Sullivan et al. (2013)

Deriving total scattering (b) from a and c : WET Labs ac-9 and ac-s

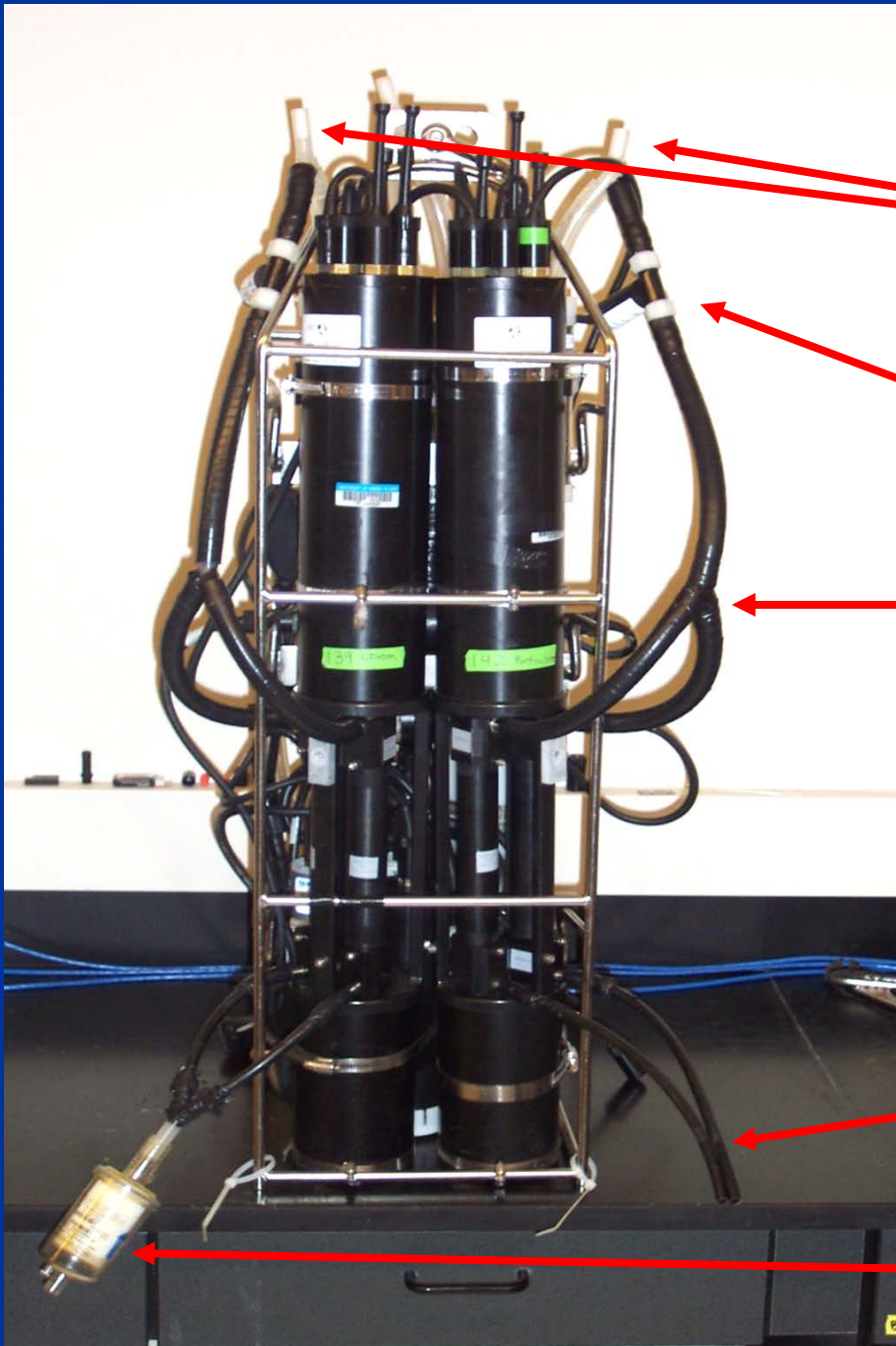


Sullivan and Donaghay (2004)
Irish fjord



Stahr and Cullen (2003)
In culture

$c_{pg}, a_{pg}, a_g, c_p, a_p, b_p$ from dual ac's



degassing "Y's"
(pumps below Y's)

in-line flow sensor

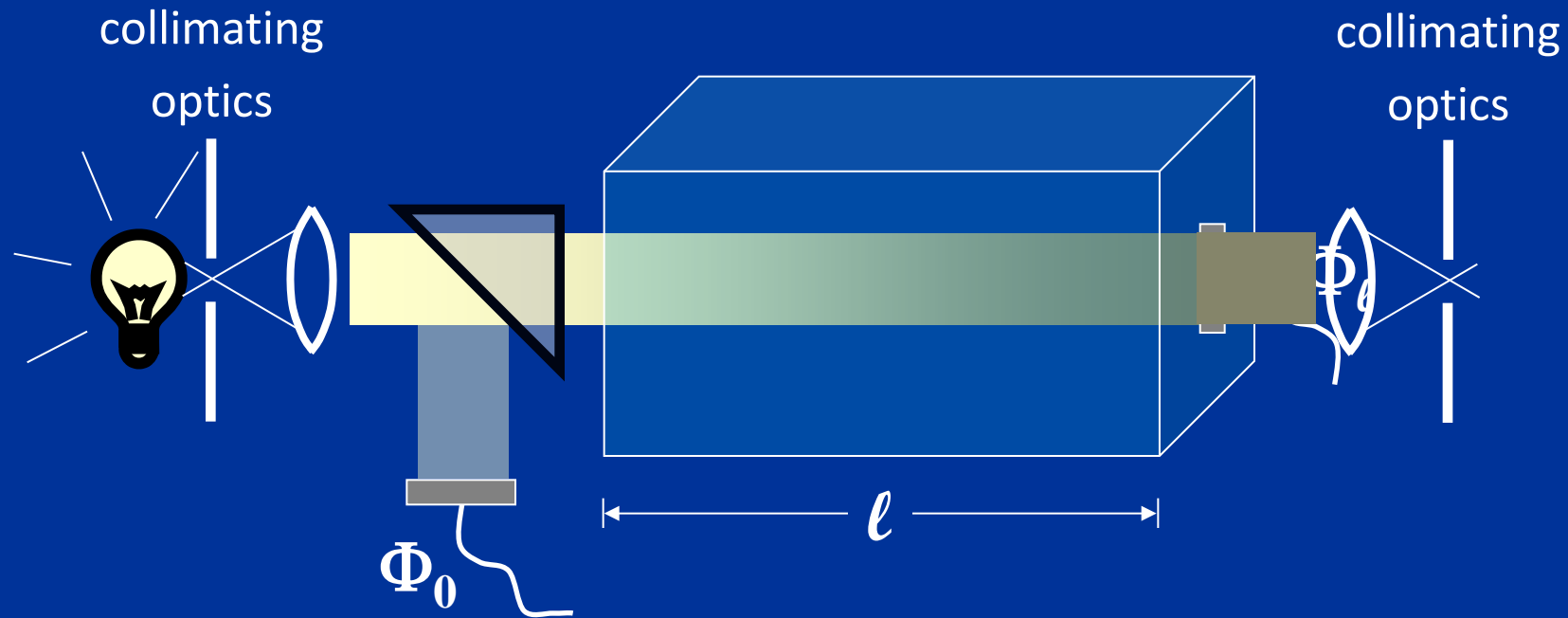
"Y" on outtakes

"smooth" flow paths

unfiltered (separate intakes)

0.2 μm pre-filter (using Y intake)

Anatomy of a beam attenuation meter (transmissometer)



The theoretically ideal attenuation meter has an acceptance angle of $\sim 0^\circ$ but at 0° no light is received – need to compromise

Problem: some scattered light also reaching detector

Beam attenuation errors from near-forward scattered light

Table 1. Configuration specifications on beam attenuation meters

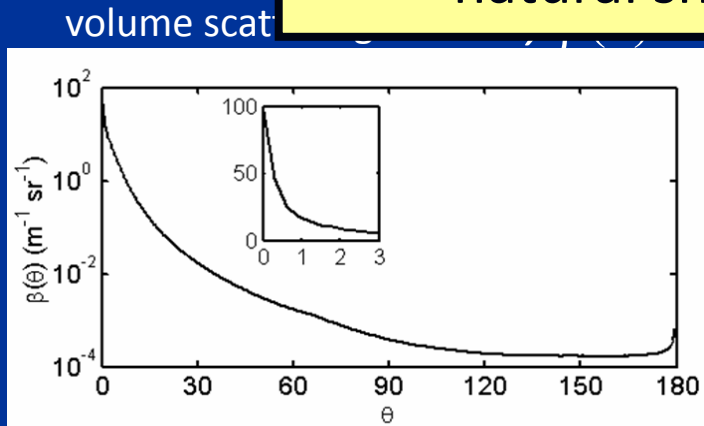
Instrument	beam source	beam width	acceptance angle (degrees)	pathlength (cm)
AlphaTracka	LED	15 mm	0.86	5
Sequoia LISST	solid state diode laser	6 mm	0.018, 0.036	5
WETLabs ac9	collimated incandescent bulb	10 mm	0.93	25
WETLabs cstar	L			

Instrument design must make compromises in acceptance angle, θ_a :

- Size
- S:N, accuracy
- Turbulence at $<0.1^\circ$

Errors dependent on both optical geometry AND natural shape of VSF

Remember...

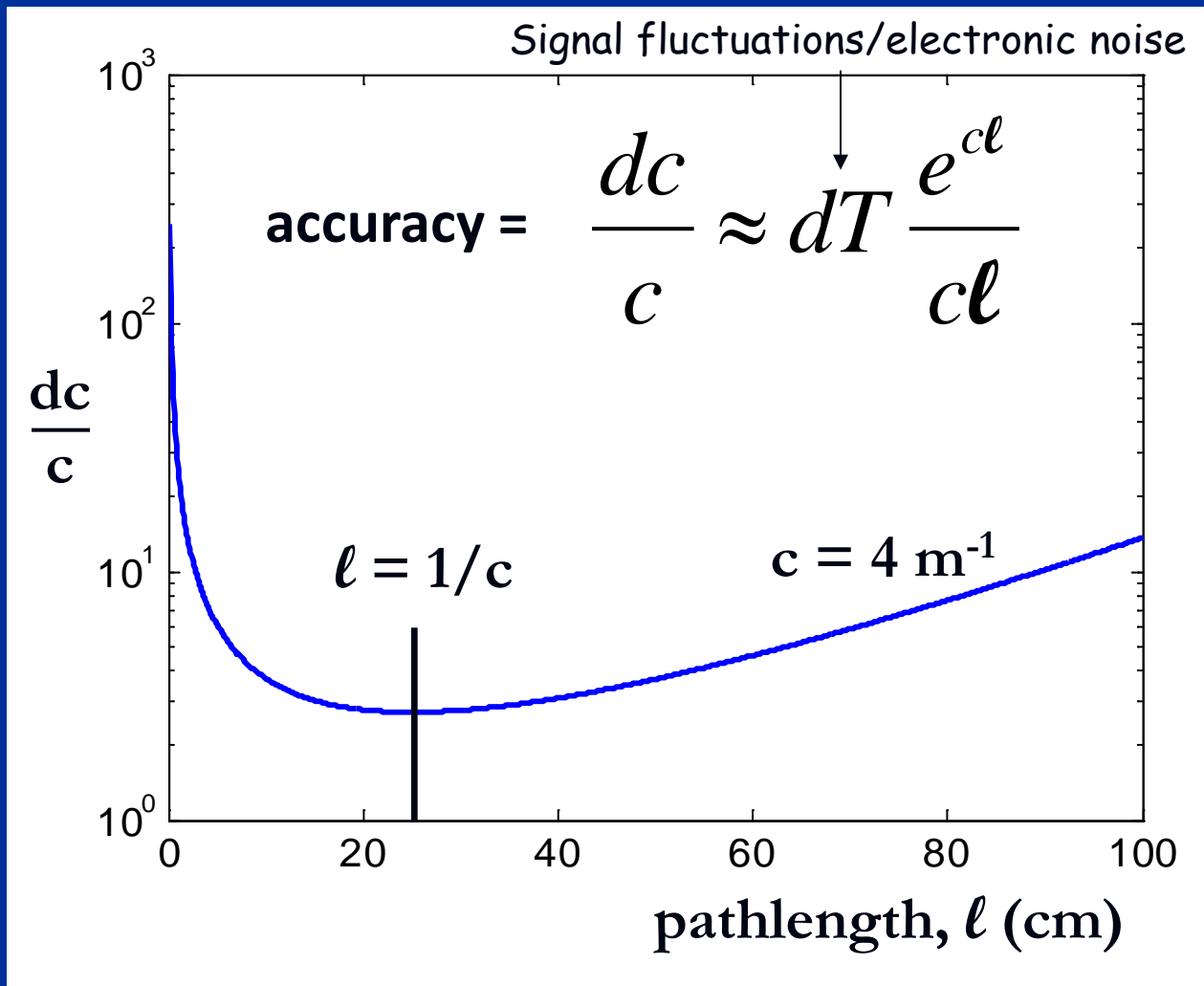


... as detected

$<0.1^\circ$	few percent?
0.7°	15-25%
0.93°	19-30%
1.5°	25-37%
1.9°	28-42%

based on Petzold VSFs

Accuracy

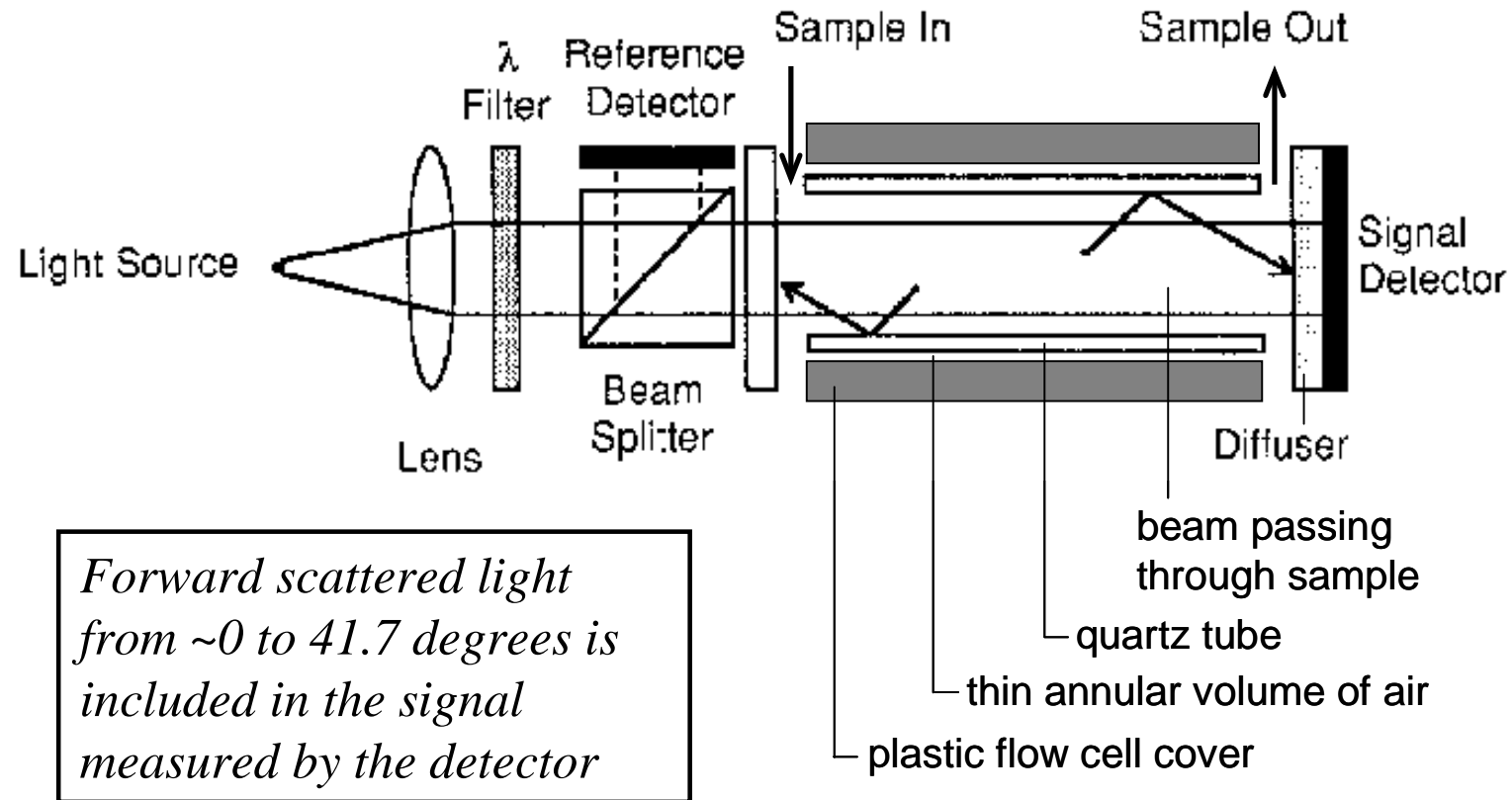


Accuracy is optimized when dc/c is minimized

Minimum occurs when $cl \approx 1$

Choose pathlength accordingly...

