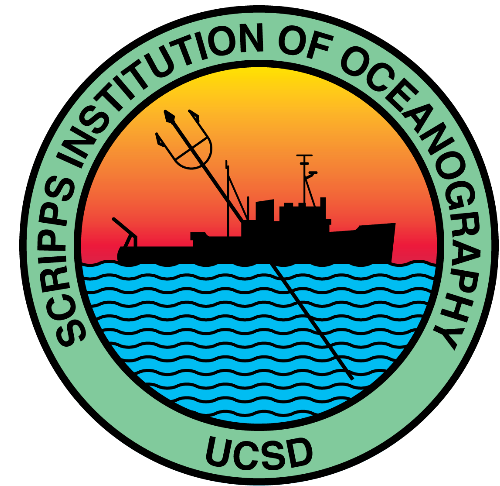


# The Nature of Light

## Interaction of Light and Matter

Dariusz Stramski

Scripps Institution of Oceanography  
University of California San Diego  
Email: [dstramski@ucsd.edu](mailto:dstramski@ucsd.edu)

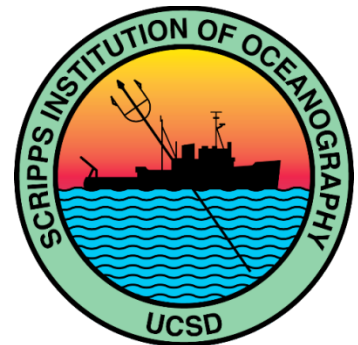


IOCCG Summer Lecture Series  
25 June - 7 July 2018, Villefranche-sur-Mer, France

- 1978. MS in Oceanography, University of Gdansk, Poland
- 1978 - 1986. Research Scientist, Institute of Oceanology, Polish Academy of Sciences, Sopot, Poland
- 1985. PhD in Earth Sciences, University of Gdansk, Poland
- 1986 -1988. Postdoctoral Fellow, Villefranche-sur-Mer, France
- 1988 -1989. Visiting Scientist, Université Laval, Québec, Canada
- 1989 -1997. Research Professor, University of Southern California, Los Angeles, USA
- 1996. “Poste Rouge” Visiting Scientist, Villefranche-sur-Mer, France
- 1997 – present. Professor, Scripps Institution of Oceanography, University of California San Diego, USA

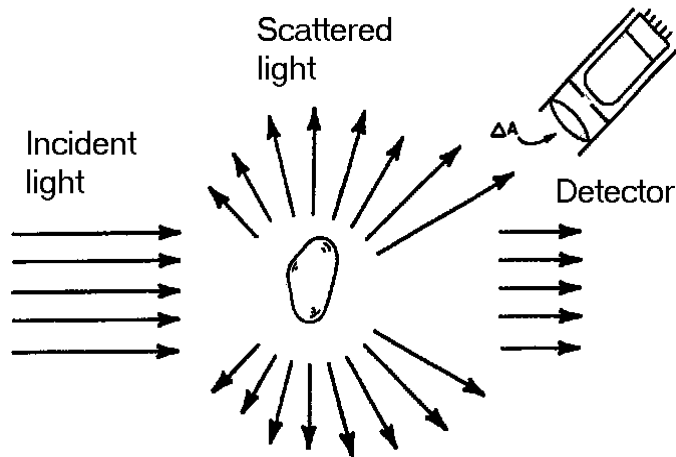


UNIVERSITÉ  
LAVAL

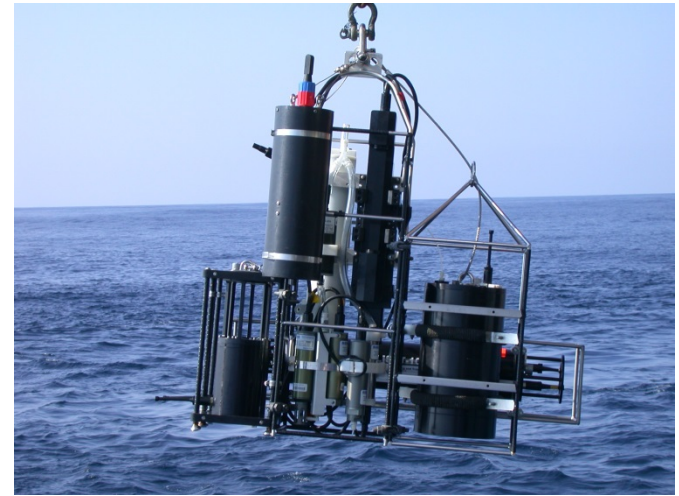


# OCEAN OPTICS RESEARCH LAB AT SIO

## PARTICLE OPTICS



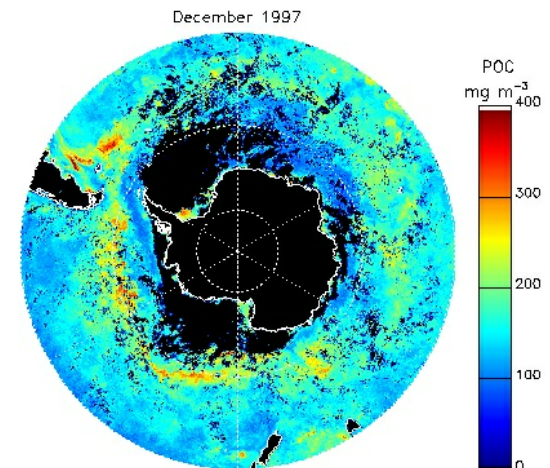
## FIELD OBSERVATIONS



## MODELING

$$\begin{aligned} \cos \theta \frac{dL(z, \xi, \lambda)}{dz} &= -c(z, \lambda)L(z, \xi, \lambda) \\ &+ \int_{\Xi} L(z, \xi', \lambda) \beta(z, \xi' \rightarrow \xi, \lambda) d\Omega(\xi') \\ &+ S(z, \xi, \lambda) \end{aligned}$$

## REMOTE SENSING



**USCGC Healy**



**R/V Nathaniel B. Palmer**



**R/V Kilo Moana**



**CCGS Amundsen**



**R/V L'Atalante**



**R/P FLIP**



**R/V Mirai**

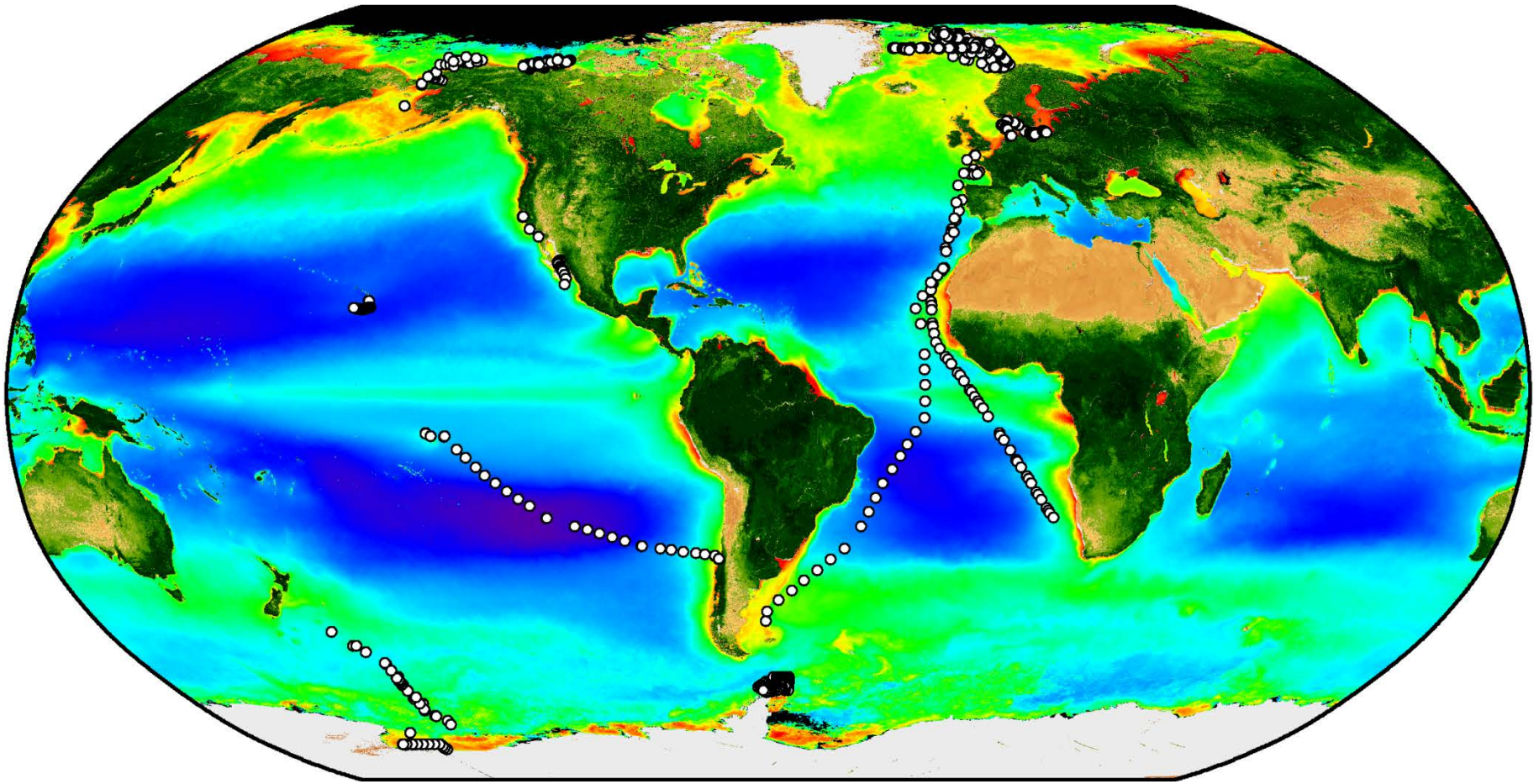


**R/V Oceania**

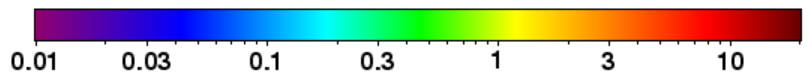


**R/V Polarstern**

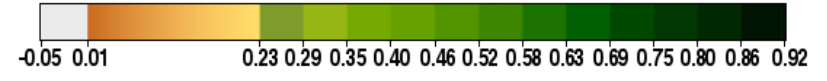




Chlorophyll a concentration ( mg / m<sup>3</sup> )



Normalized Difference Vegetation Index



# What is light?

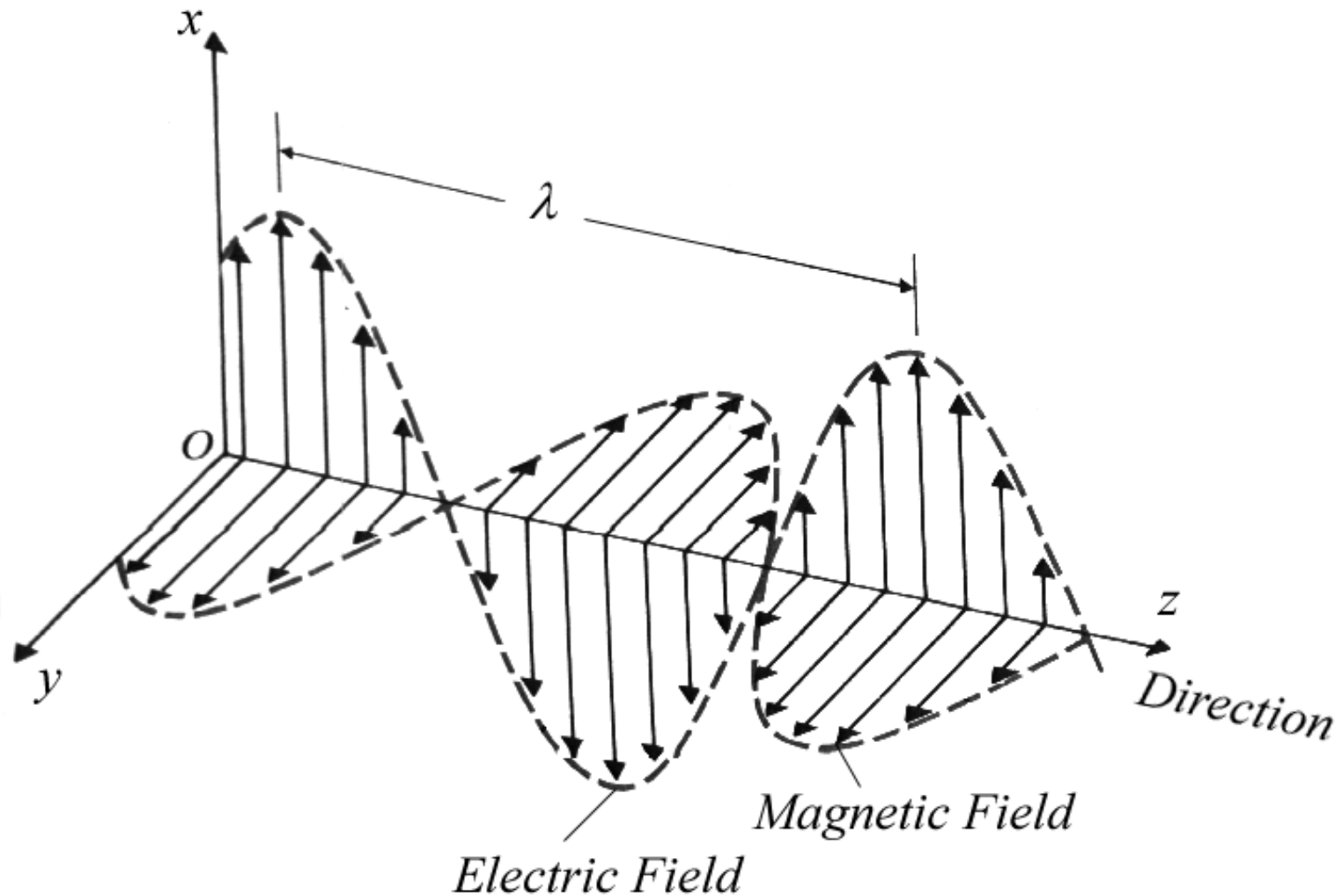
“Every physicist thinks he knows what a photon is. I spent my life to find out what a photon is and I still don't know it”