Reflective tube method for absorption



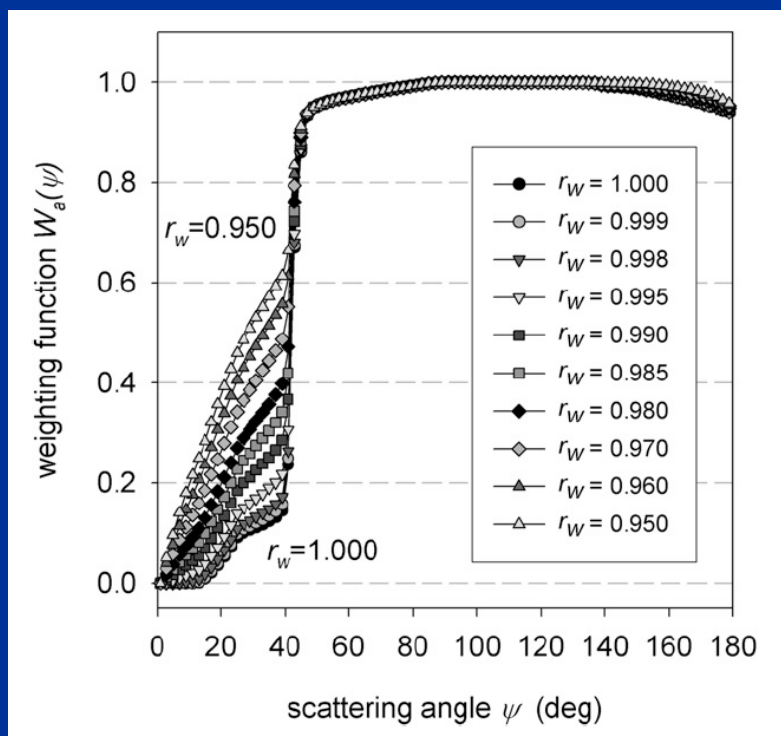
from Zaneveld et al. (1992)

Scattering error with reflective tube absorption

- Scattered light from $\sim 41^\circ$ - 180° not measured
 - error usually ~ 15 - 22% of b and there are correction schemes (see Zaneveld et al. 1994)

There is a weighting function, $W(\theta)$ that defines the scattering error:

$$error = 2\pi \int_0^{180^\circ} W(\theta) \beta(\theta) \sin(\theta) d\theta$$



Can find r value that provides closest results to PSICAM (R. Rottgers)

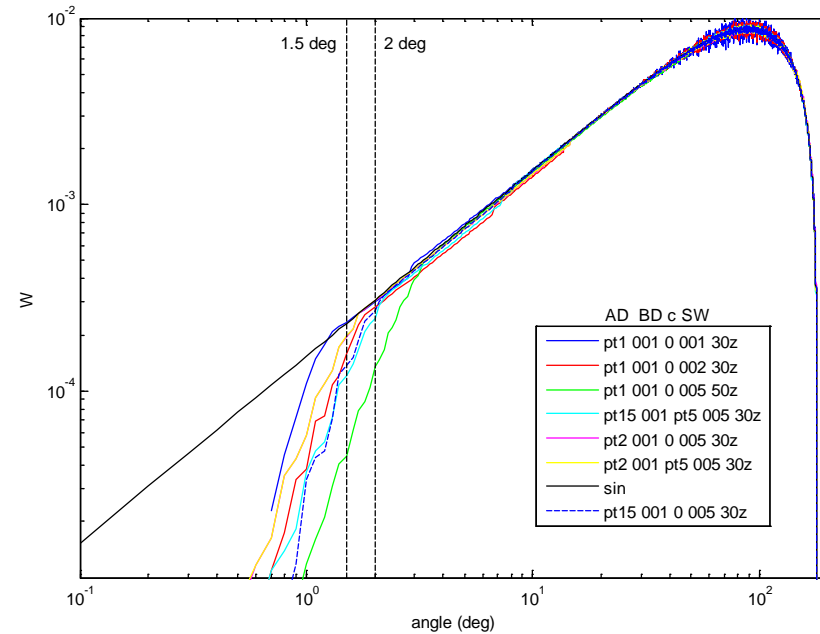
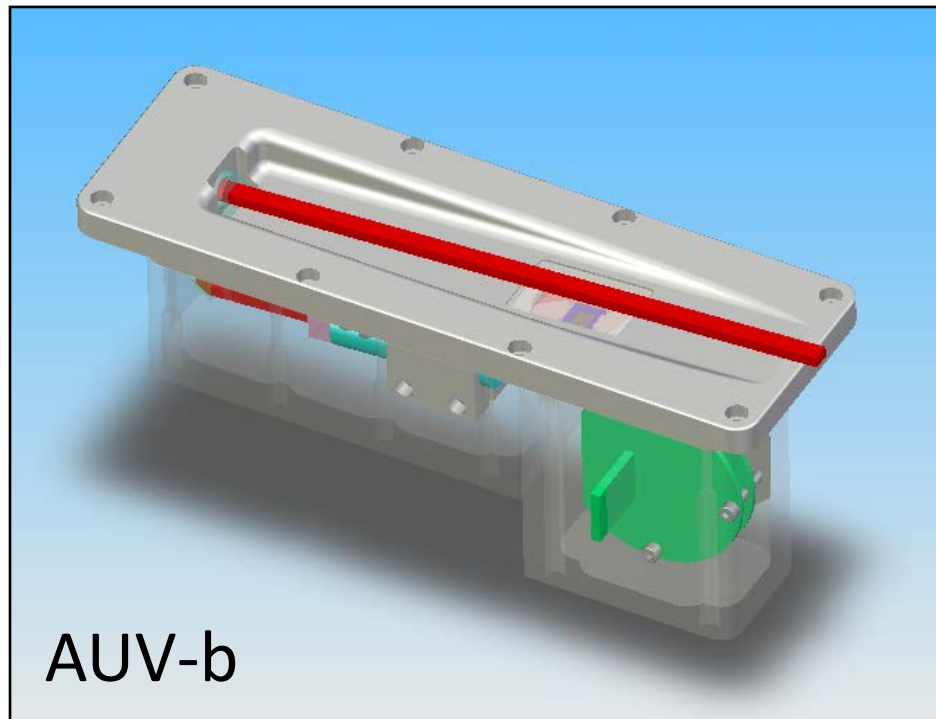
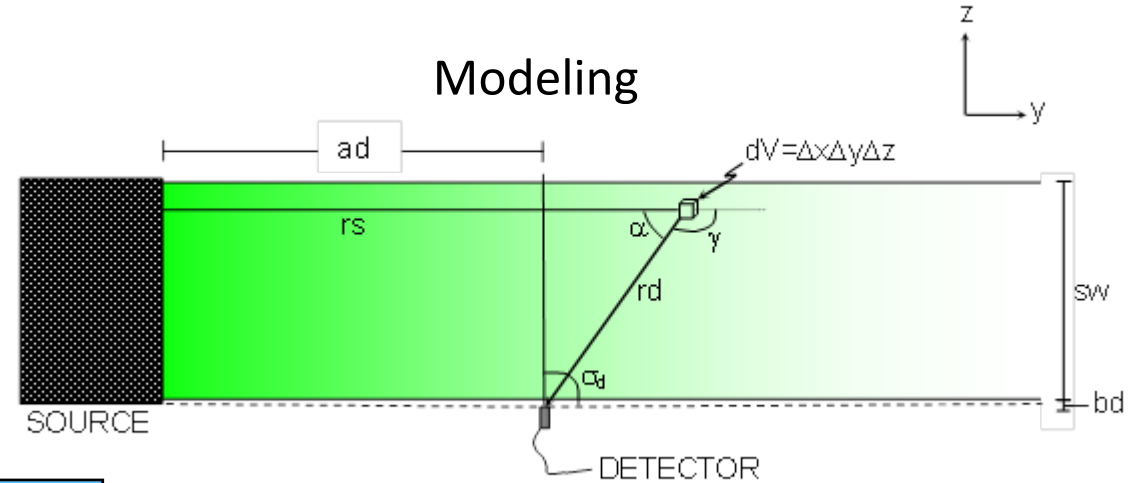
- Found 97% to 98% (Stockley et al., in prep)
- Variability possibly attributed to aging ac device tubes

McKee et al. (2013)

Measuring total scattering, b

Remember...

$$b = 2\pi \int_0^\pi \sin(\theta) \beta(\theta) d\theta$$



Very close to $\sin(\theta)$ weighting function

Combination bb-b meter

Fry and Twardowski

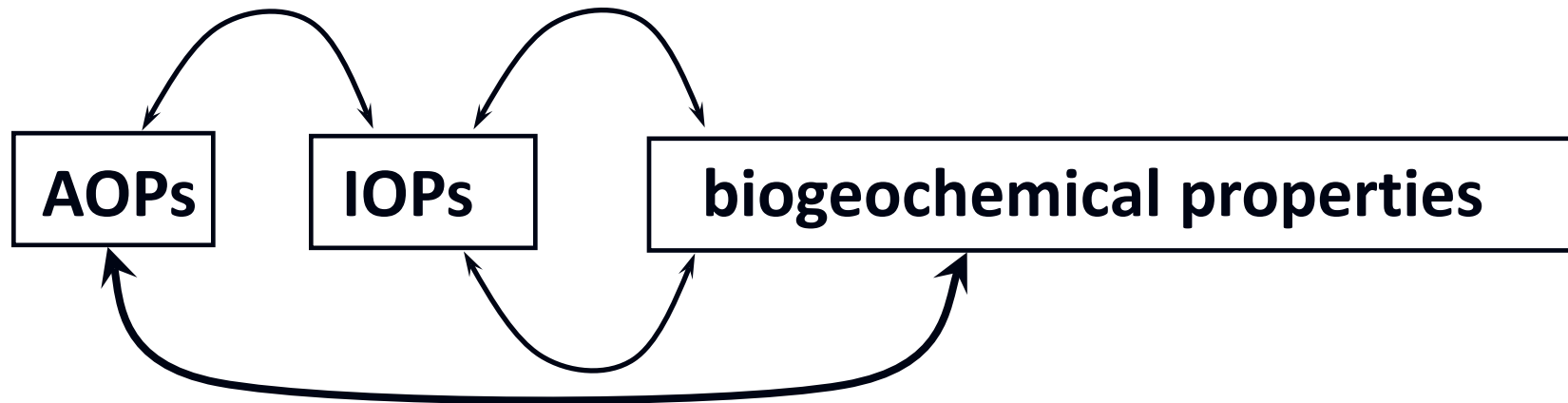
NSF project



Interpretation and Application

General paths for application

Analytical: from first principles



Empirical: statistical correlations

Usually empirical methods are based on some theoretical principle, and “analytical” methods usually must include some empiricism.

Scattering as a proxy for biogeochemical properties

A common example → Beer's Law: $IOP = \epsilon[\text{conc}]$

Some biogeochemical properties that influence optical properties:

chlorophyll, phytoplankton pigments, particle size, particle density, particle composition, particle shape, particle concentration, total particle mass (TSM, SPM), POM/C, DOM/C, biomass, humic substances, hydrocarbons, CaCO₃,...

However: pools of particulate and dissolved matter can be highly variable and complex in composition, especially in coastal regions, usually confounding simple relationships.

Links Between IOPs & Biogeochemicals

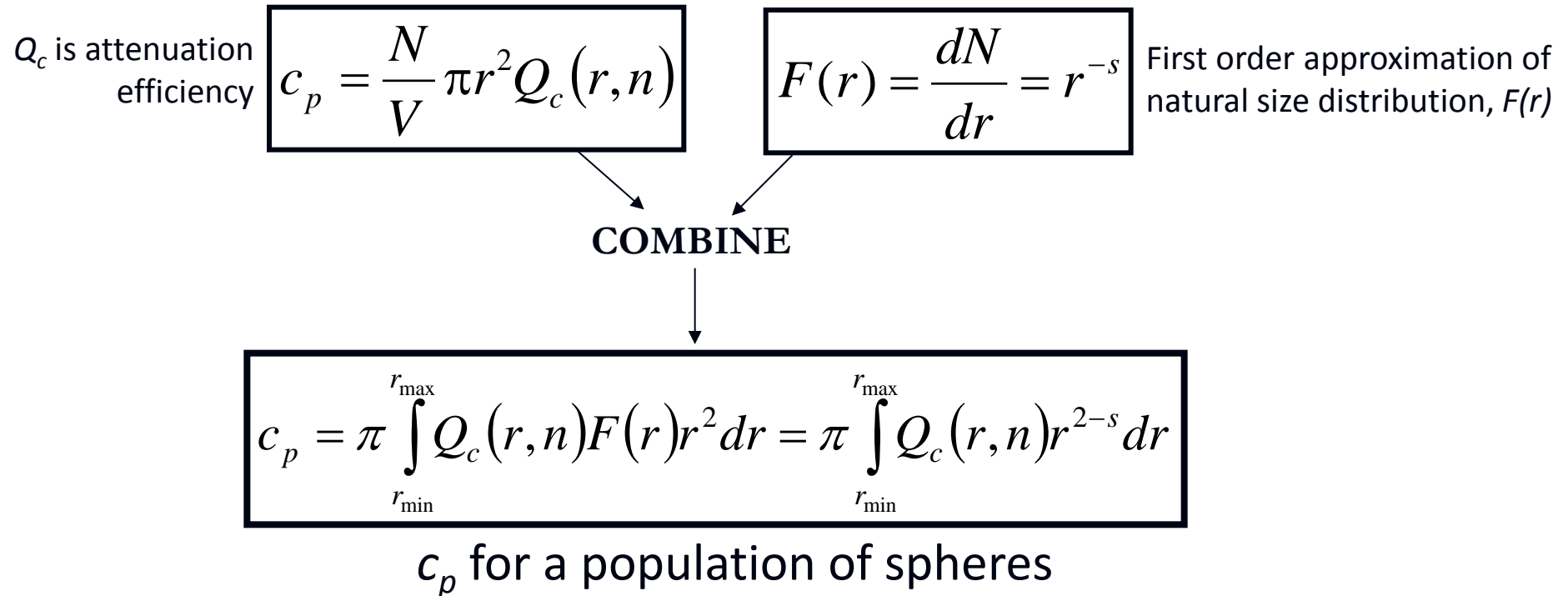
- Chlorophyll
- POC
- TSM
- DOM, DOC
- Phytoplankton pigments
- Size distribution
- Bulk refractive index
- Sewage
- Hydrocarbons
- ...

Table 1. Some biogeochemical properties derived from optical properties.

Biogeochemical property	Optical Property	Example Reference(s)
Particulate Organic Carbon (POC)	1) c_p or b_p	Peterson 1978; Gardner et al. 1993, 2001; Loisel and Morel 1998; Bishop 1999; Bishop et al. 2002; Claustre et al. 1999, 2000; Mishonov et al. 2003
Total Suspended Matter (TSM)	2) b_{bp}	Stramski et al. 1999; Balch et al. 1999
	1) c_p or b_p	Peterson 1978; Gardner et al. 1993, 2001; Walsh et al. 1995; Prahl et al. 1997
Dissolved Organic Matter or Carbon (DOM, DOC)	2) turbidity	Fugate and Friedrichs 2002
	1) a_g	Pages and Gadel 1990; Vodacek et al. 1997
DOM composition ^a	2) Fluorescence	Coble et al. 1993; Ferrari et al. 1996; Klinkhammer et al. 2000
	1) a_g , spectral shape	Carder et al. 1989; Blough and Green 1995
Chlorophyll	2) Fluorescence, multi-spectral shapes	Coble 1996; Del Castillo et al., 1999; McKnight et al. 2001
	1) a_p	Bricaud et al. 1998; Claustre et al. 2000
Phycobiliproteins	2) Fluorescence	e.g., Yentsch and Menzel 1963; Claustre et al. 1999
	Fluorescence	Cowles et al. 1993; Sosik et al. 2002
Phytoplankton pigment ratios	a_p , spectral shape	Trees et al. 2000; Eisner et al. 2003
Proteins	Fluorescence	Coble et al. 1993; Mayer et al. 1999
Hydrocarbons	Fluorescence	e.g., Holdway et al. 2000
Particle size distribution	1) c_p , spectral shape	Morel 1973; Boss et al. 2001
	2) $\beta(\theta)$	Brown and Gordon 1974; Zaneveld et al. 1974; Agrawal and Pottsmith 2000
Particulate refractive index	1) $\beta(\theta)$	Brown and Gordon 1974; Zaneveld et al. 1974
	2) $c_p(\lambda)$, b_{bp} , and b_p	Twardowski et al. 2001
Sewage	Fluorescence	Petrenko et al. 1997
Nitrate	UV absorption	Johnson and Coletti 2002

^aFor example – ratio of dissolved humic acid to fulvic acid, DOM molecular size distribution, DOM aromaticity, DOM source

How is c_p (or b_p or b_{bp}) linked to particles?

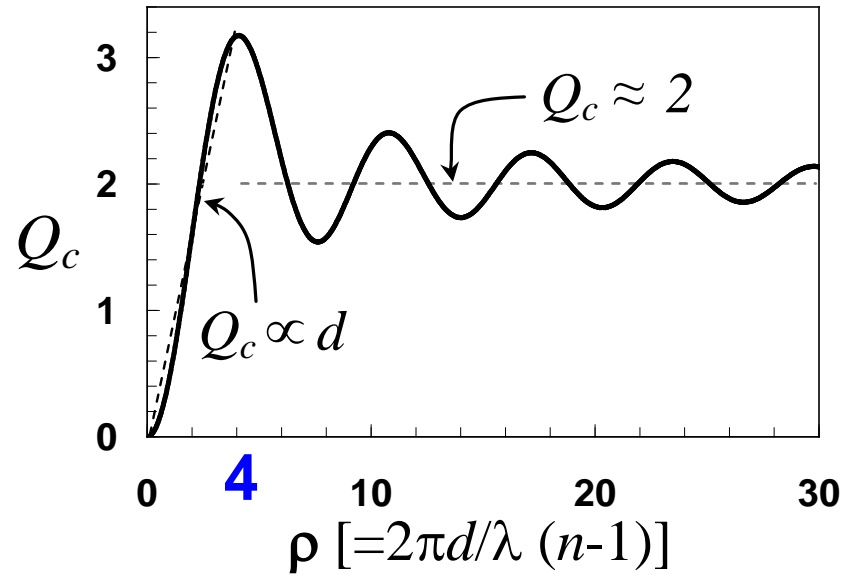


Widely varying natural size distributions and refractive indices, n , are the main reason why c_p -TSM, c_p -POC etc relationships vary

See reviews: Morel and Bricaud 1986 and Morel 1991

How is c_p (or b_p or b_{bp}) linked to particles?

$$c_p = \pi \int_{r_{\min}}^{r_{\max}} Q_c(r, n) F(r) r^2 dr$$

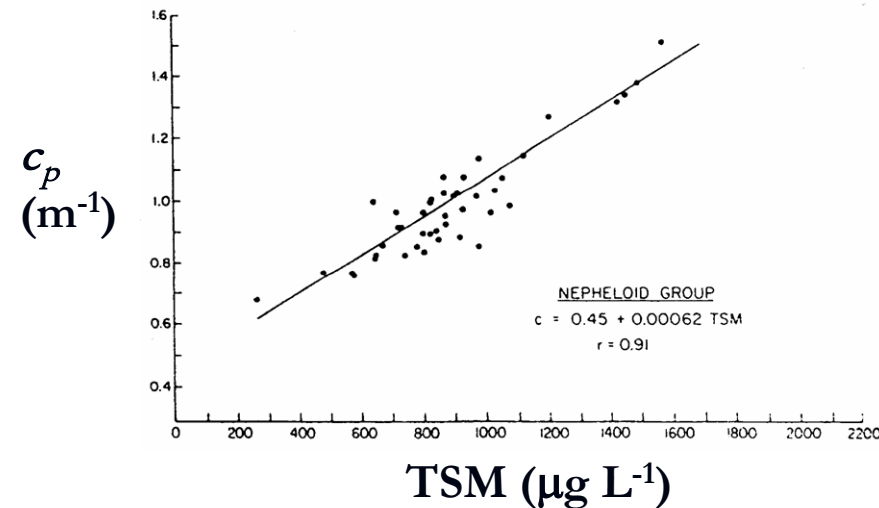
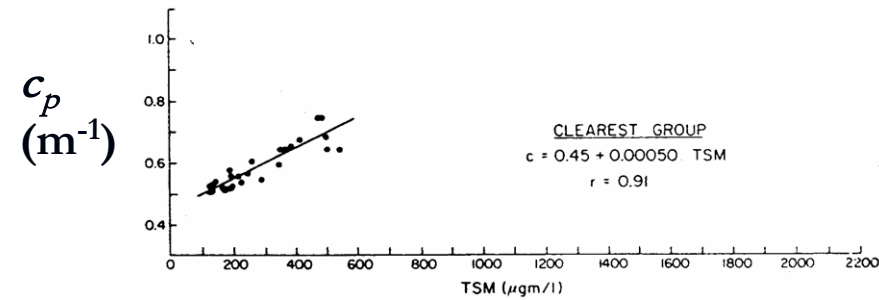
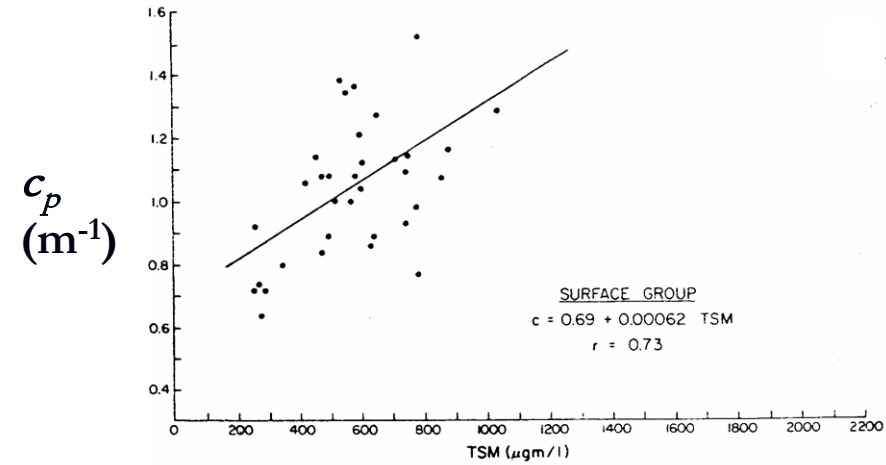


Can be modeled well for spheres with van de Hulst approximation

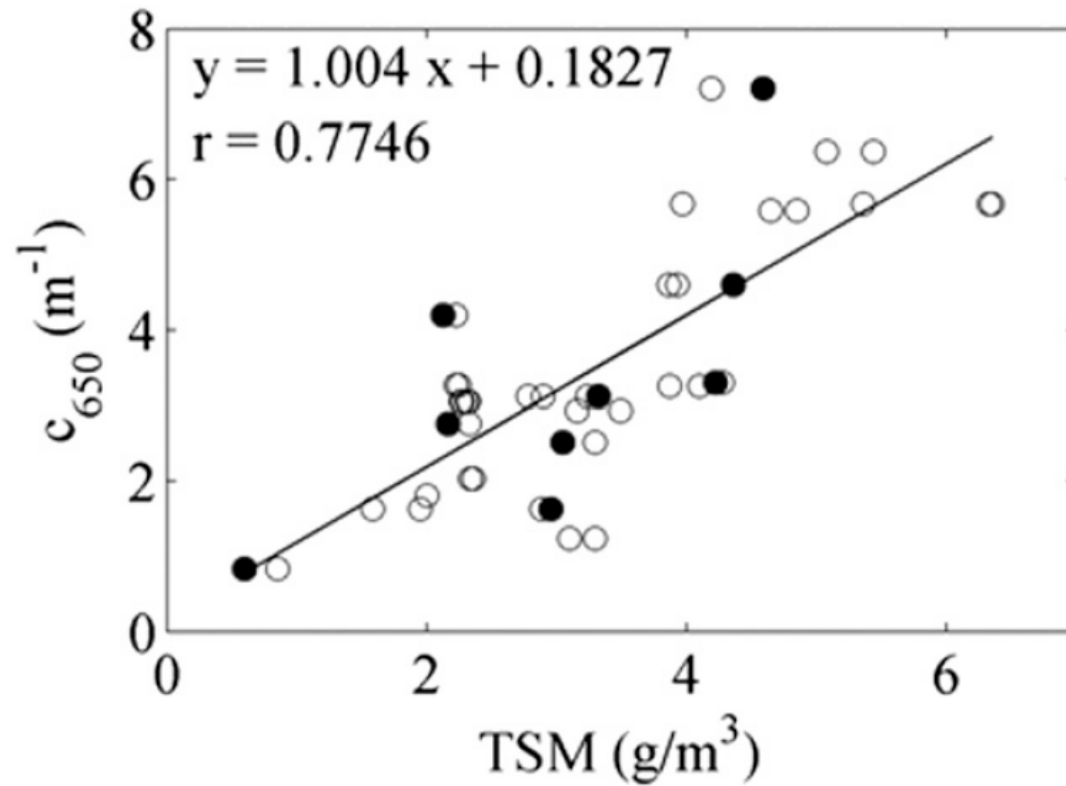
$$c_p \propto \begin{cases} \sum_{i=1}^N d_i^3, & \rho < 4 \xrightarrow{\infty} \text{total particle volume (TPV)} \\ \sum_{i=1}^N d_i^2, & \rho > 4 \xrightarrow{\infty} \text{total surface area (TSA) OR total cross-sectional area (\Sigma G)} \end{cases}$$

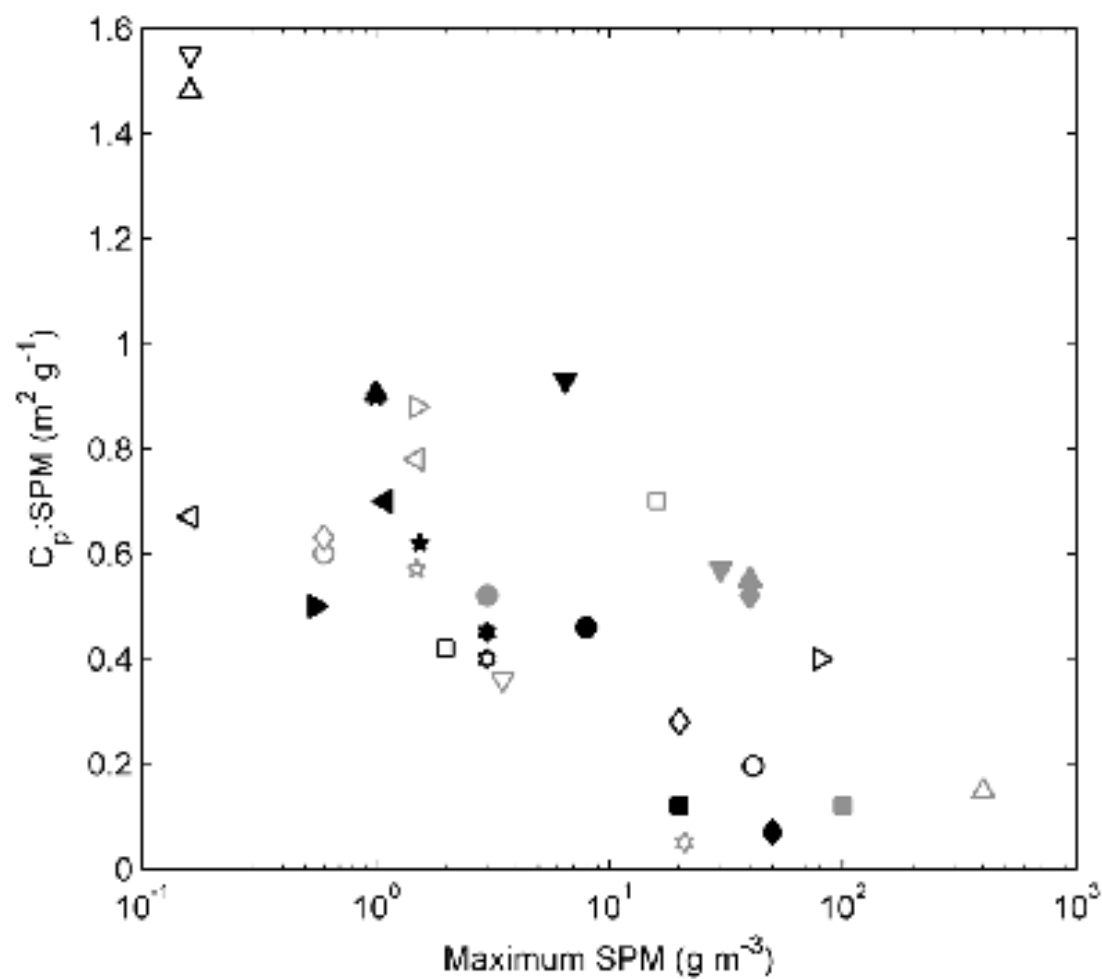
Example: c_p and TSM

Reasonable correlations
for each regression, but
slopes are different for
different water masses



c_p and TSM: Long Island Sound





- This Study
- Baker and Lavelle, 1984
- ◇ Baker and Lavelle, 1984
- ▽ Bishop, 1999
- △ Bishop, 1999
- ◁ Bishop, 1999
- ▷ Boss et al., 2009b
- ☆ Gardner et al., 2001
- ⊛ Gardner et al., 2001
- Gardner et al., 2001
- Guillen et al., 2000
- ◇ Hall et al., 2000
- ▽ Harris and O'Brien, 1998
- △ Holdaway et al., 1999
- ◁ Inthorn et al., 2006
- ▷ Inthorn et al., 2006
- ☆ Inthorn et al., 2006
- ⊛ Jago and Bull, 2000
- Jago and Bull, 2000
- Jago and Bull, 2000
- ◆ Jago and Bull, 2000
- ▼ Karageorgis et al., 2008
- ▲ McCave 1983
- ◄ Peterson, 1977
- Peterson, 1977
- ☆ Peterson, 1977
- Pierson and Weyhenmeyer, 1994
- Puig et al., 2000
- Sherwood et al., 1994
- ◆ Wells and Kim, 1991
- ▼ Wells and Kim, 1991
- ▲ Wells and Kim, 1991