“Physics should be made as simple as possible, but no simpler”

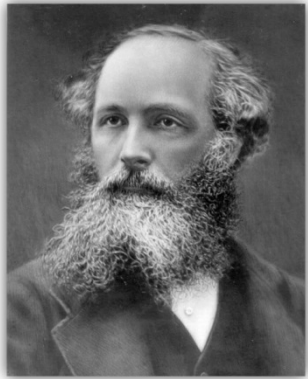
- Albert Einstein

# Electromagnetic wave

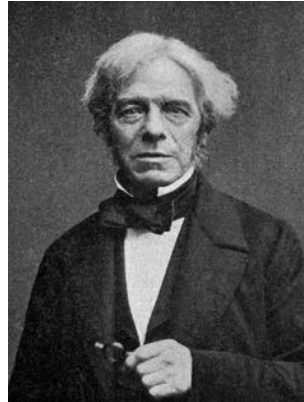
Time-varying electric and magnetic fields are coupled in an electromagnetic field radiating from the source



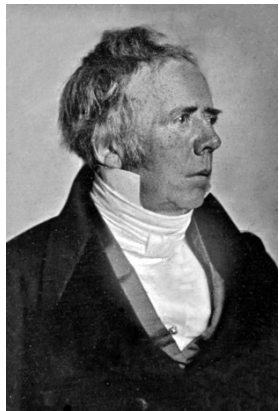
# Maxwell equations: How is an electromagnetic field produced?



James Clerk Maxwell  
(1831 - 1879)



Michael Faraday  
(1791 - 1867)



Hans Christian Ørsted  
(1777 - 1851)



André-Marie Ampère  
(1775 - 1836)

## Electric fields are generated by:

- Electric charges
- Time-varying magnetic fields

## Magnetic fields are generated by:

- Charges in motion (electric currents)
- Time-varying electric fields



## Force equations: How fields affect charges?

- If a point charge experiences a force  $\vec{F}_E$ , the electric field at the position of charge is:  $\vec{F}_E = q \vec{E}$
- A moving charge may experience another force that is proportional to its velocity  $\vec{v}$ :  $\vec{F}_M = q \vec{v} \times \vec{B}$
- If forces  $\vec{F}_E$  and  $\vec{F}_M$  occur concurrently then the charge experiences electric and magnetic fields:  $\vec{F} = q \vec{E} + q \vec{v} \times \vec{B}$

- From Maxwell's equations in differential form we obtain in free space

$$\nabla^2 \vec{E} = \mu_0 \epsilon_0 \frac{\partial^2 \vec{E}}{\partial t^2}$$

$$\nabla^2 \vec{B} = \mu_0 \epsilon_0 \frac{\partial^2 \vec{B}}{\partial t^2}$$

where  $\nabla^2 \equiv \nabla \cdot \nabla$  is the scalar operator known as Laplacian

$$\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$$

- Example of one of six scalar equations

$$\frac{\partial^2 E_x}{\partial x^2} + \frac{\partial^2 E_x}{\partial y^2} + \frac{\partial^2 E_x}{\partial z^2} = \epsilon_0 \mu_0 \frac{\partial^2 E_x}{\partial t^2}$$

- Wave equation if

$$\epsilon_0 \mu_0 = \frac{1}{c^2}$$

# Poynting Vector

Energy transported by electromagnetic wave per unit time per unit area

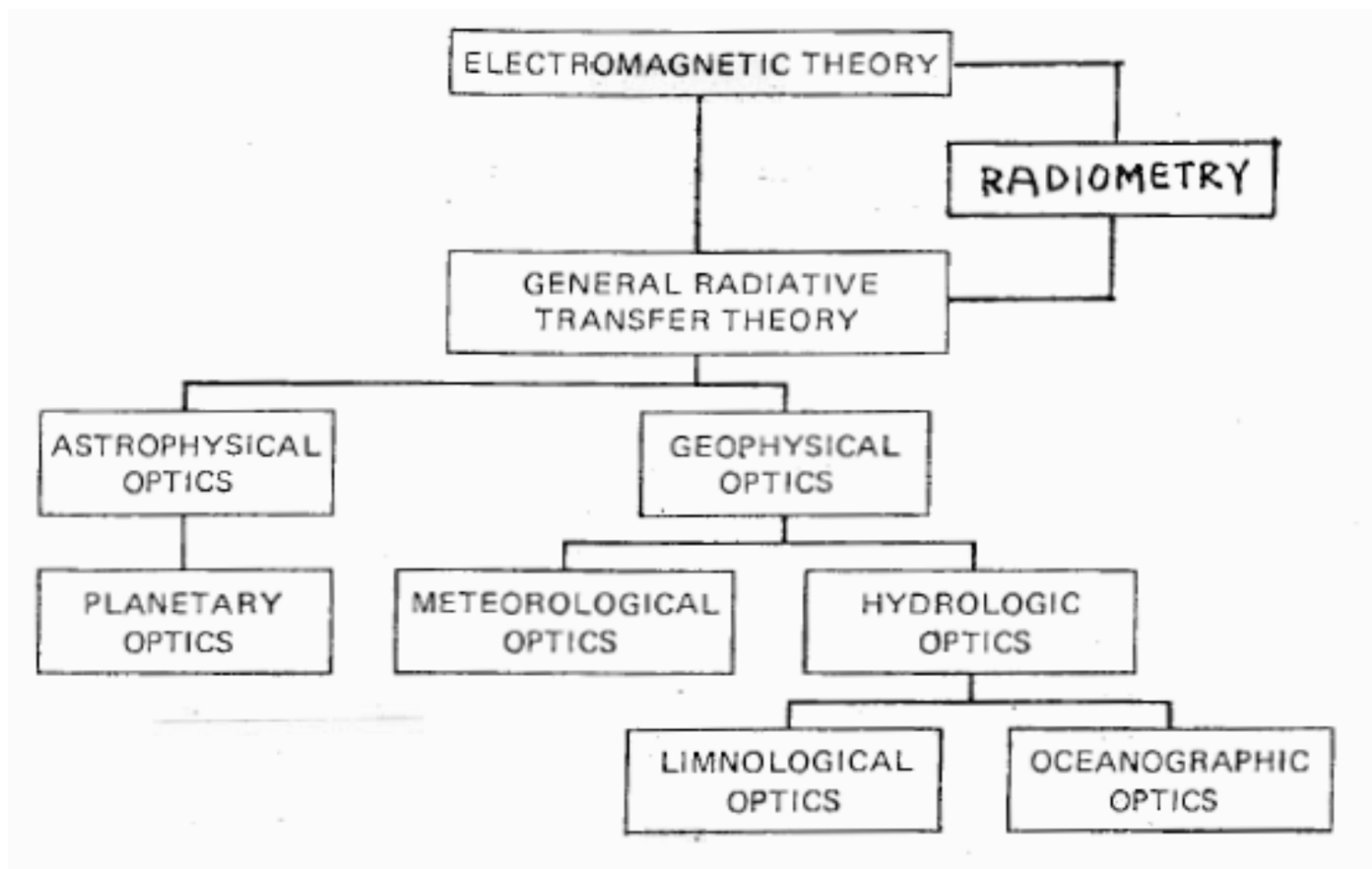
- Poynting vector at time instant  $t$

$$\vec{S}(t) = \frac{1}{\mu_0} \vec{E}(t) \times \vec{B}(t) = c^2 \epsilon_0 \vec{E}(t) \times \vec{B}(t)$$

- Time-average magnitude of  $\vec{S}(t)$  is

$$\langle S \rangle_T = \frac{c^2 \epsilon_0}{2} |\vec{E}_0 \times \vec{B}_0| = \frac{c \epsilon_0}{2} E_0^2$$

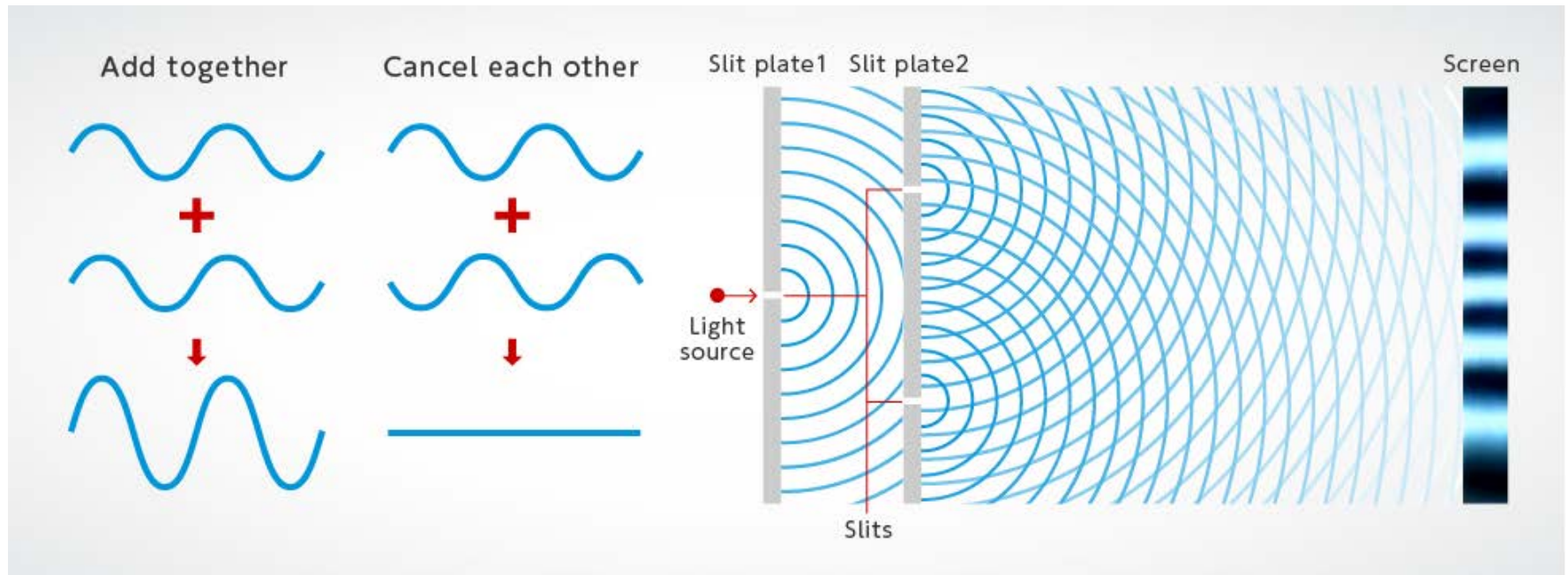
# The relation between ocean optics and fundamental electromagnetic theory in physics

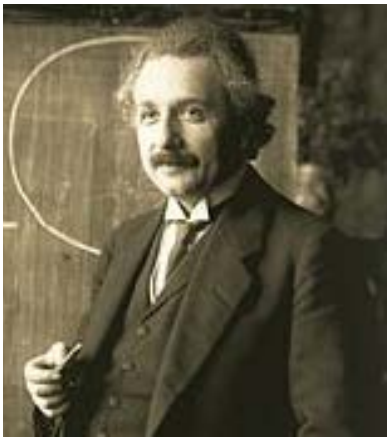




Thomas Young  
(1773 - 1829)

In 1807, an English physicist Thomas Young asserted that light has the properties of a wave in an experiment called Young's Interference Experiment. This Young's interference experiment showed that light beams (waves) passing through two slits (double-slit) add together or cancel each other and then interference fringes appear on the screen. This phenomenon can be explained if light is considered as a wave.