Published slopes for TSM- c_p and POC- c_p

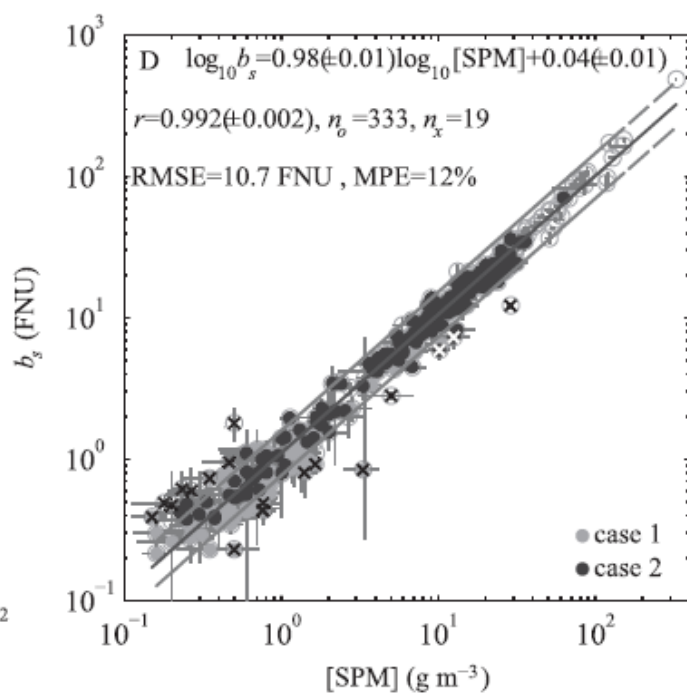
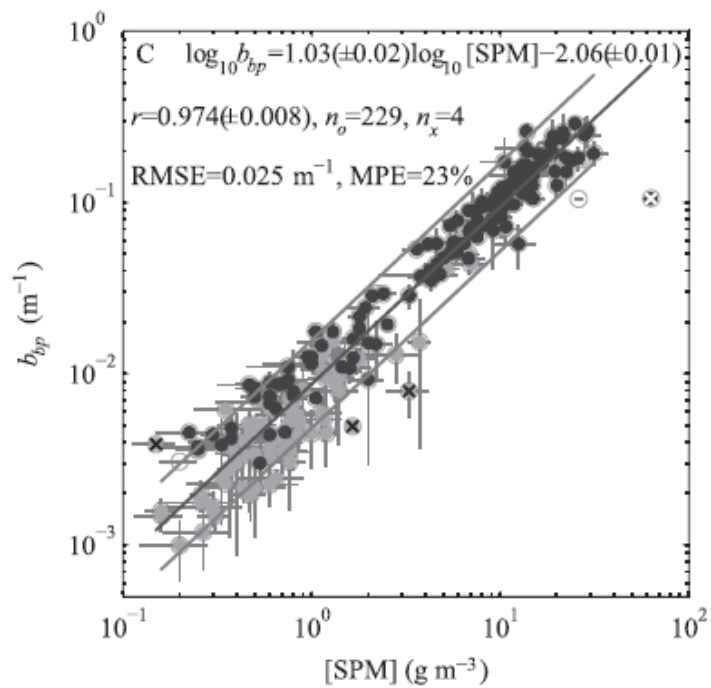
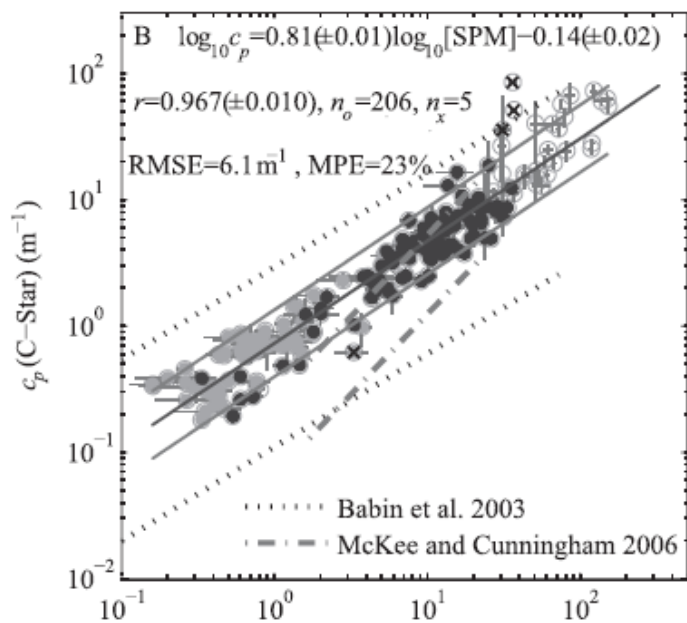
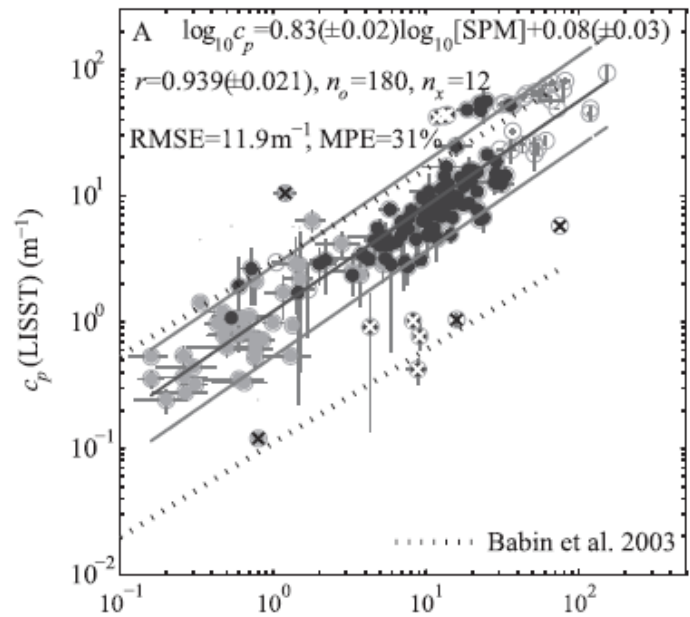
Table 1. Published biogeochemical-optical data.

reference	location	$\frac{\text{TSM}}{c_p^a}$ ($\mu\text{g-m/L}$)	$\frac{\text{POC}}{c_p^a}$ ($\mu\text{g-m/L}$)
Peterson (1977)	OR coast - nepheloid layer	1600	
	OR coast - clearest waters	2000	
	OR coast - surface	1600	
Mishonov et al. (2000)	Ross Sea		674
	NABE		319
	APFZ		455
Bishop et al. (1999)	N. Pacific		195
Gardner et al. (1992)	N. Atlantic	1020	378
	NW Atlantic - pre-hurricane 1996, surface	1000	400
Gardner et al. (2001)	NW Atlantic - pre-hurricane 1996, subsurface	1100	105
	NW Atlantic - post-hurricane 1996, surface	770	455
	NW Atlantic - post-hurricane 1996, subsurface	2500	135
	NW Atlantic - Spring 1997, surface	770	
	NW Atlantic - Spring 1997, subsurface	1700	
	NW Atlantic - Spring 1997, mid-water		1250
Walsh et al. (1995)	Eq. Pac April, 1992	451	
	Eq. Pac October, 1992	642	
Walsh (1990)	Gulf of Mexico	660	
Mishonov et al. (2003)	BATS		323
	NABE (revised from Mishonov et al. 2000)		303

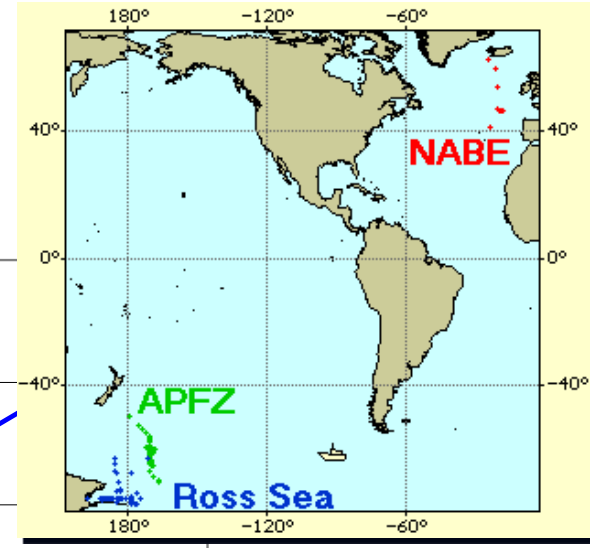
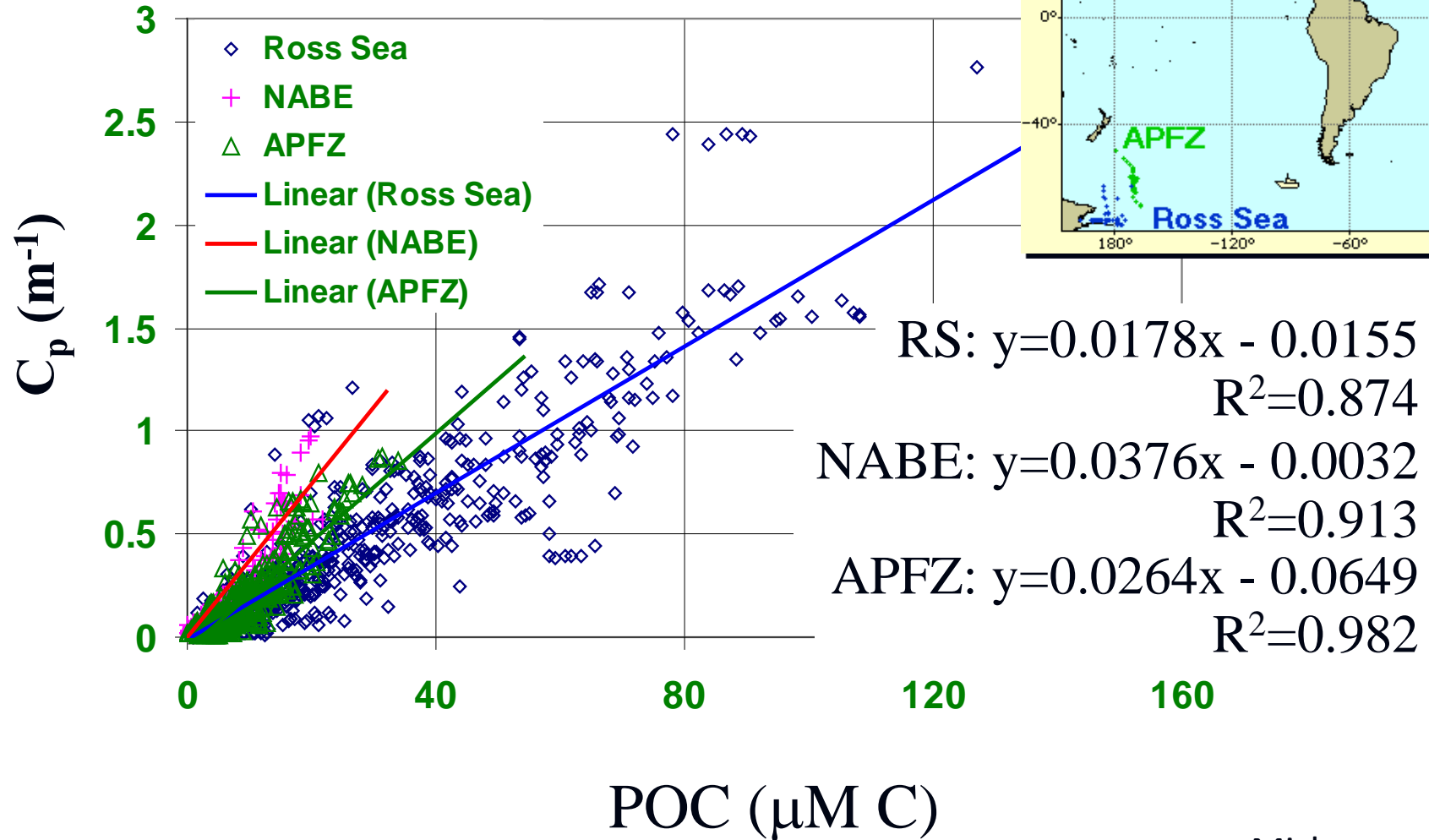
^a – wavelength typically 660 nm

TSM/ c_p range:
~450-2500

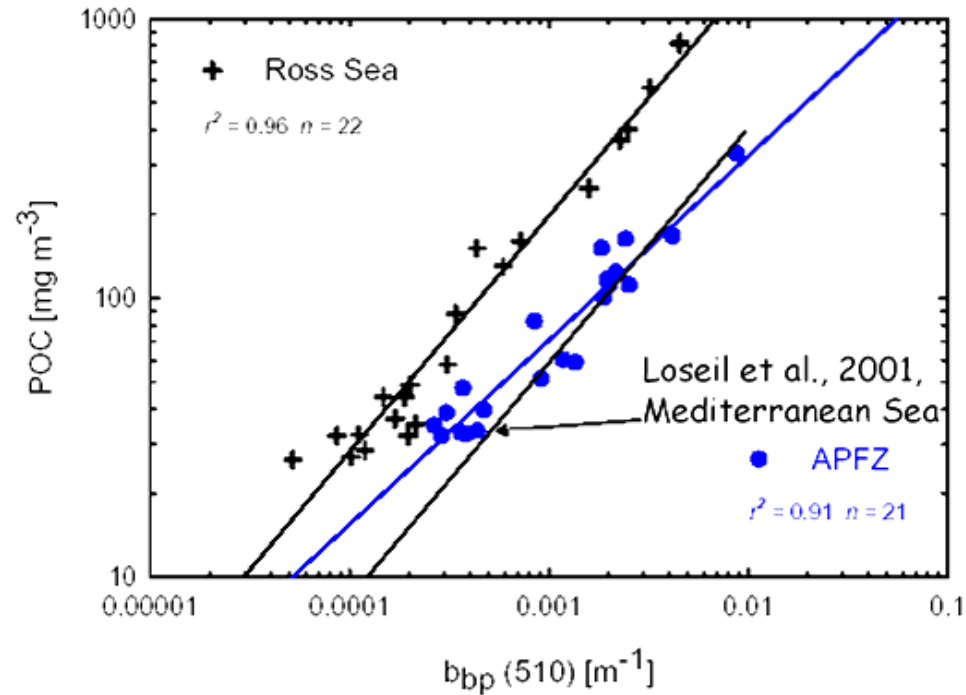
POC/ c_p range:
~100-1250



C_p and POC: Mishonov and Gardner



Obtaining POC from $b_{bp}(510)$:



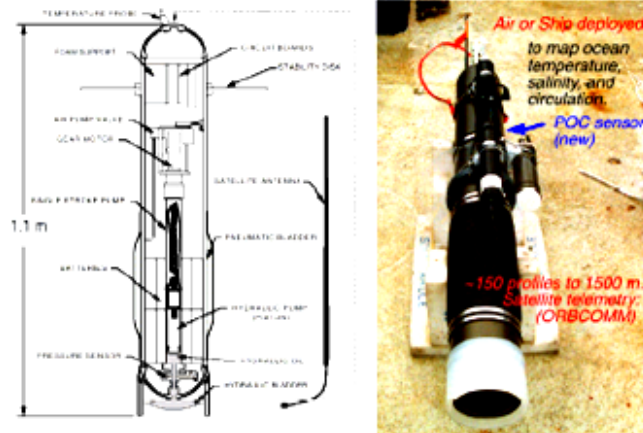
Stramski et al, 1999.

Likely causes for variability: b_{bp} computation, PSD, composition, Particles not accounted by POC method.

Obtaining POC from Beam-c (660):

SOLO float-
Carbon explorers:

NEW OBSERVING SYSTEMS Sounding Oceanographic Lagrangian Observer (SOLO)



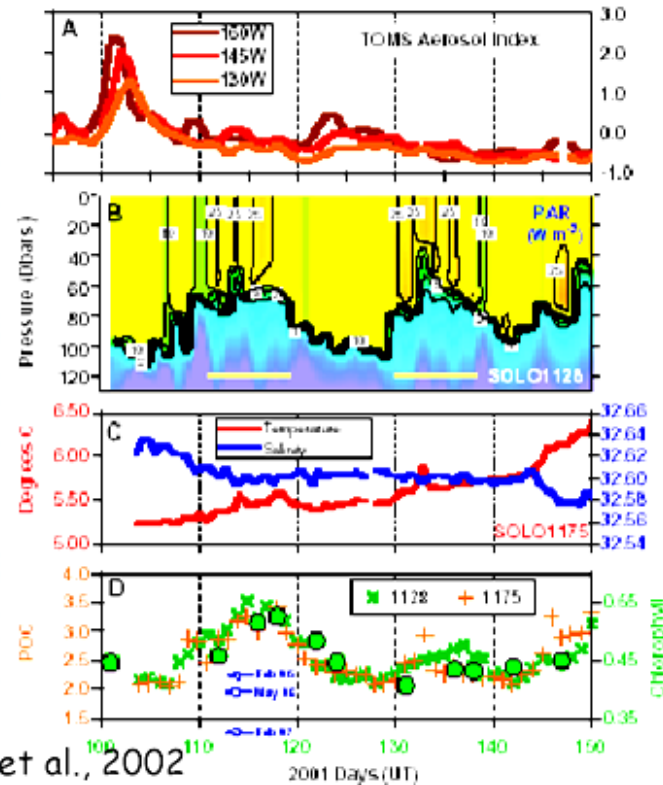
(Davis et al., 1999)

Results:

Two blooms of phytoplankton in North Pacific following dust deposition event (iron fertilization?).

SeaWIFS [chl] and POC covary.

Notice co-variation of blooms and stratification and high chl/C ratios (vernal bloom?).



Bishop et al., 2002

Particle size distribution (PSD) slope and spectral attenuation

With a PSD modeled well by a power law (i.e., a “Junge” type PSD), a correlation is expected between the power law slope of $c_p(\lambda)$, γ , and the power law slope of the PSD, s :

$$s = 3 + \gamma$$

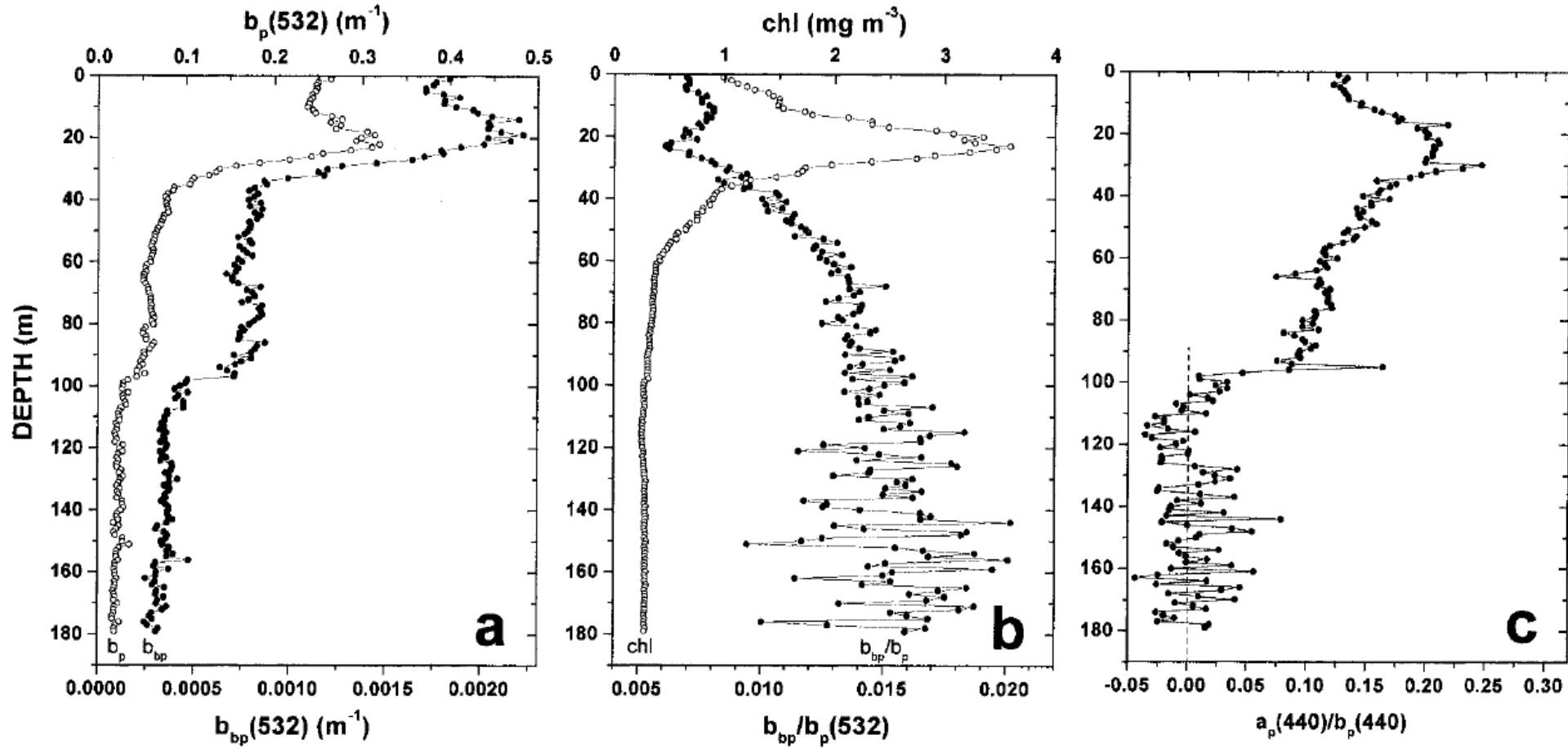
(Volz 1954, Morel 1973)

Or, more accurately when exact particle size limits are considered:

$$s = 3 + \gamma - 0.5\exp(-6\gamma)$$

(Boss et al. 2001)

Bulk particle refractive index model



Field data from
Gulf of California

Bulk particle refractive index model

$$\hat{n}_p(\tilde{b}_{bp}, \gamma) = 1 + \tilde{b}_{bp}^{0.5377+0.4867(\gamma)^2} [1.4676 + 2.2950(\gamma)^2 + 2.3113(\gamma)^4].$$

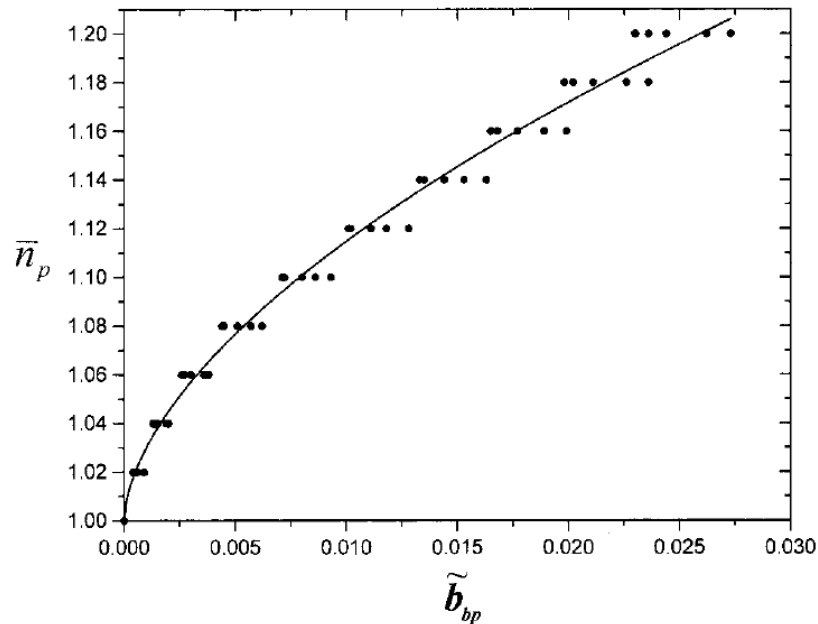
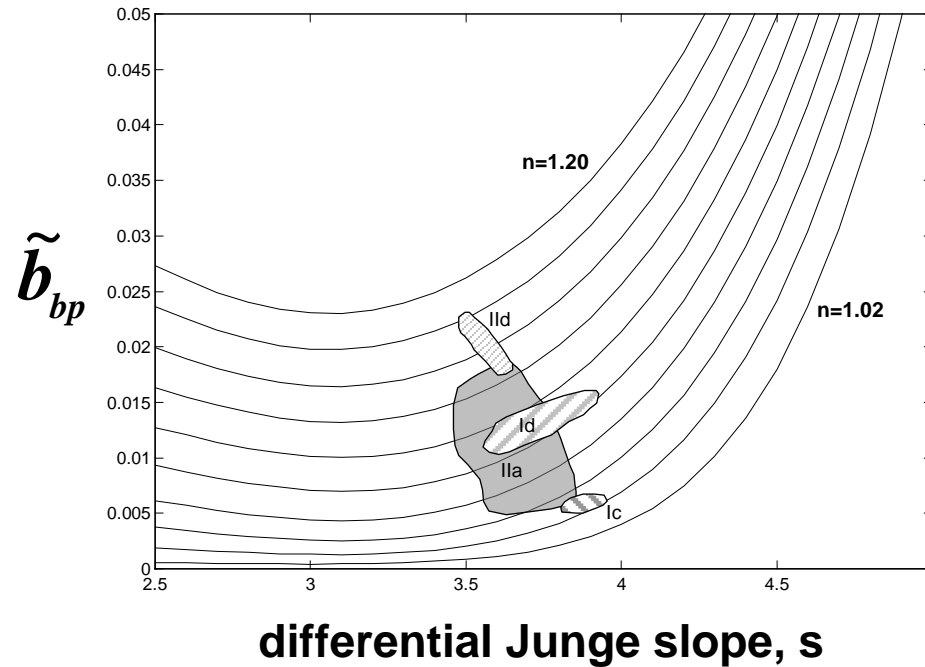


Figure 10. The relationship between bulk refractive index \bar{n}_p and \tilde{b}_{bp} for hyperbolic slopes ranging between 2.5 (0.25) 3.5 (data from Figure 1a replotted and fitted). For these ranges of ξ , \bar{n}_p was a strong function of \tilde{b}_{bp} (regression given in text, equation (14)).

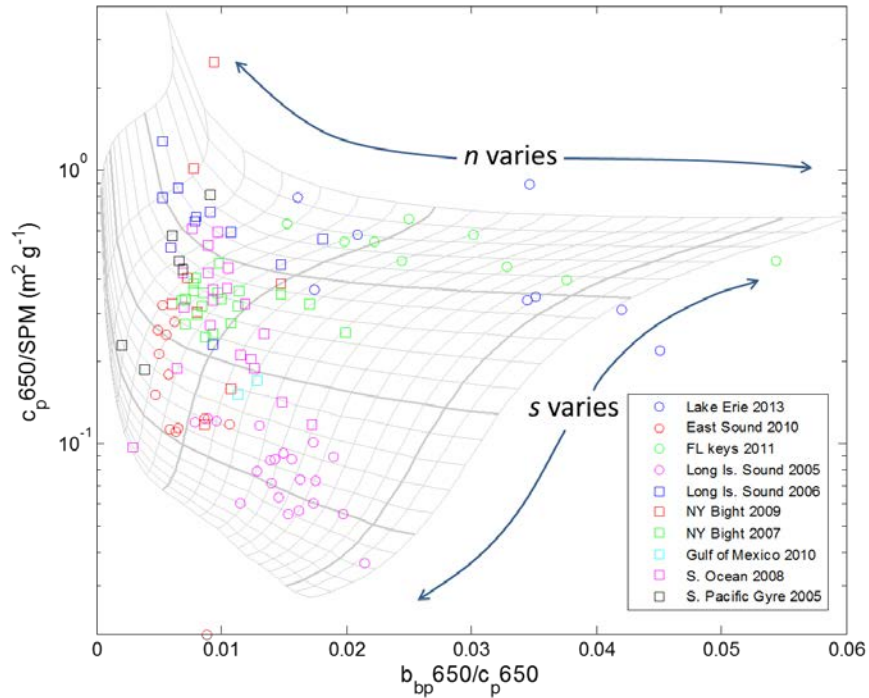


Field data from
Gulf of California

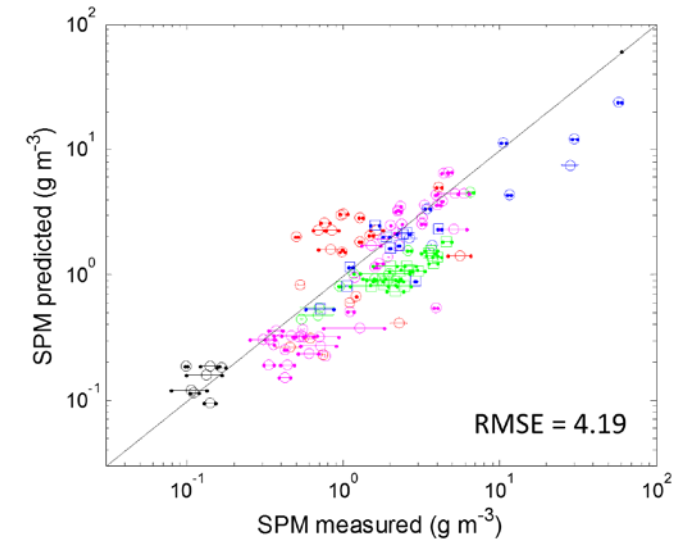
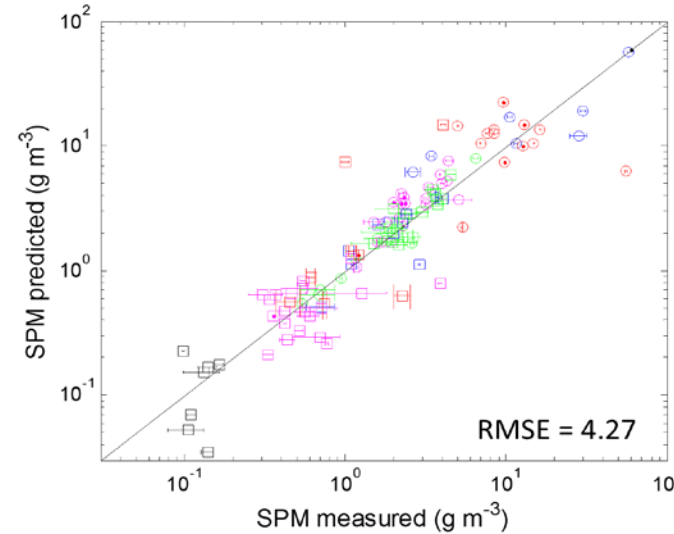
Based on Lorenz-
Mie theory

- Ic** – Case I, chlorophyll maximum
- Id** – Case I, deep water
- Ila** – Case II, south of midrift islands
- Ild** – Case II, bottom water, north of midrift islands

Can we use n and PSD models to improve SPM estimation?