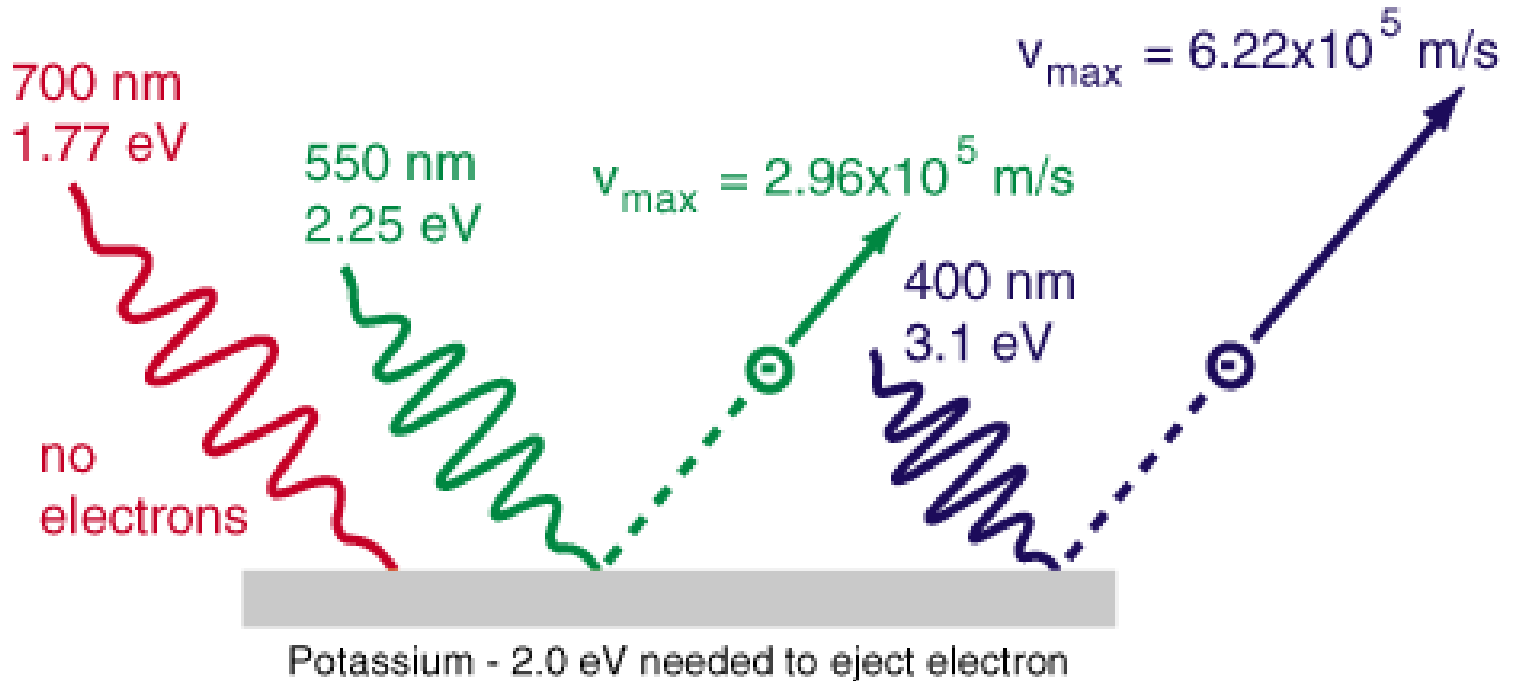


Albert Einstein (1879 - 1955)  
Nobel Prize 1921

On a Heuristic Viewpoint Concerning the Production and Transformation of Light, *Annalen der Physik*, **17** (6), 132–148 (1905).

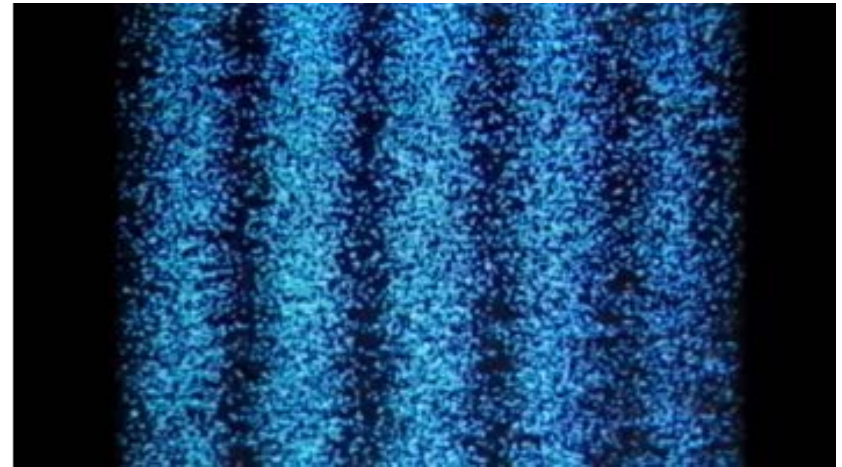
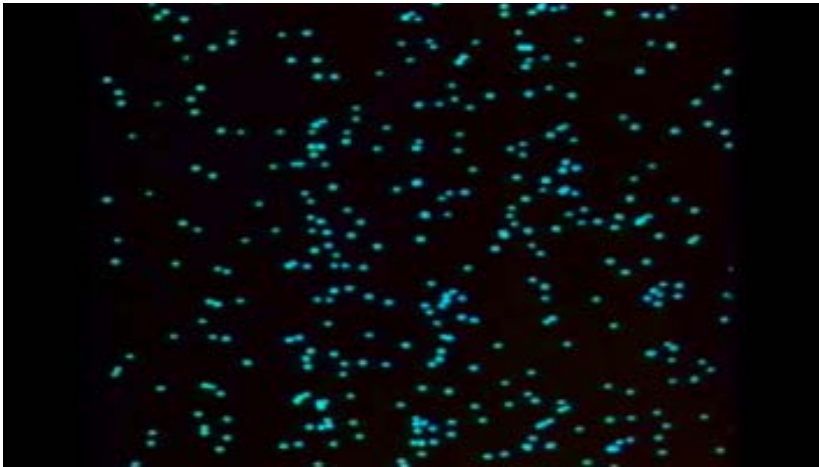
One of four Einstein's Annus Mirabilis (Miracle Year) papers published in 1905.

$$E_{\text{photon}} = h\nu$$



# Photoelectric effect

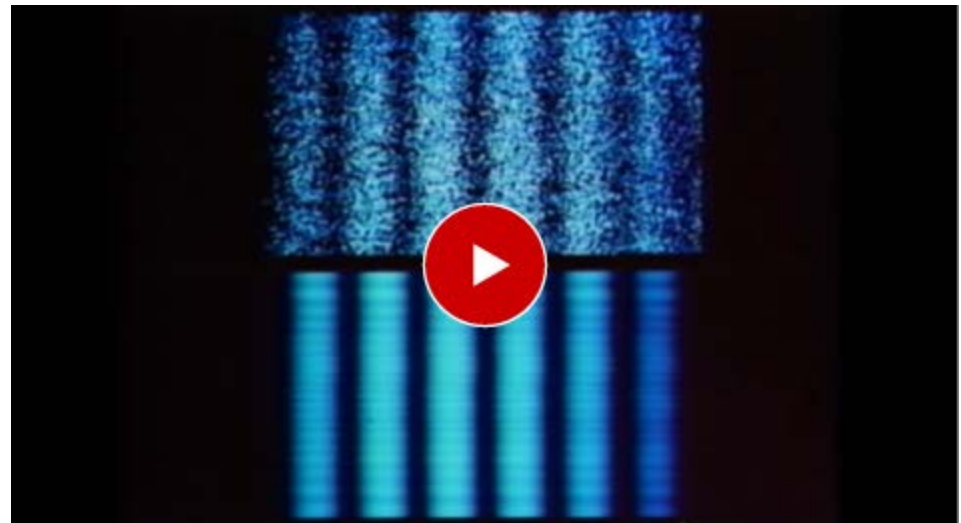
Young's Interference Experiment or Double-slit Interference Experiment carried out using technology to detect individual light particles to investigate whether interference fringes appear even if the light is drastically weakened to the level having only one particle. Results from the experiment confirmed that one photon exhibited an interference fringe (Hamamatsu Photonics, 1981).



Young's Interference Experiment  
with a single photon (top)

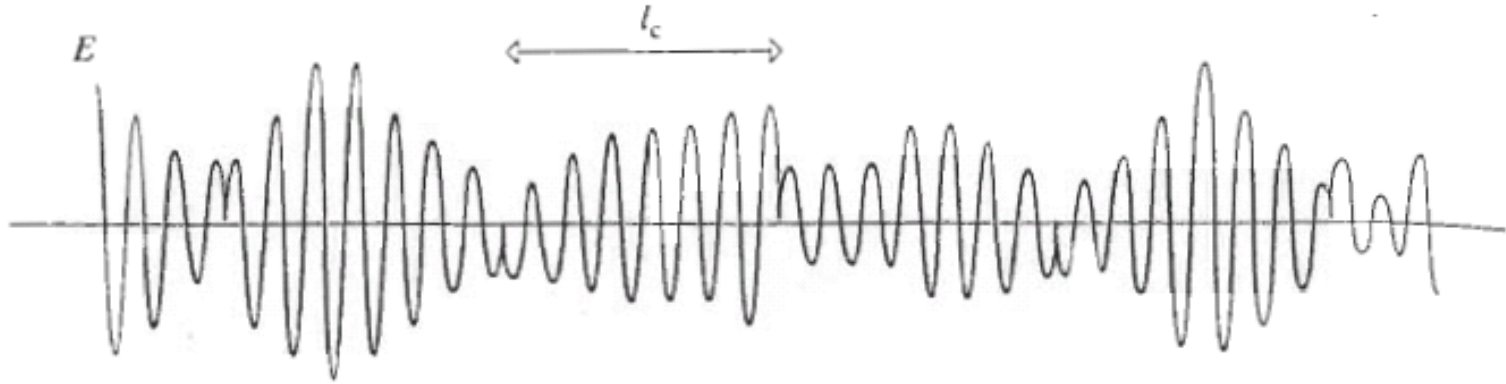
Young's Interference Experiment  
with a very large number of photons  
(bottom)

<http://photonterrace.net/en/photon/duality/>



This experiment captured the dual nature of the photon by a special camera for the first time ever

# Electromagnetic radiation: A mix of photon wavetrains



The energy  $q$  of photon is related to its frequency  $f$  and corresponding wavelength  $\lambda$  :

$$q = h f = h c / \lambda$$

where  $h = 6.626 \times 10^{-34}$  J s is Planck's constant and  $c = 2.998 \times 10^8$  m s<sup>-1</sup> is the speed of photons (phase velocity) in free space.

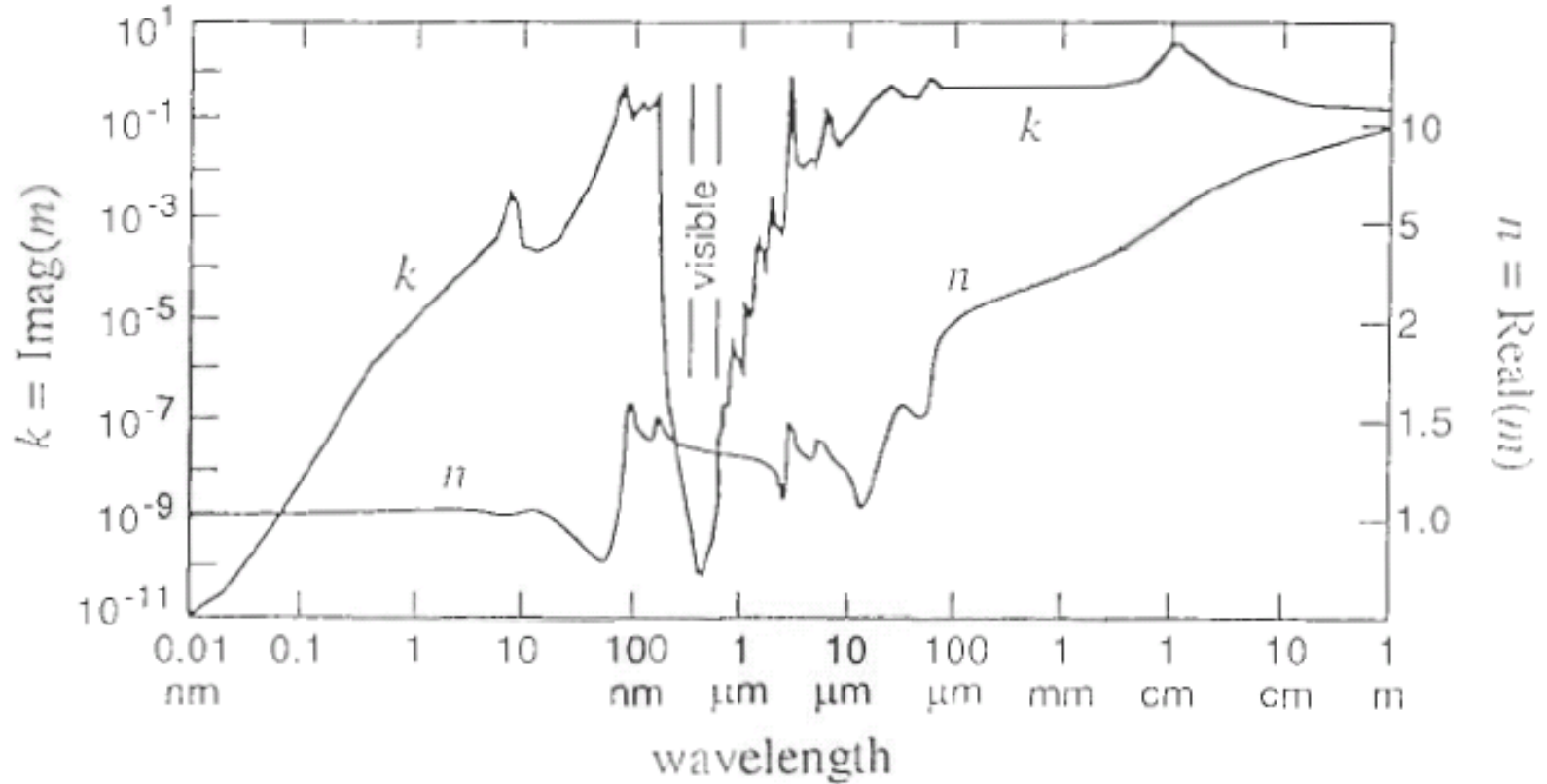
The speed of photons (phase velocity) in water is  $v_w = c / n_w$  where  $n_w$  is refractive index of water  $n_w = c / v_w$

The energy  $q_w$  of photon in water is:

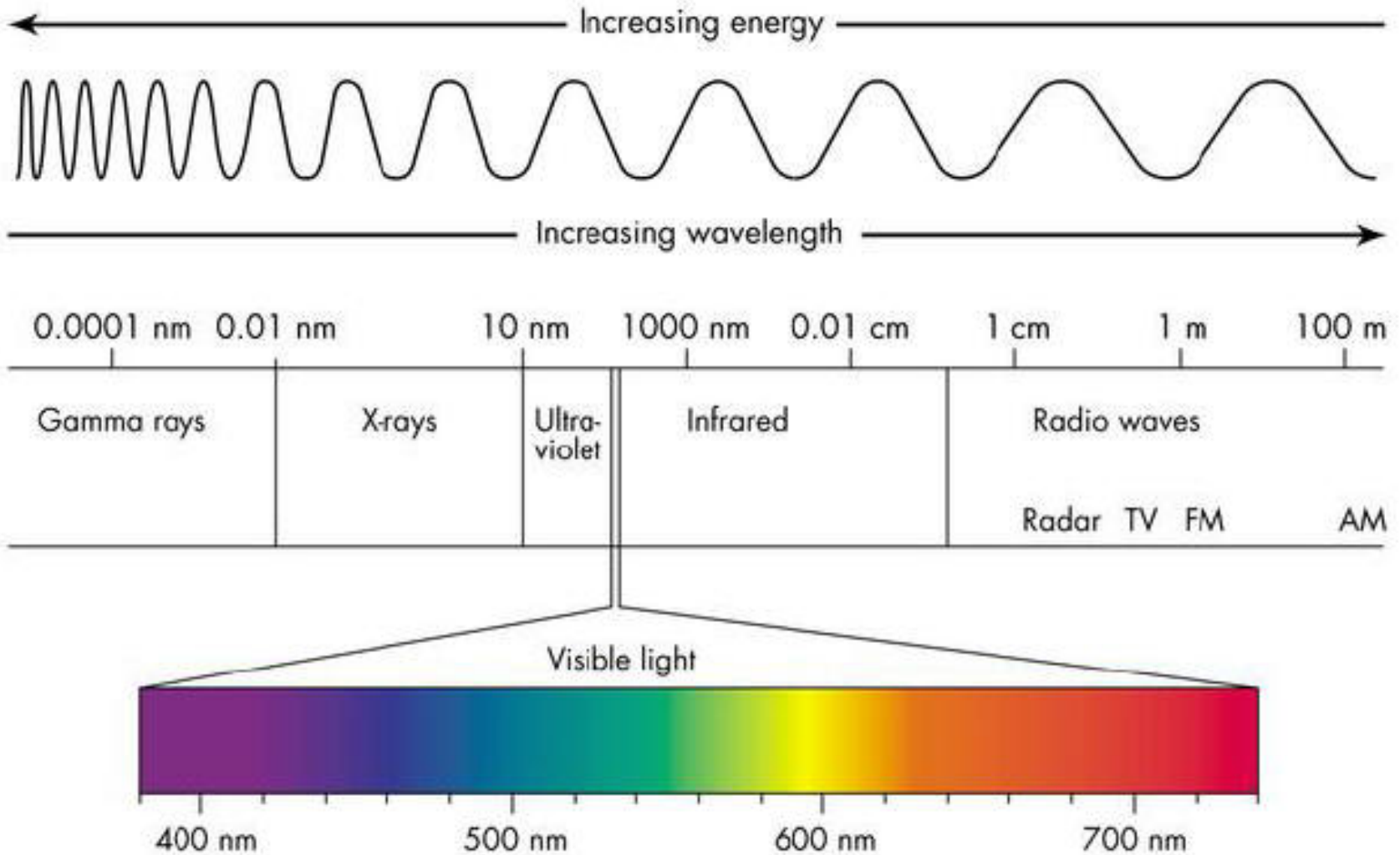
$$q_w = q = h f = h v_w / \lambda_w \quad \text{where } \lambda_w = \lambda / n_w$$



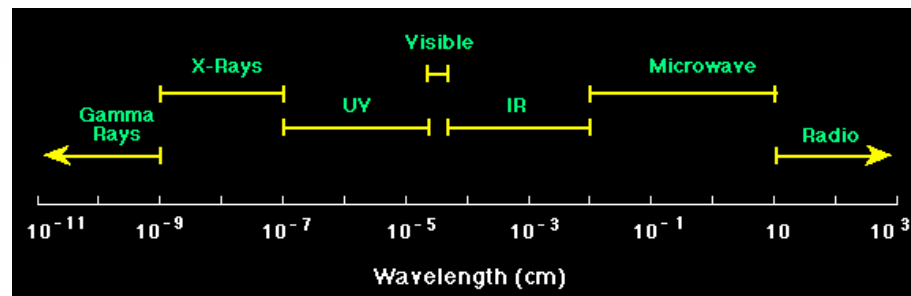
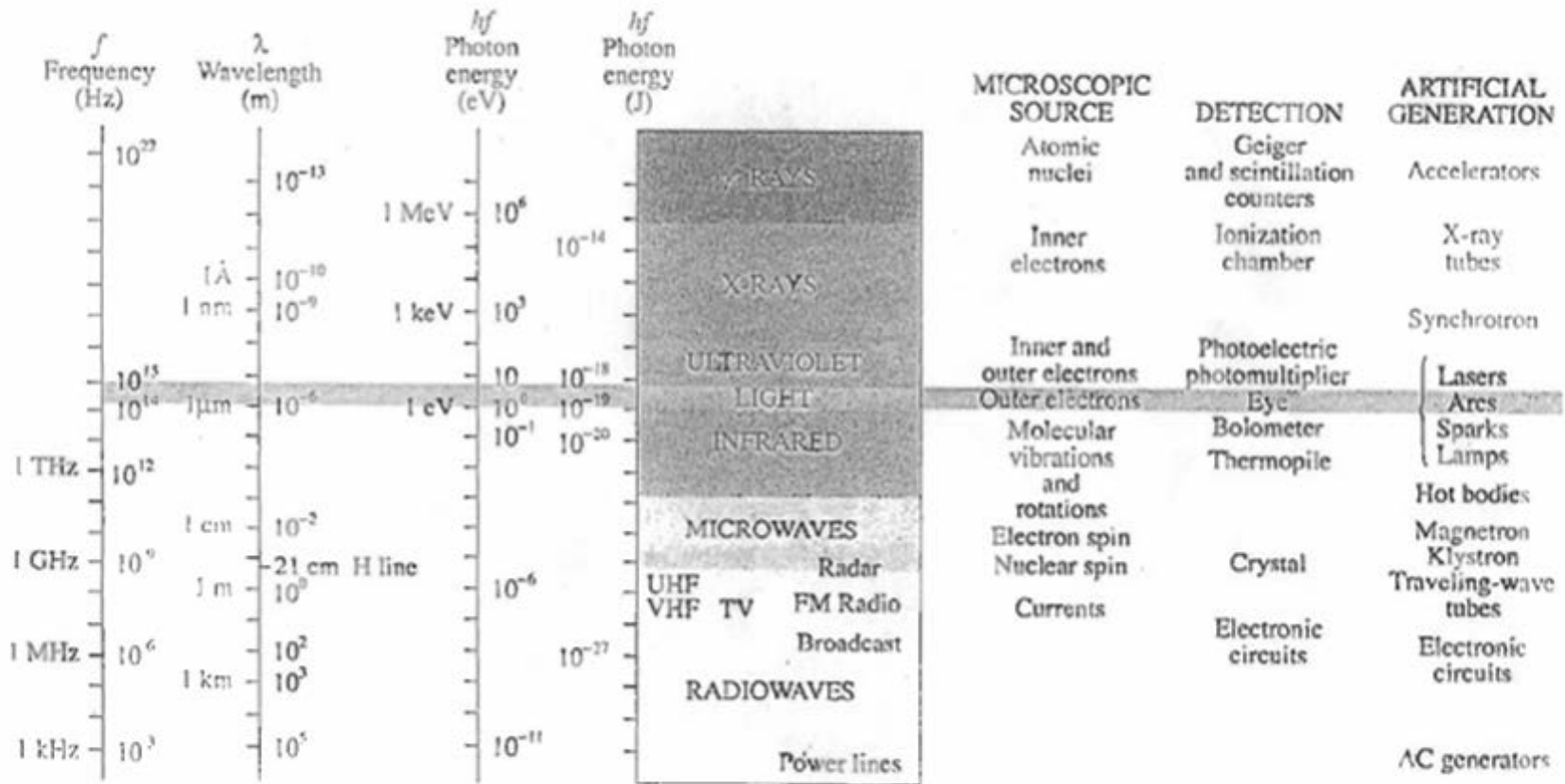
# Refractive Index of Water



# The Electromagnetic-Photon Spectrum

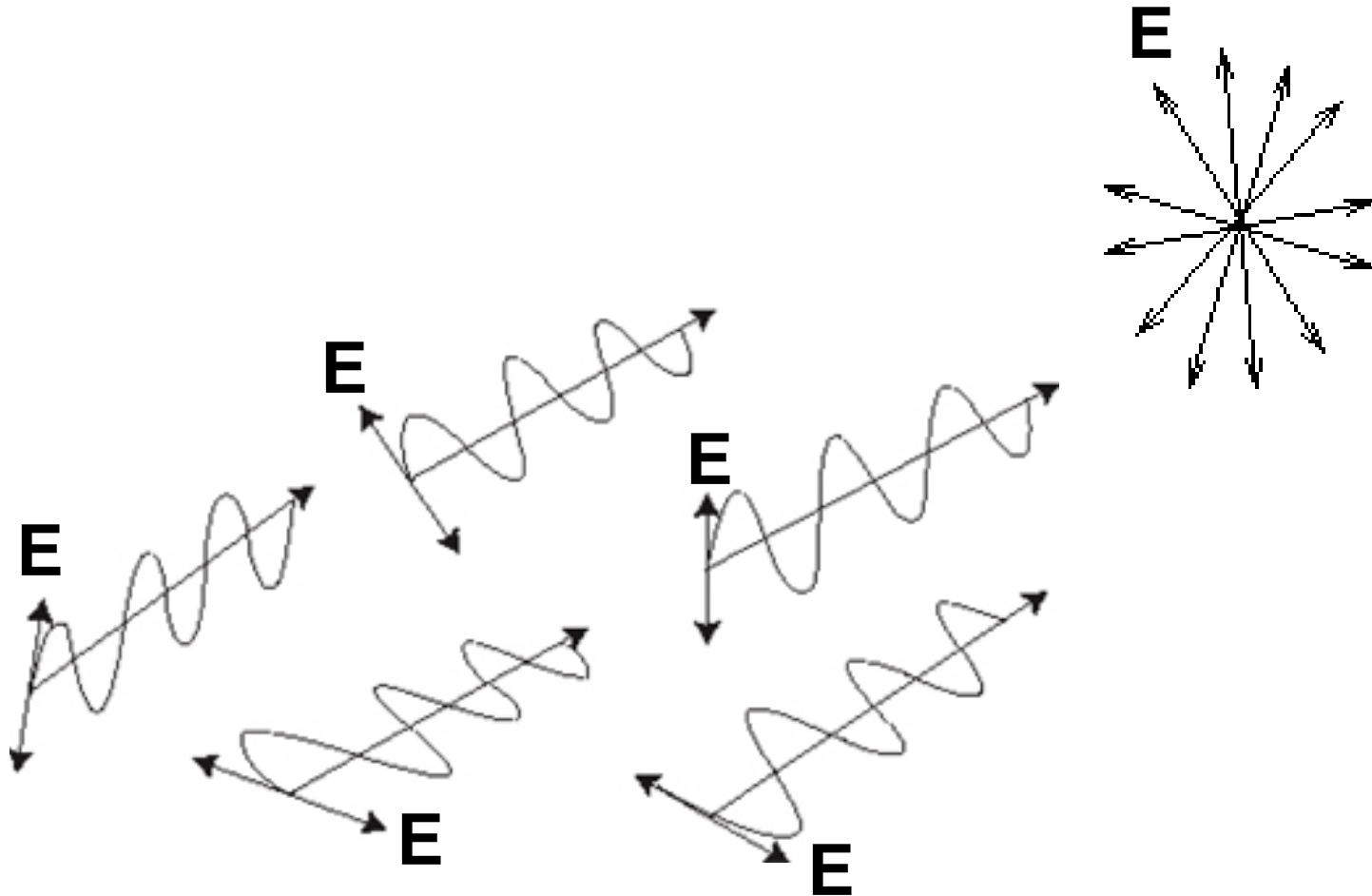


# The electromagnetic-photon spectrum



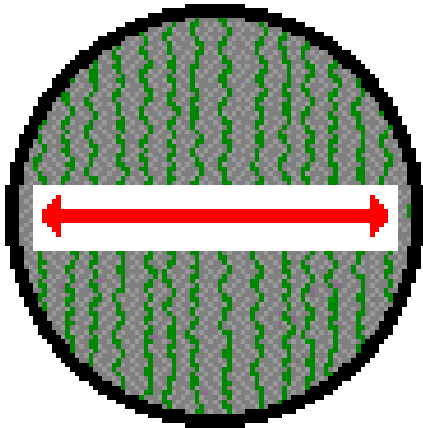
(Hecht 1994)

Randomly polarized (unpolarized) light is a jumble  
of random, rapidly changing **E**-fields