Field data (122 sample sites from 10 different global locations) overlying analytical model results.

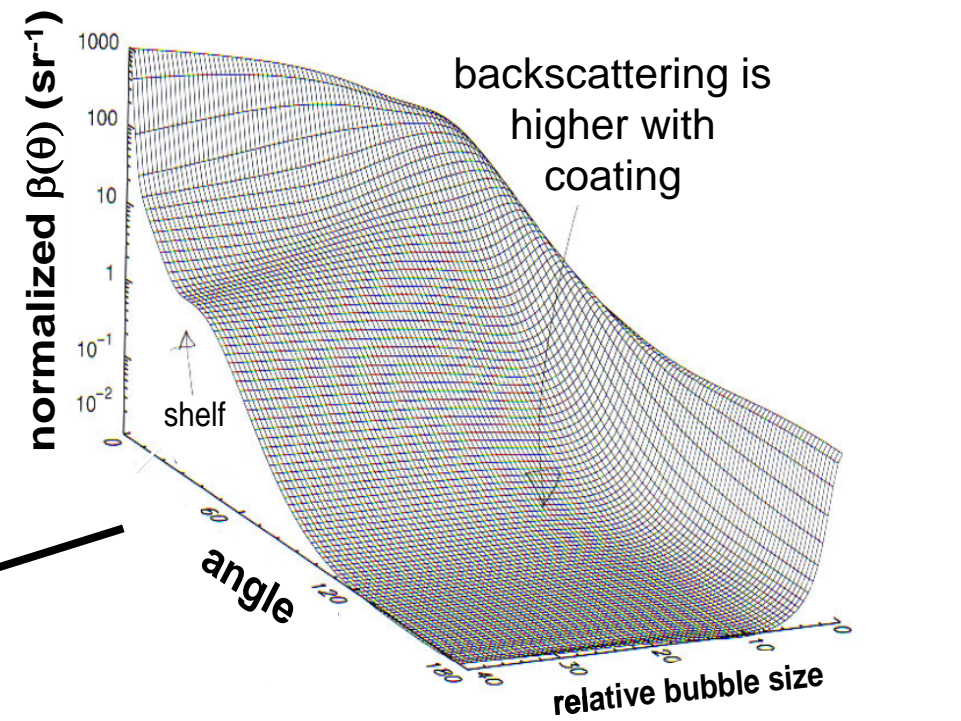
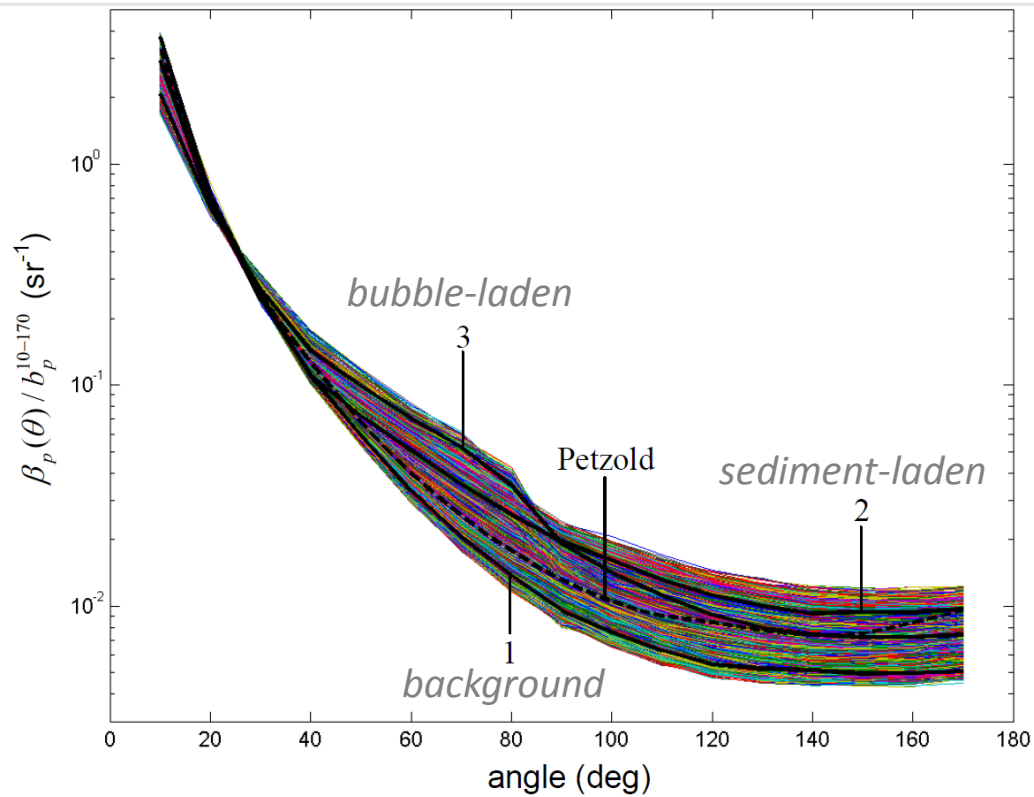


- 1) derive PSD slope s from the c_p slope (Boss et al. 2001),
- 2) use measured b_{bp}/c_p and derived s to solve for c_p/SPM with the model,
- 3) divide measured c_p by the derived $c_p/SPM = SPM$.

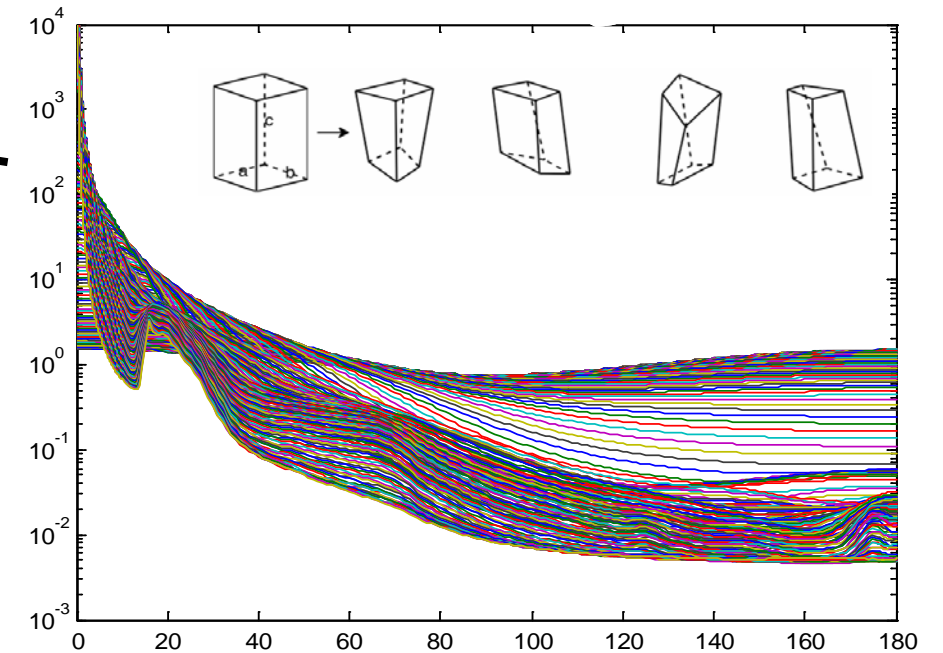
empirical state-of-the-art: SPM predicted from a Type II linear regression between measured SPM and c_p , plotted versus measured SPM, i.e., if one had *a priori* knowledge of the best linear fit