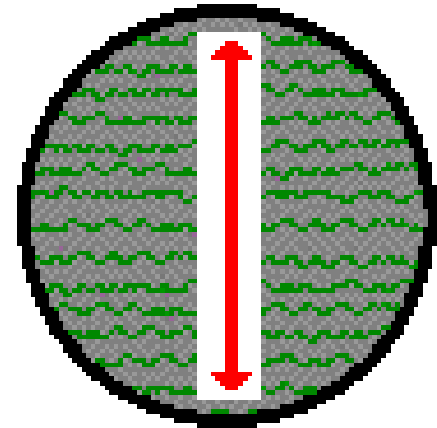


# Polarization by transmission (polarizing filters)

## Relationship Between Long-Chain Molecule Orientation and the Orientation of the Polarization Axis

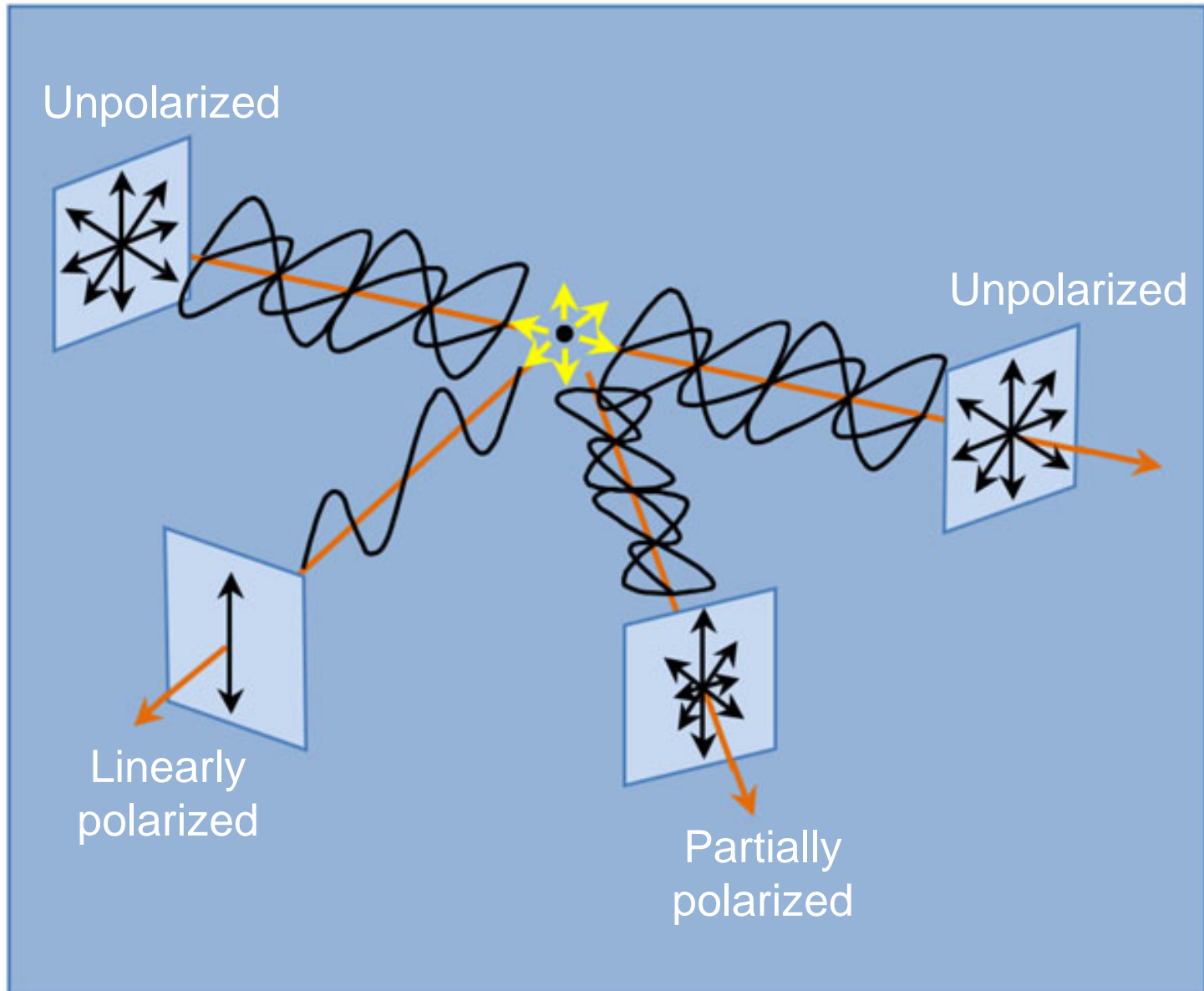


**When molecules in the filter  
are aligned vertically, the  
polarization axis is horizontal.**

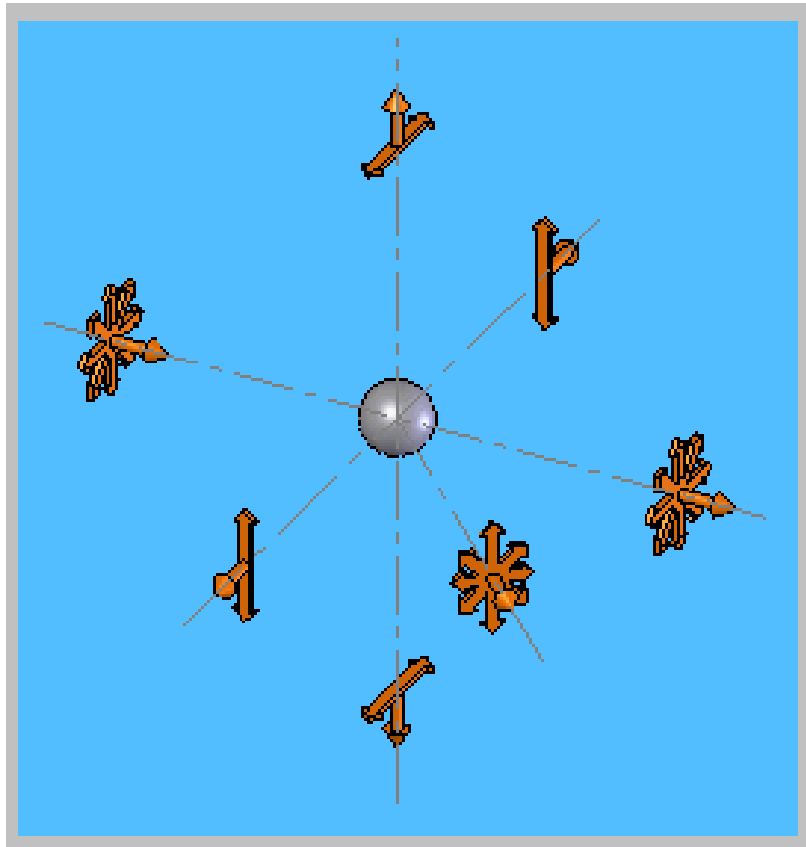


**When molecules in the filter  
are aligned horizontally, the  
polarization axis is vertical.**

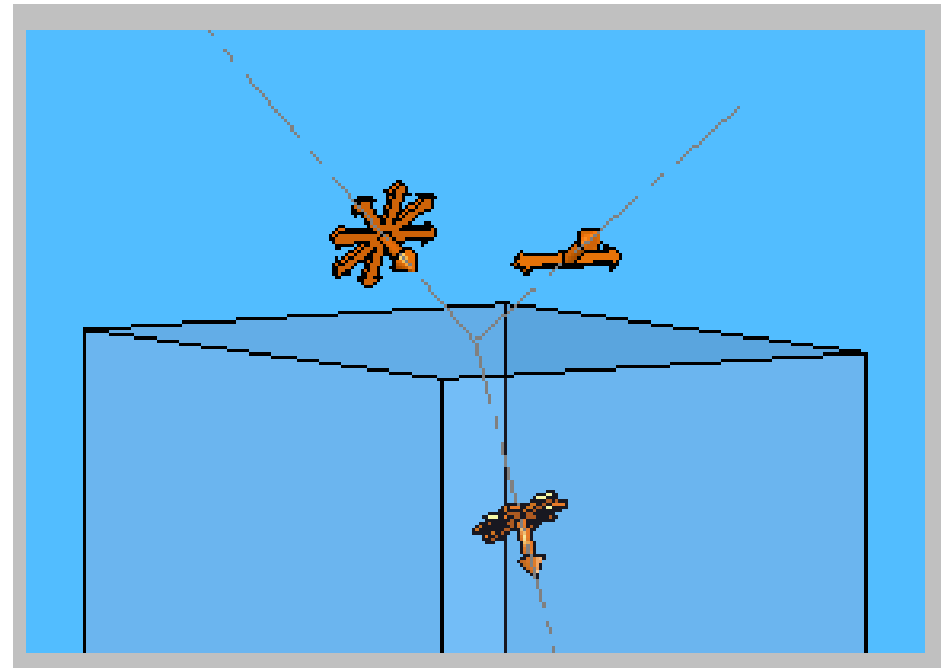
# Polarization by scattering



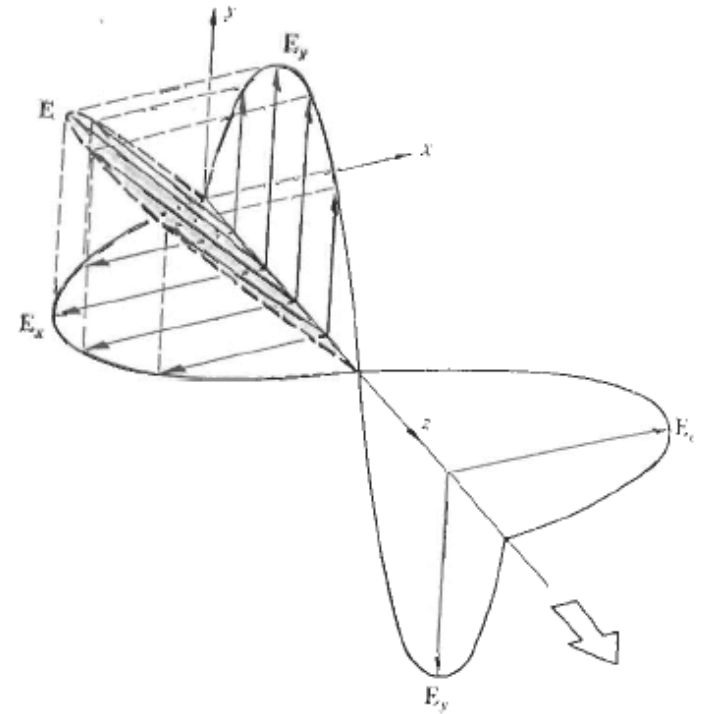
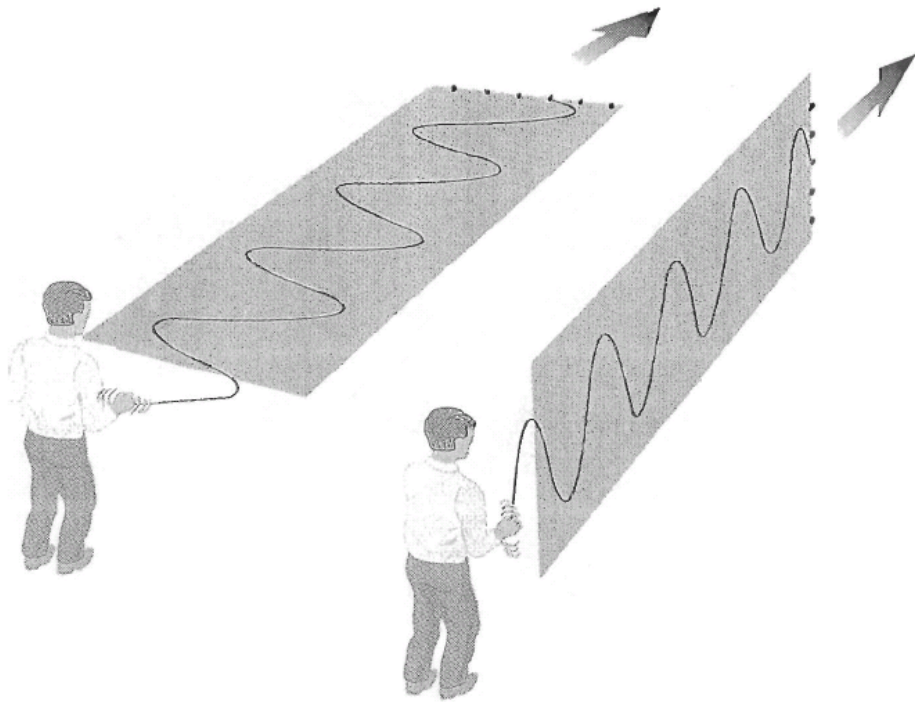
# Polarization by scattering



# Polarization by reflection

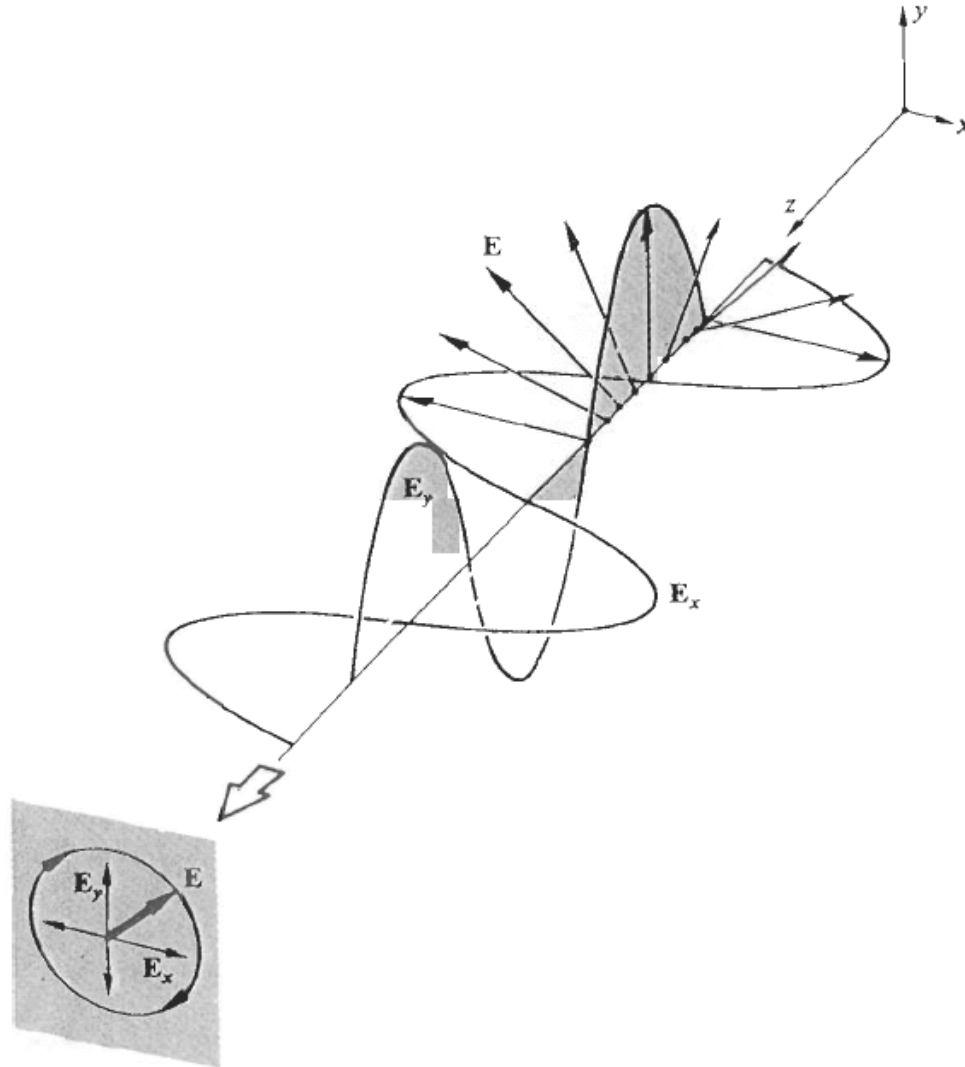


# Plane-Polarized or Linearly-Polarized Light

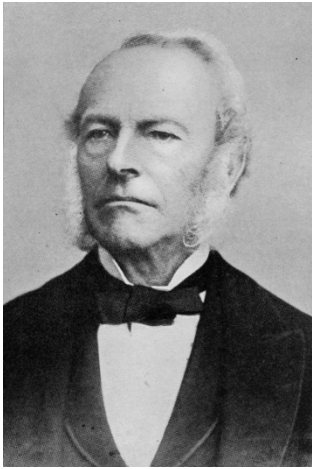




# Right-circular light



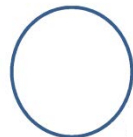
# Stokes vector



George Gabriel Stokes  
(1819 – 1903)

$$S = \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix} = \begin{pmatrix} \langle E_x^2 \rangle + \langle E_y^2 \rangle \\ \langle E_x^2 \rangle - \langle E_y^2 \rangle \\ 2E_x E_y \cos \xi \\ 2E_x E_y \sin \xi \end{pmatrix}$$

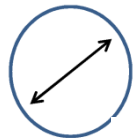
$$I = \longleftrightarrow + \updownarrow$$

 Unpolarized:  
transmits intensity  
of any incident light

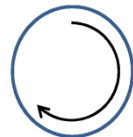
$$Q = \longleftrightarrow - \updownarrow$$

 transmits only  
horizontal light

$$U = \nearrow - \searrow$$

 transmits only  
linear light at 45°

$$V = \circlearrowleft - \circlearrowright$$

 transmits only  
R-polarized light

*Degree of  
polarization*

$$p = \frac{\sqrt{Q^2 + U^2 + V^2}}{I},$$

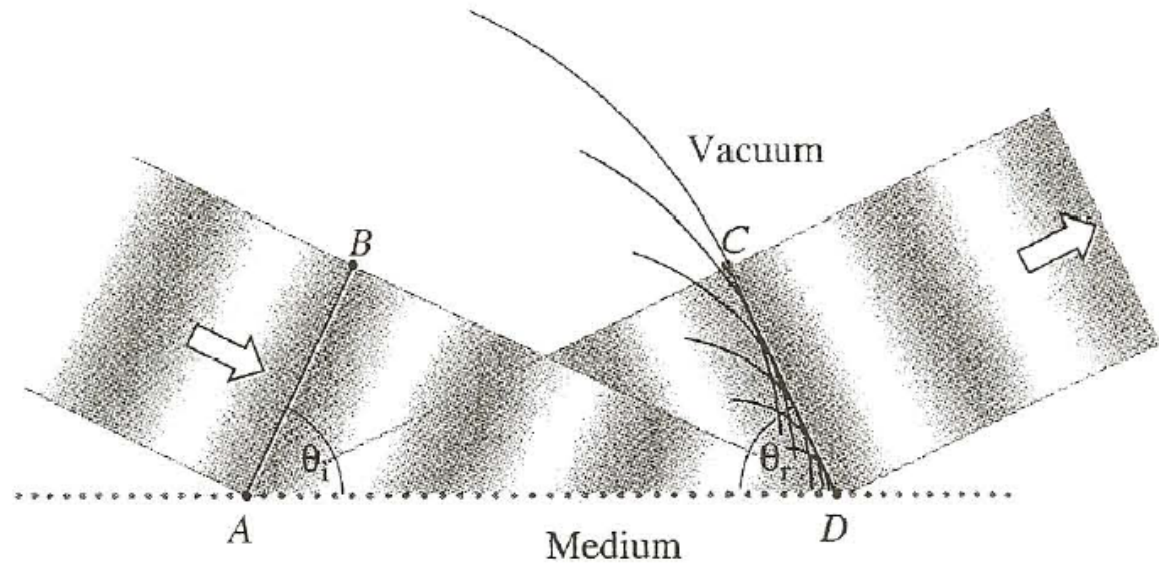
$$p_{\text{lin}} = \frac{\sqrt{Q^2 + U^2}}{I},$$

$$p_{\text{circ}} = \frac{V}{I}$$

# Reflection at the boundary between the media of different densities (refractive index)



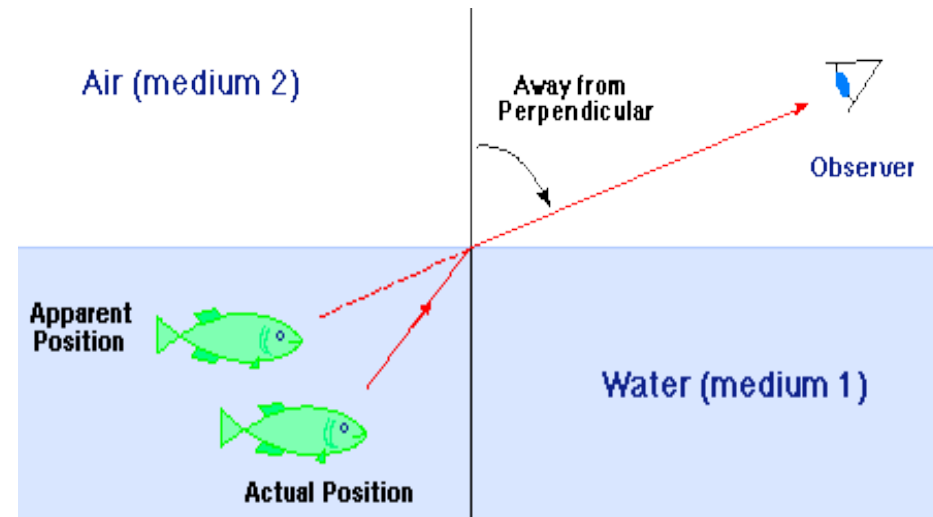
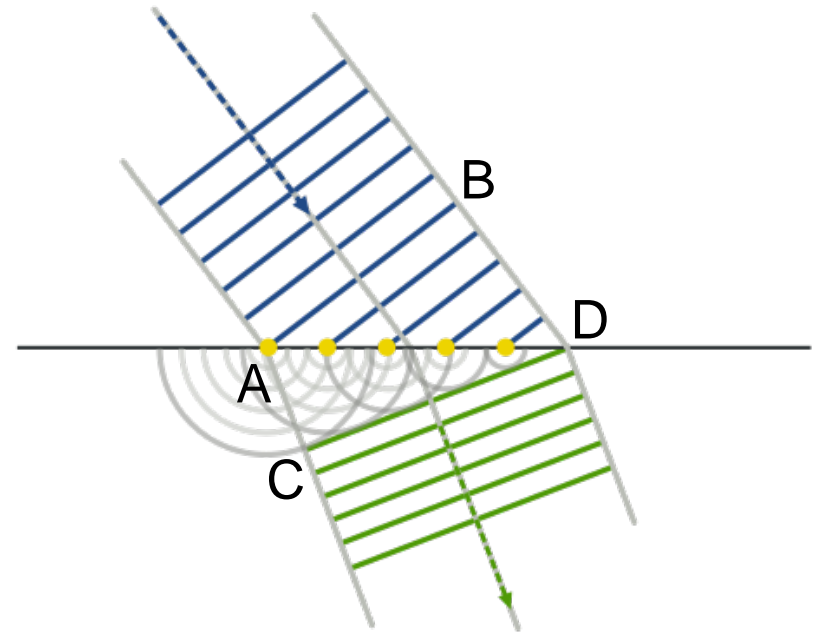
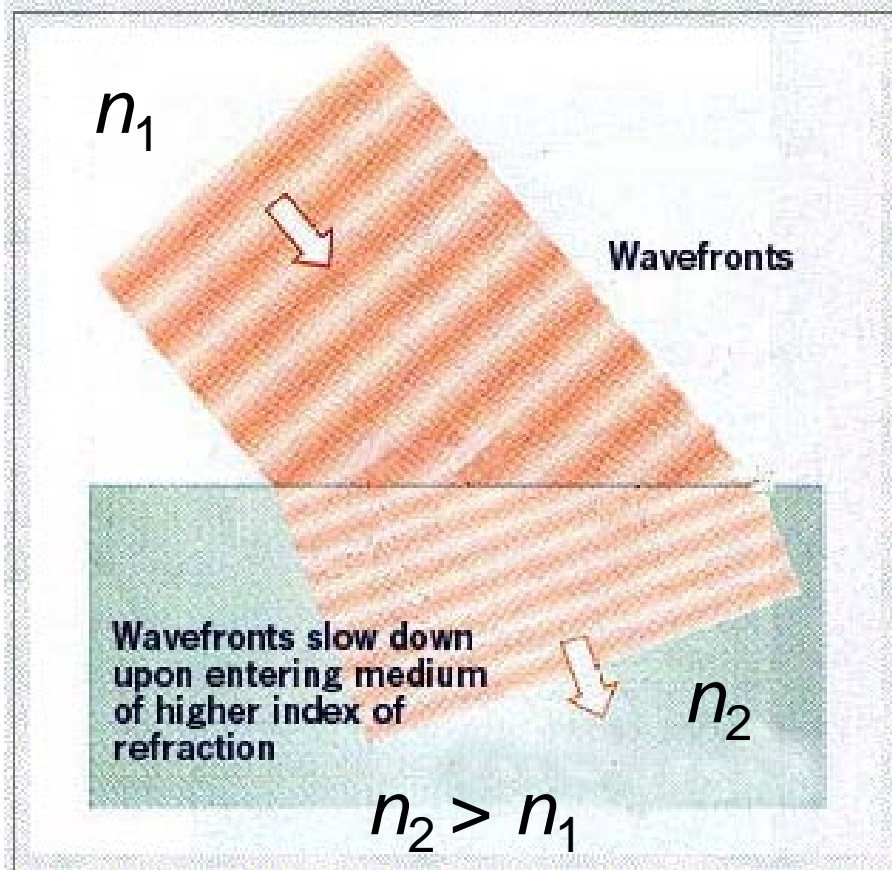
Christian Huygens  
(1629 - 1695)



Wavefront geometry for reflection. The reflected wavefront  $\overline{CD}$  is formed of waves scattered by the atoms on the surface from A to D. Just as the first wavelet arrives at C from A, the atom at D emits, and the wavefront along  $\overline{CD}$  is completed.