VSF inversion

Scripps Pier, 2008



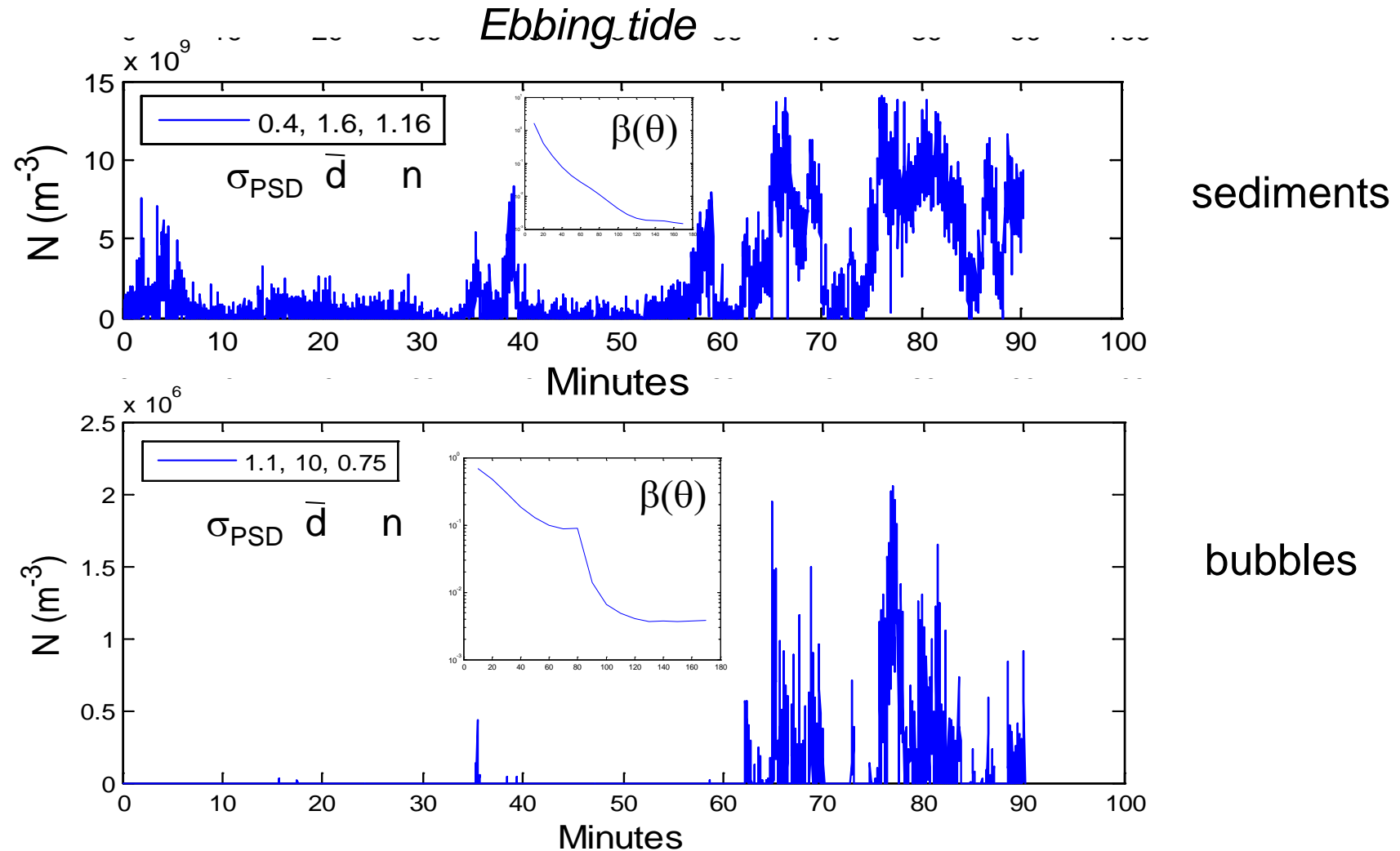
Fit to
measured
VSFs



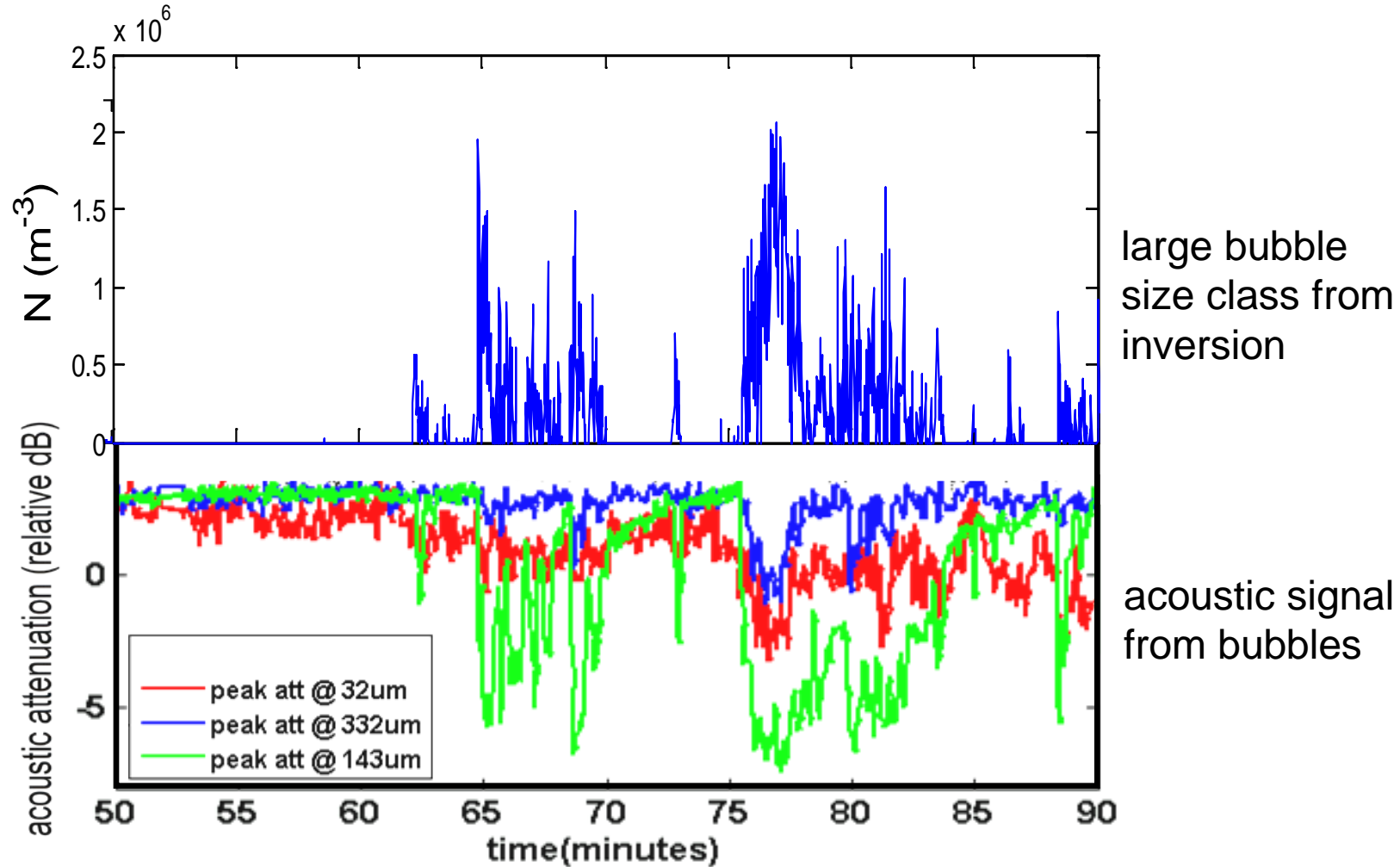


Scripps Pier

VSF inversion: large bubble subpopulation

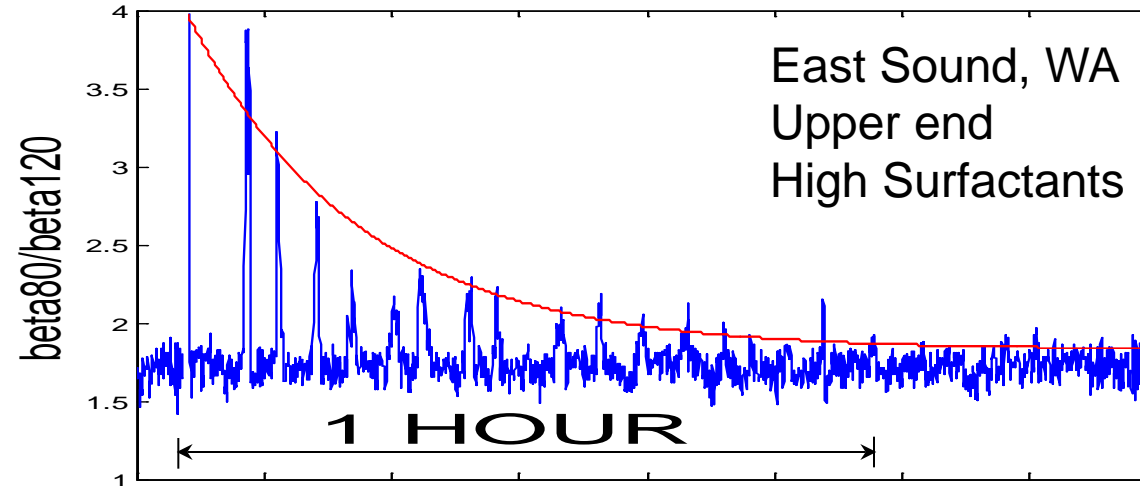


Bubbles resolved with optics and acoustics

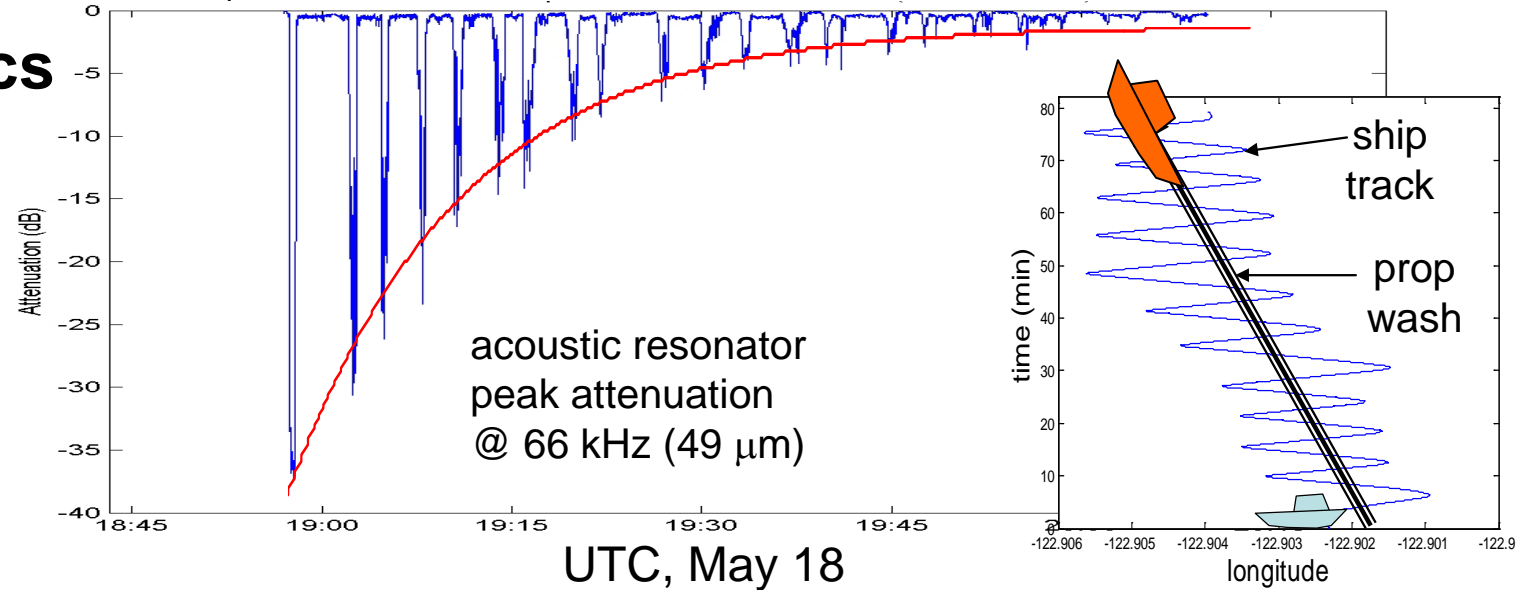


Surfactants are important for bubbles

Optics



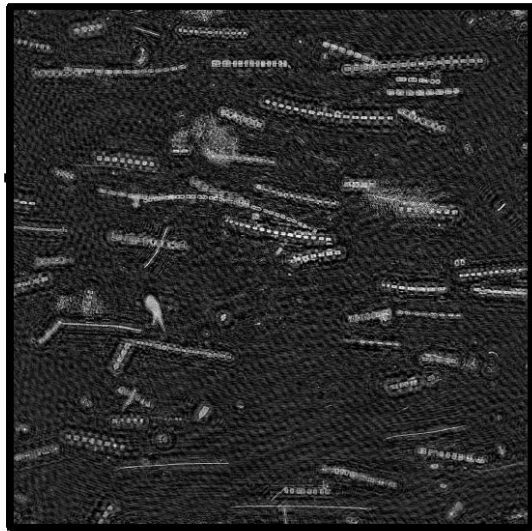
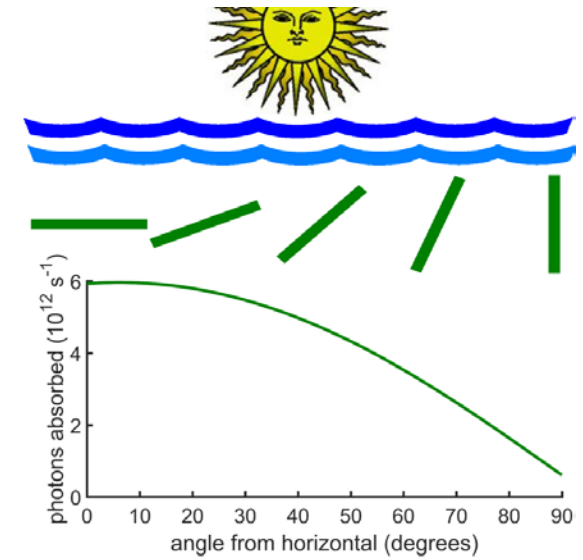
Acoustics



Particle orientation

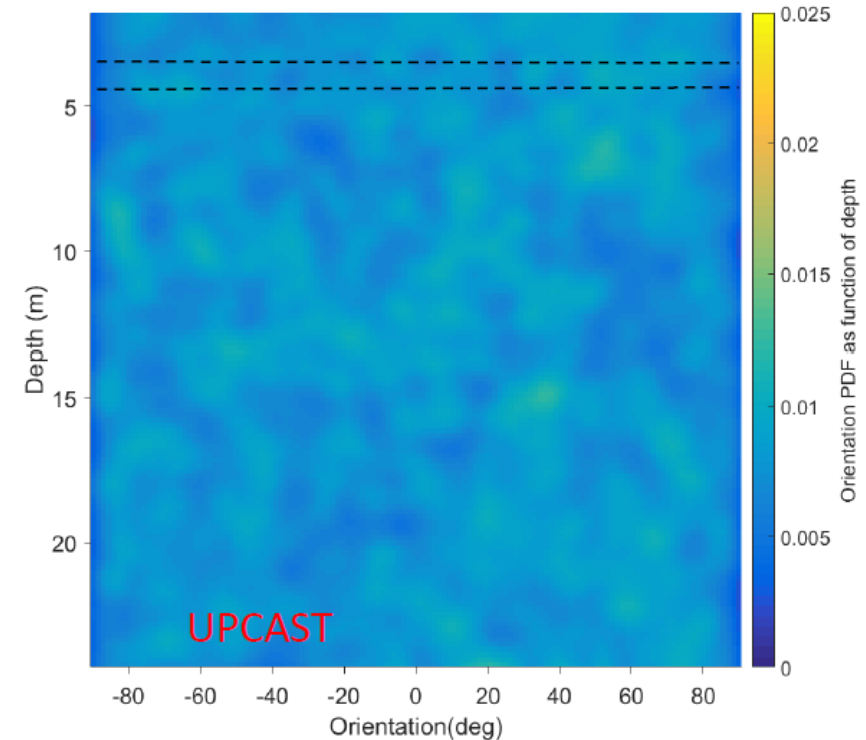
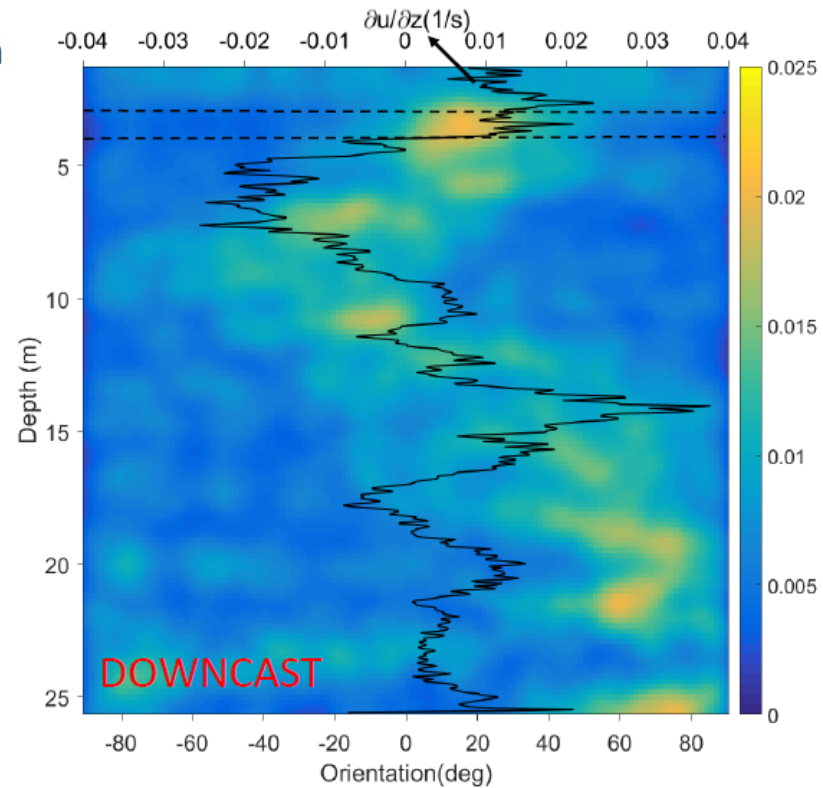


In situ holographic microscope



9.4 mm

Image from ~ 3.5 m depth showing horizontal orientation of diatom colonies (mostly *Ditylum brightwellii*) within a thin layer.

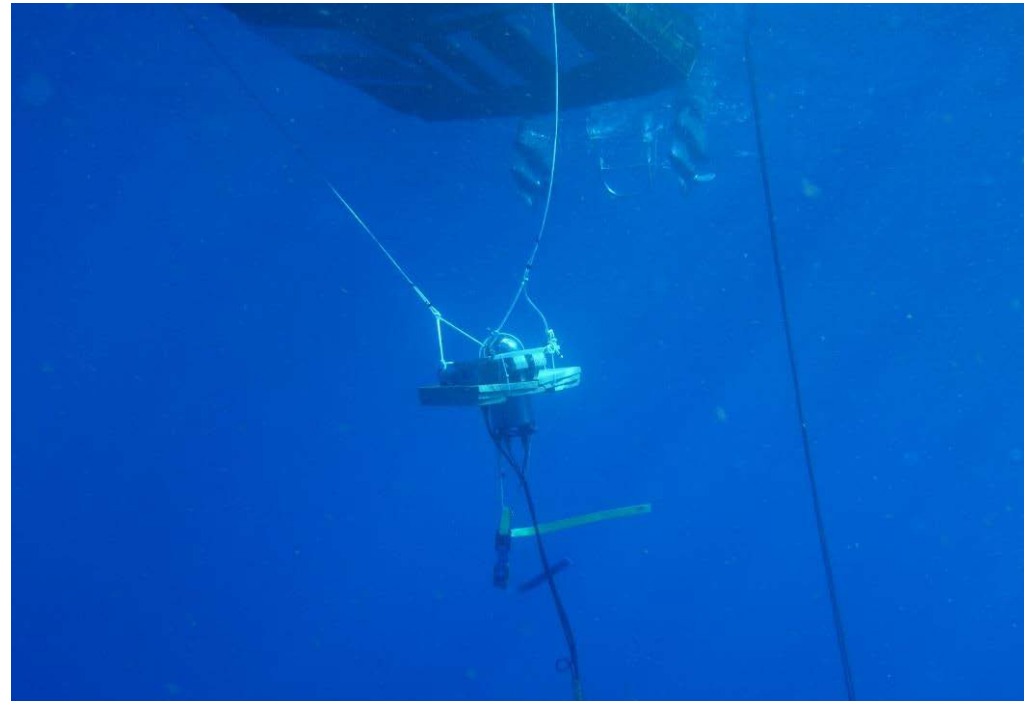
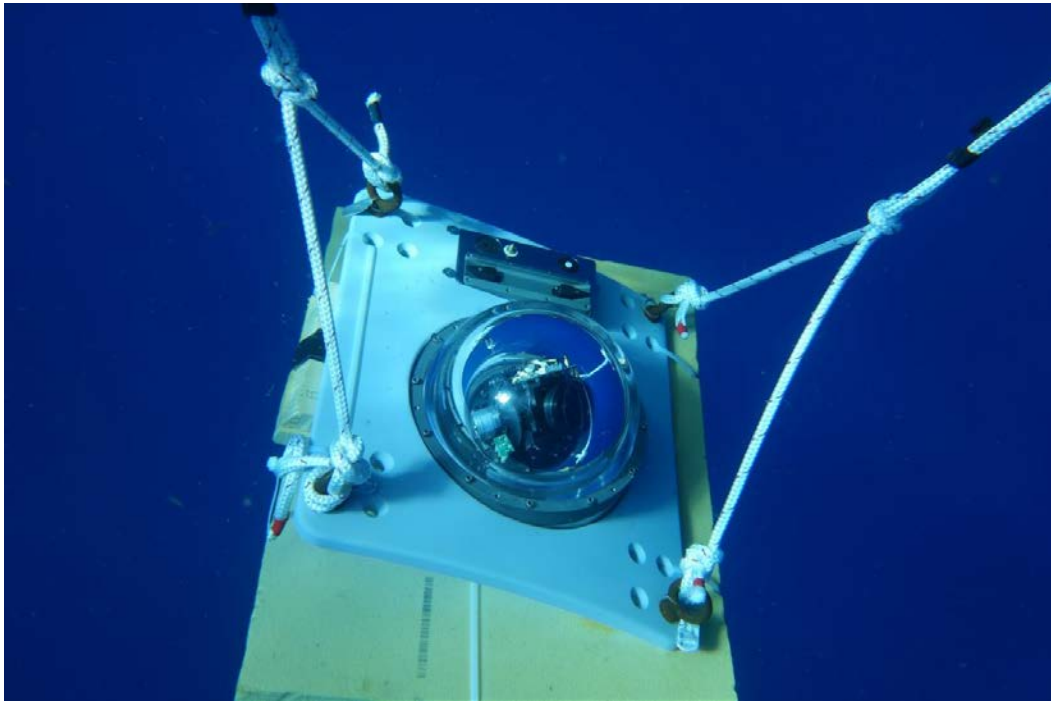