Angle of incidence = Angle of reflection

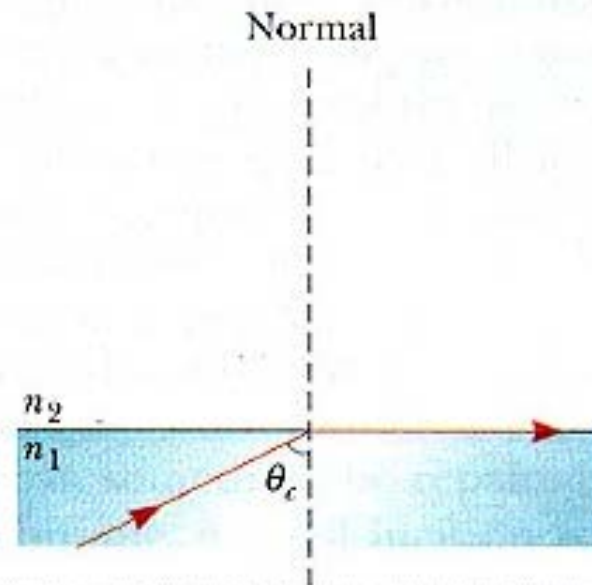
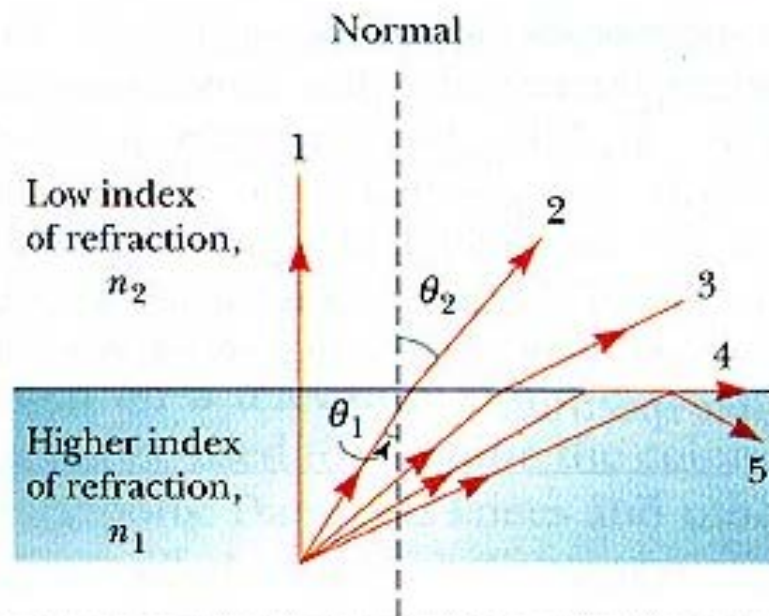
# Refraction



Snell's law

$$n_1 \sin(i) = n_2 \sin(r)$$

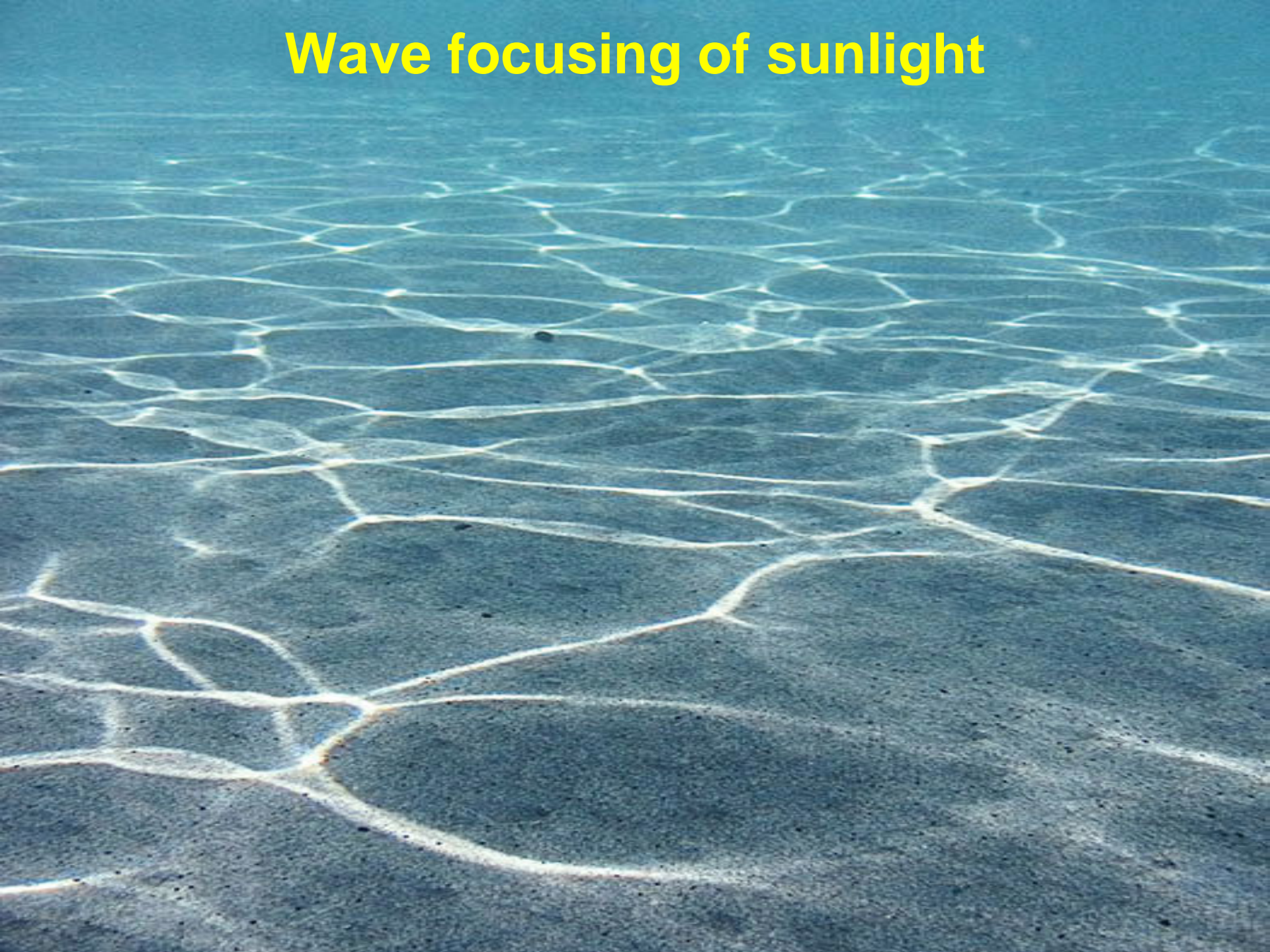
# Internal Reflection



Ray 4 is the first to be 100 % reflected; its angle of incidence is called the *critical angle*.



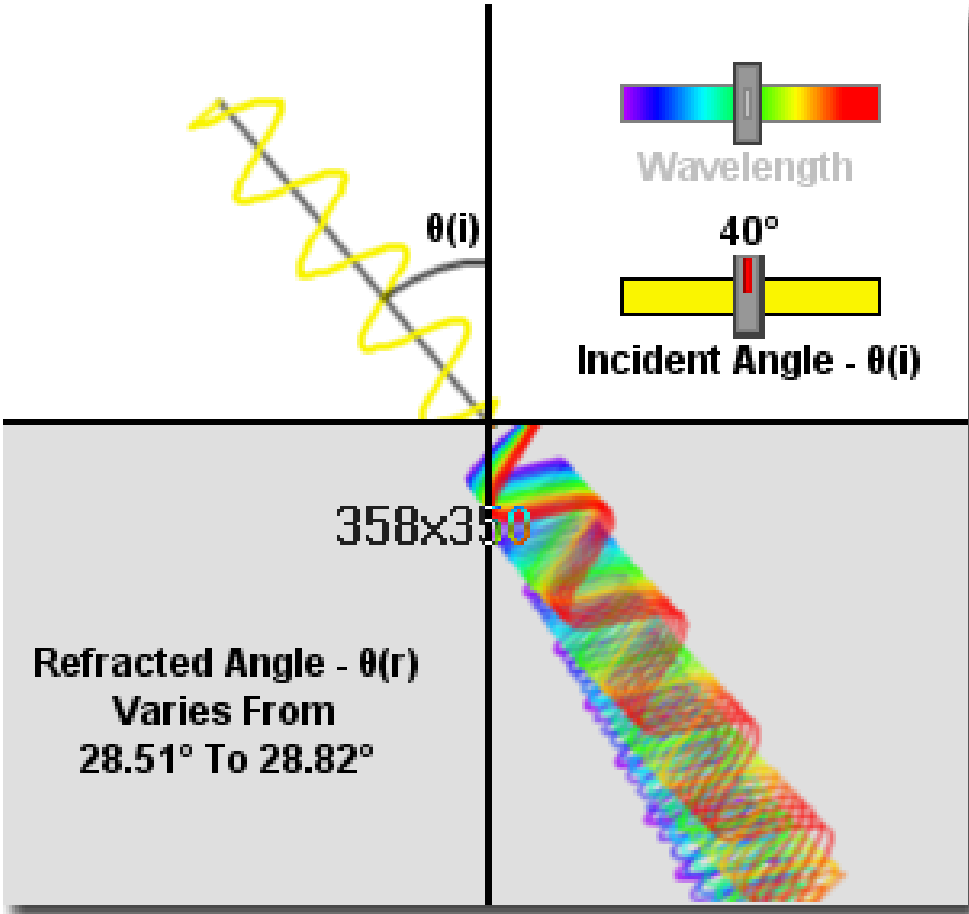
# Wave focusing of sunlight







# Dispersion

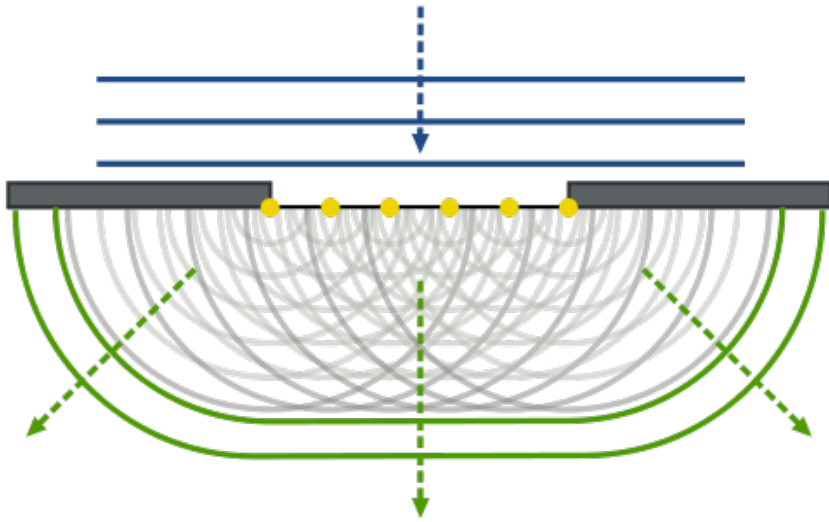


- White Light
- Monochromatic

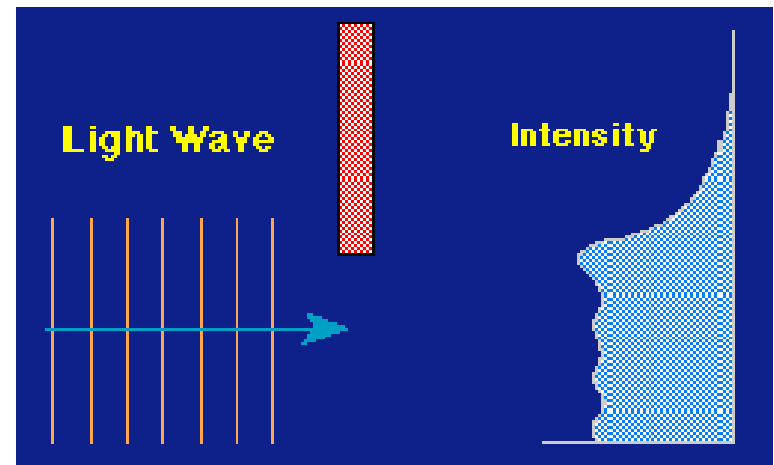
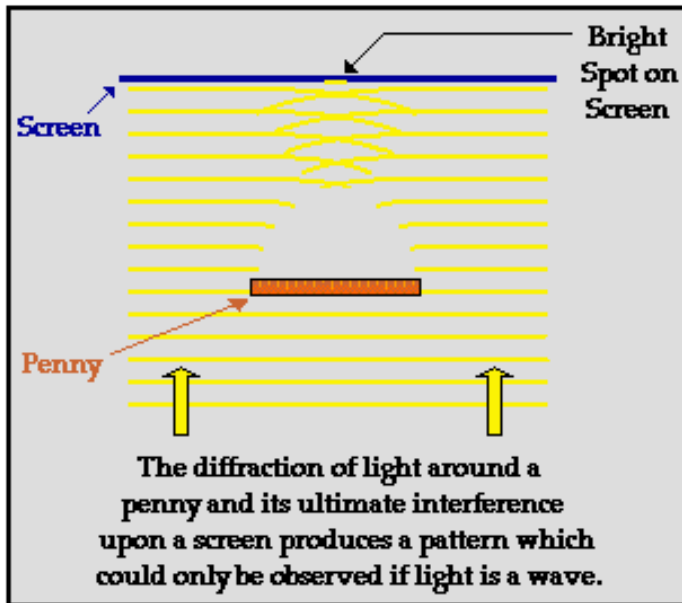
Choose A Material (RI)

Water	1.3330	▼
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# Diffraction



Augustin-Jean Fresnel  
(1788 - 1827)



The intensity of light behind the barrier is not zero in the shadow region due to diffraction (light wave has a capability to “bend around corners”)

# Light and matter

Emission - birth of a photon

Absorption - death of a photon

Scattering - life of a photon

# Emission of Light

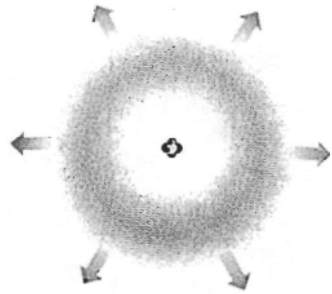
## Thermal radiation

light emission is related to the temperature of an object with all molecules, atoms, and subatomic particles involved in thermal motion