Nayak et al. (2017)

McFarland et al., in prep

Imaging

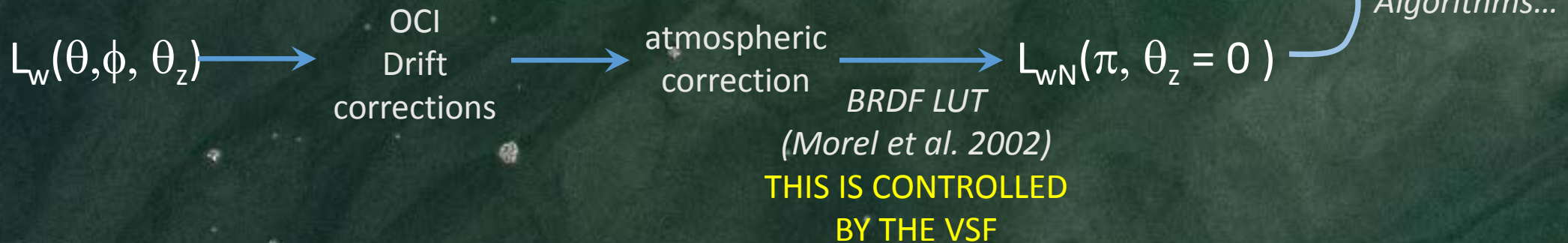
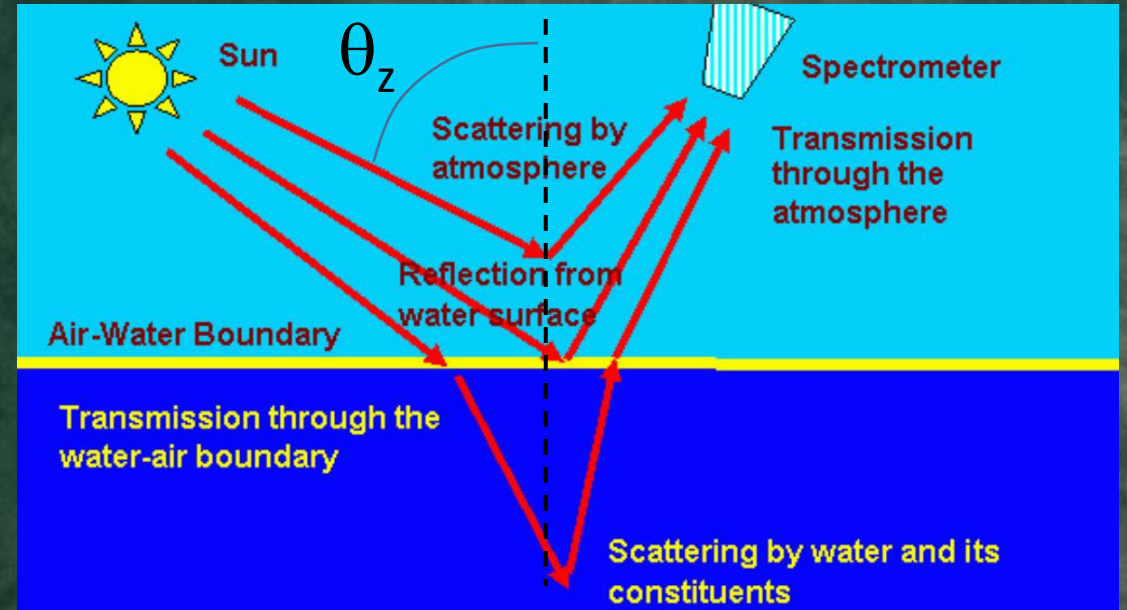
$$\text{upward looking range} = Z_i = \frac{1}{c - K} \left[-\ln \left(\frac{C_L}{2M_0} \right) + \frac{bd}{4\pi\theta_0} \right]$$



Relevance of VSF to ocean color

$$R_{rs}(0^-) = \frac{L_u(0^-)}{E_d(0^-)} \cong \Psi \left(\frac{b_b}{a + b_b} \right)$$

Gordon (1975)
Morel and Prieur (1975)



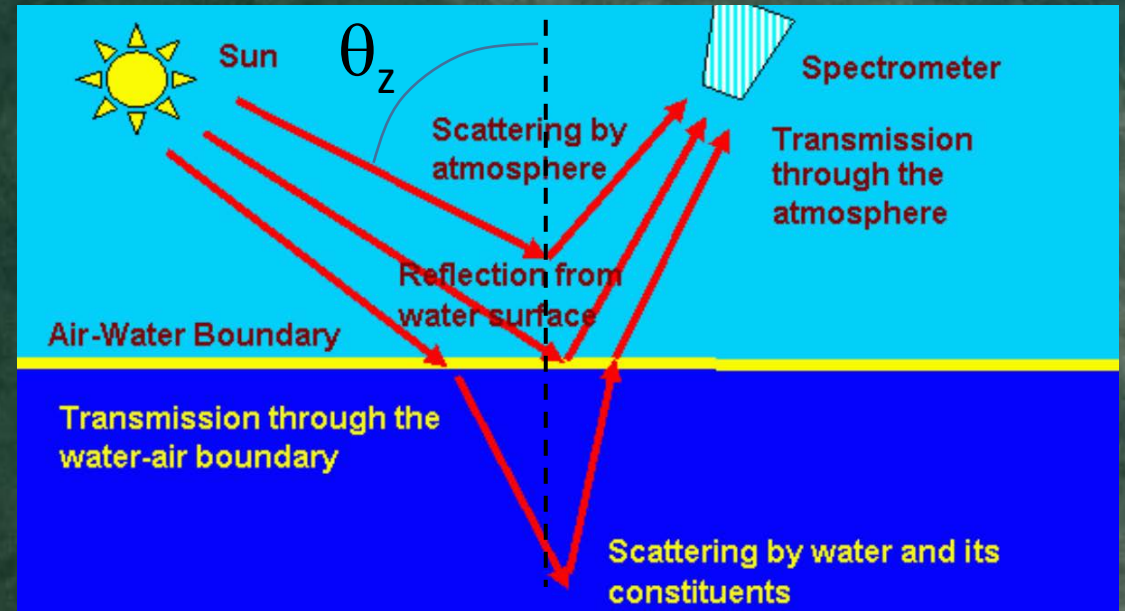
Explicit inclusion of the VSF in SA algorithms

$$\frac{L_u}{E_{od}} = \frac{\beta(\pi - \theta_z)}{a(1 + \bar{\mu}_\infty^{-1}) + b_b - 0.05b_f}$$

Zaneveld (1995)

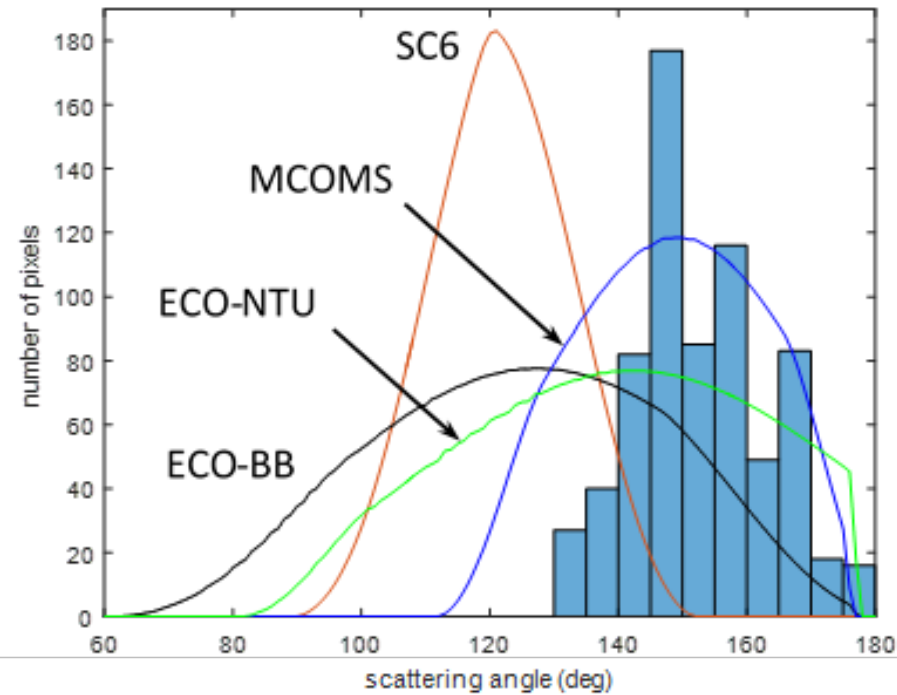
$$\frac{L_u}{E_d} = \sec(\theta_z) \frac{\beta(\pi - \theta_z)}{c} \frac{\sec(\pi)}{\sec(\pi) - \sec(\theta_z)} e^{-cz \sec(\theta_z)}$$

Jerlov (1976)



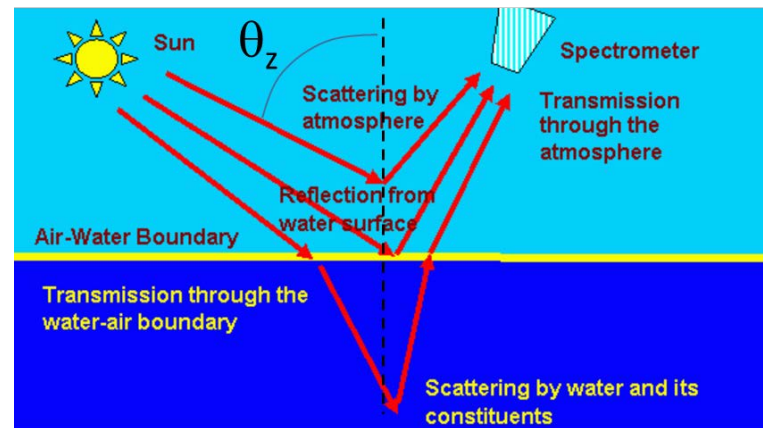
- Could directly apply VSF information from a PACE polarimeter
- Without polarimeter, could apply representative phase function basis vectors (similar to SA basis vector models summarized in Werdell et al)

Scattering angle distributions from space

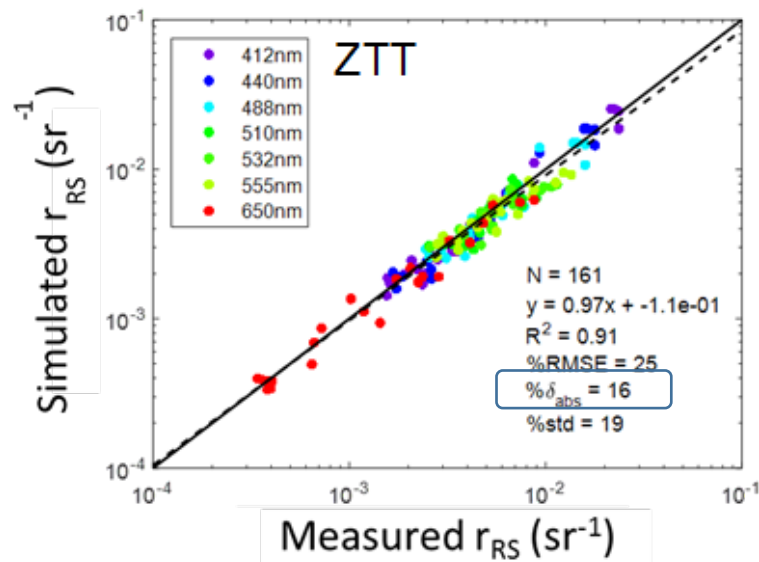


In-water single scattering angles from future PACE imager through an orbit

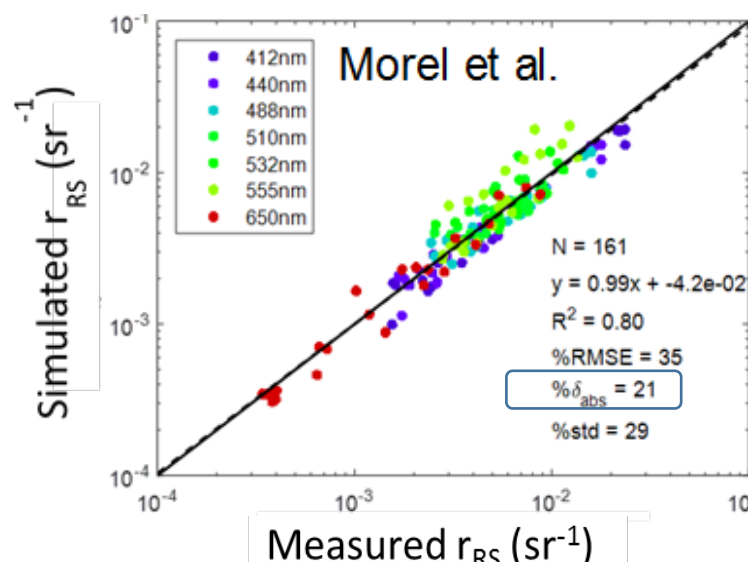
Analytical algorithm using VSF (ZTT)



$$r_{RS}(\theta_s, \theta_v, \phi, V, a, b_b) \cong r_{RS,Raman}(\theta_s', a, b_b) + \frac{1}{\bar{\mu}_d(\theta_s', V, \frac{b_b}{a}, \eta_{bb})} \left[\frac{\beta(\gamma)}{b_b} \left(\frac{a}{b_b} \left(1 - \cos(\theta_v) \Psi_{KLu}(\theta_s') / \bar{\mu}_\infty \left(\frac{b_b}{a}, \eta_{bb} \right) \right) + f_L(\theta_s, \theta_v, \phi) + (1 - f_L(\theta_s, \theta_v, \phi)) \tilde{b}_b^{-1} \right) \right]^{-1}$$



constant β/b_b shape is assumed...



State-of-the-art LUT

Twardowski and Tonizzo (in review)

SO MUCH TO DO...!

- Pure water: depolarization ratio (0.039, 0.051, 0.09?)
- Pure seawater: effect of salts (only have Morel 1968 experiment)
- Spectral scattering:
 - hyperspectral bb
 - phase function shape
 - anomalous dispersion
- $\beta(180)$
- Scattering by nonspherical, complex particle populations
- Effect of scattering by nonrandomly oriented particles
- Anything to do with polarized scattering
- Ocean color algorithms from space that explicitly include VSF
-?