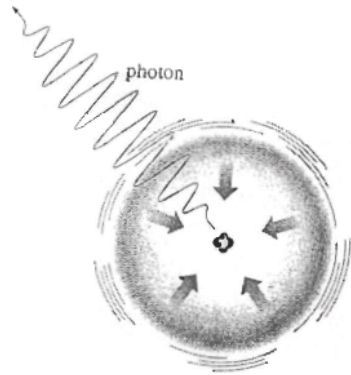
## Luminescence

light emission is related to the specific changes in the energy levels of specific molecules

# Energy changes within atoms



Excitation of the ground state



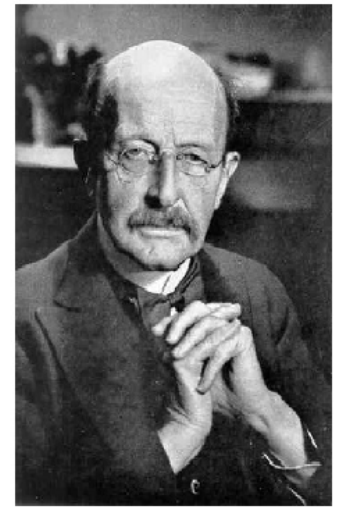
De-excitation with emission of a photon



Ground state  $\sim 10^{-9}$  -  $10^{-8}$  sec later

# Planck Radiation Law

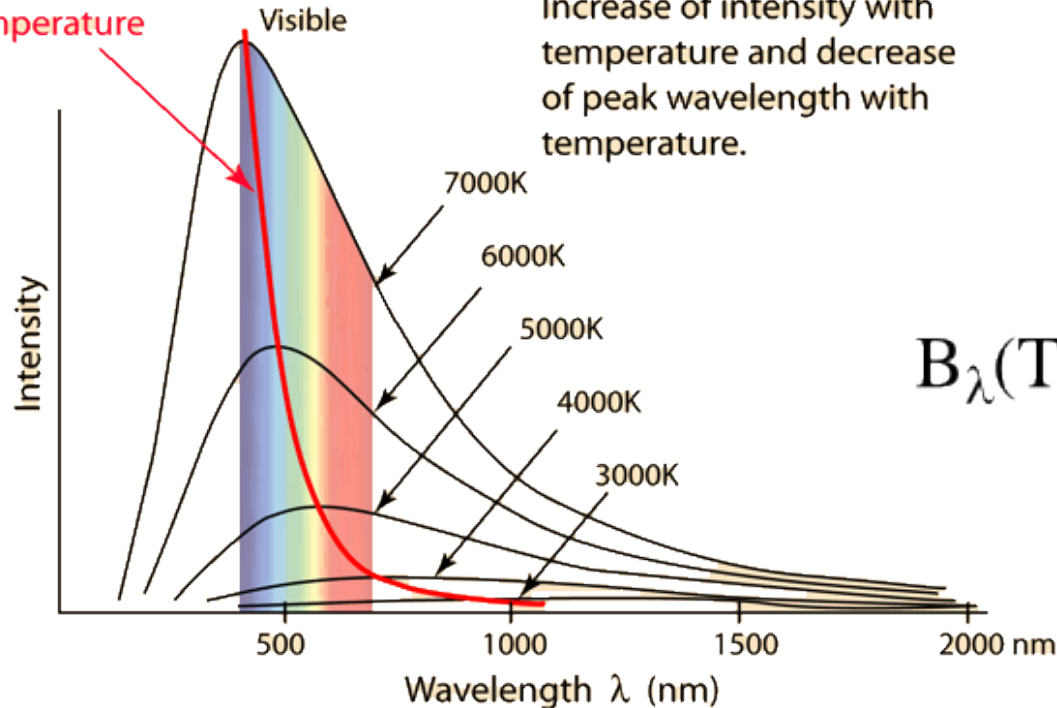
This law governs the intensity of radiation emitted by unit surface area into a fixed direction (solid angle) from the blackbody as a function of wavelength for a fixed temperature.



Max Planck (1858 - 1947)  
Nobel Prize 1918

Decrease of  $\lambda_{\text{peak}}$   
with increase in  
temperature

Increase of intensity with  
temperature and decrease  
of peak wavelength with  
temperature.



$$B_{\lambda}(T) = \frac{2hc^2}{\lambda^5} \frac{1}{e^{\frac{hc}{\lambda k_B T}} - 1}$$

$h$  = Planck's constant =  $6.626 \cdot 10^{-34} \text{ J} \cdot \text{s}$

$c$  = speed of light =  $2.997925 \cdot 10^8 \text{ m} / \text{sec}$

$\lambda$  = wavelength (m)

$k$  = Boltzmann's constant =  $1.381 \cdot 10^{-23} \text{ J} / \text{K}$

$T$  = temperature (K)

# Stefan-Boltzmann Law

**The Stefan-Boltzmann law** states that a blackbody emits electromagnetic radiation with a total energy flux  $E$  proportional to the fourth power of the Kelvin temperature  $T$  of the object



Joseph Stefan  
(1835 - 1893)

$$E = \sigma T^4$$

where  $\sigma$  (sigma) =  $5.67 \times 10^{-8} \text{ Wm}^{-2} \text{ K}^{-4}$   
and  $T$  is the temperature in Kelvin



Ludvig Boltzmann  
(1844 - 1906)

# Wien's Displacement Law

**Wien's displacement law** states that dominant wavelength at which a blackbody emits electromagnetic radiation is inversely proportional to the Kelvin temperature of the object

$$\lambda_{\max} = \frac{0.0029 \text{ K m}}{T}$$

$\lambda_{\max}$  = wavelength of maximum emission of the object  
(in meters)

$T$  = temperature of the object (in kelvins)



For example

– The Sun,  $\lambda_{\max} = 500 \text{ nm} \rightarrow T = 5800 \text{ K}$

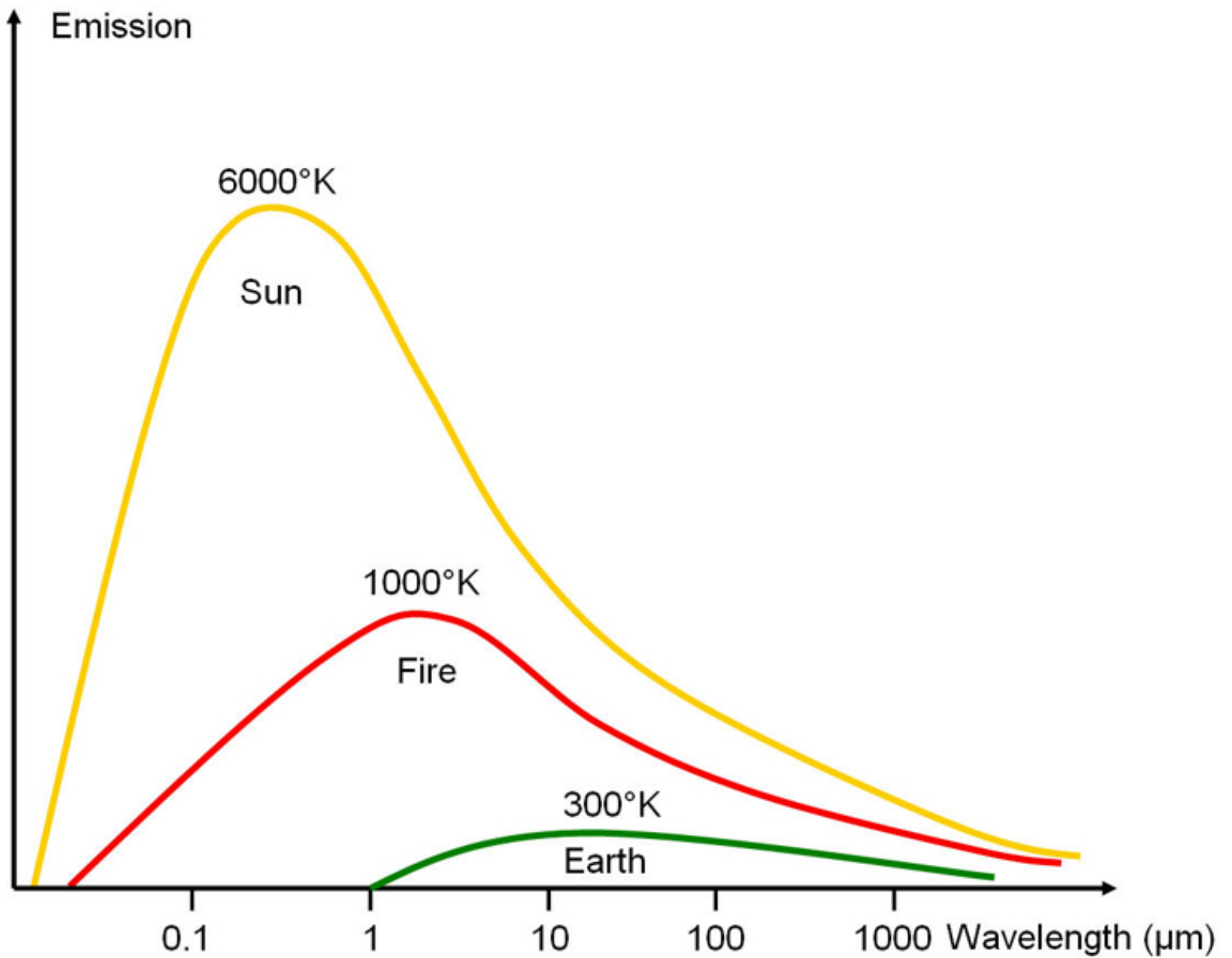
– Human body at 37 degrees Celsius or 310 Kelvin  $\rightarrow \lambda_{\max} = 9.35 \text{ } \mu\text{m} = 9350 \text{ nm}$

Wilhelm Wien (1864 - 1928)  
Nobel Prize 1911



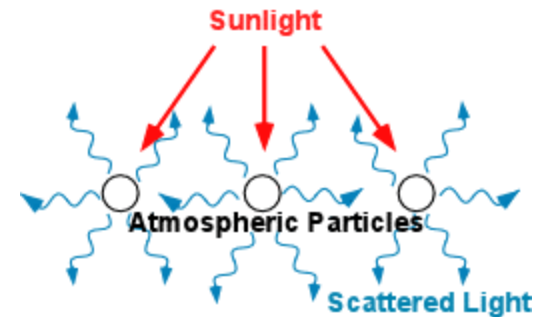
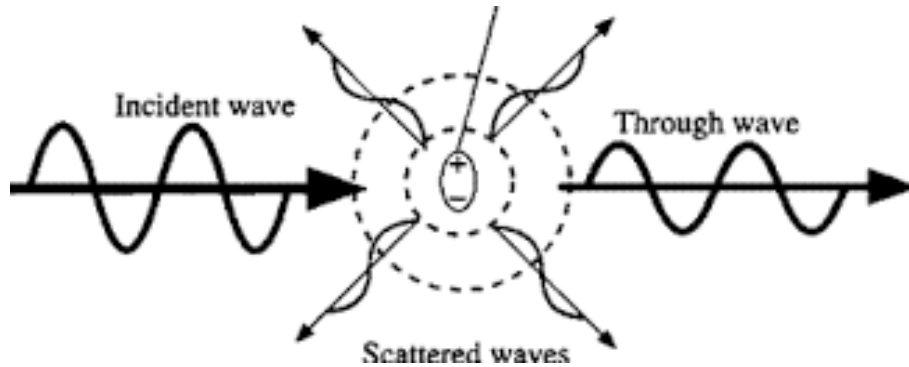
**Ocean optics is concerned primarily with the study of visible light, more specifically the relatively narrow range of electromagnetic spectrum from near-UV through visible to near-IR**



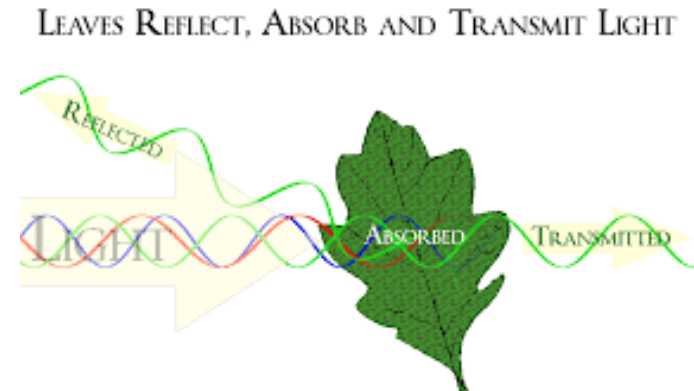
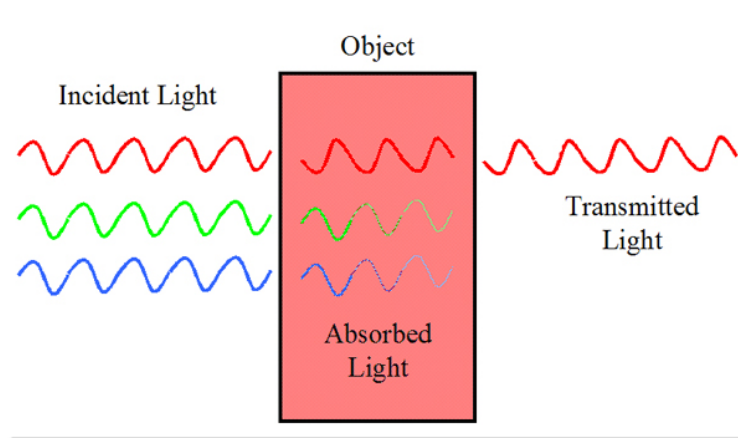


# Interaction of Light and Matter

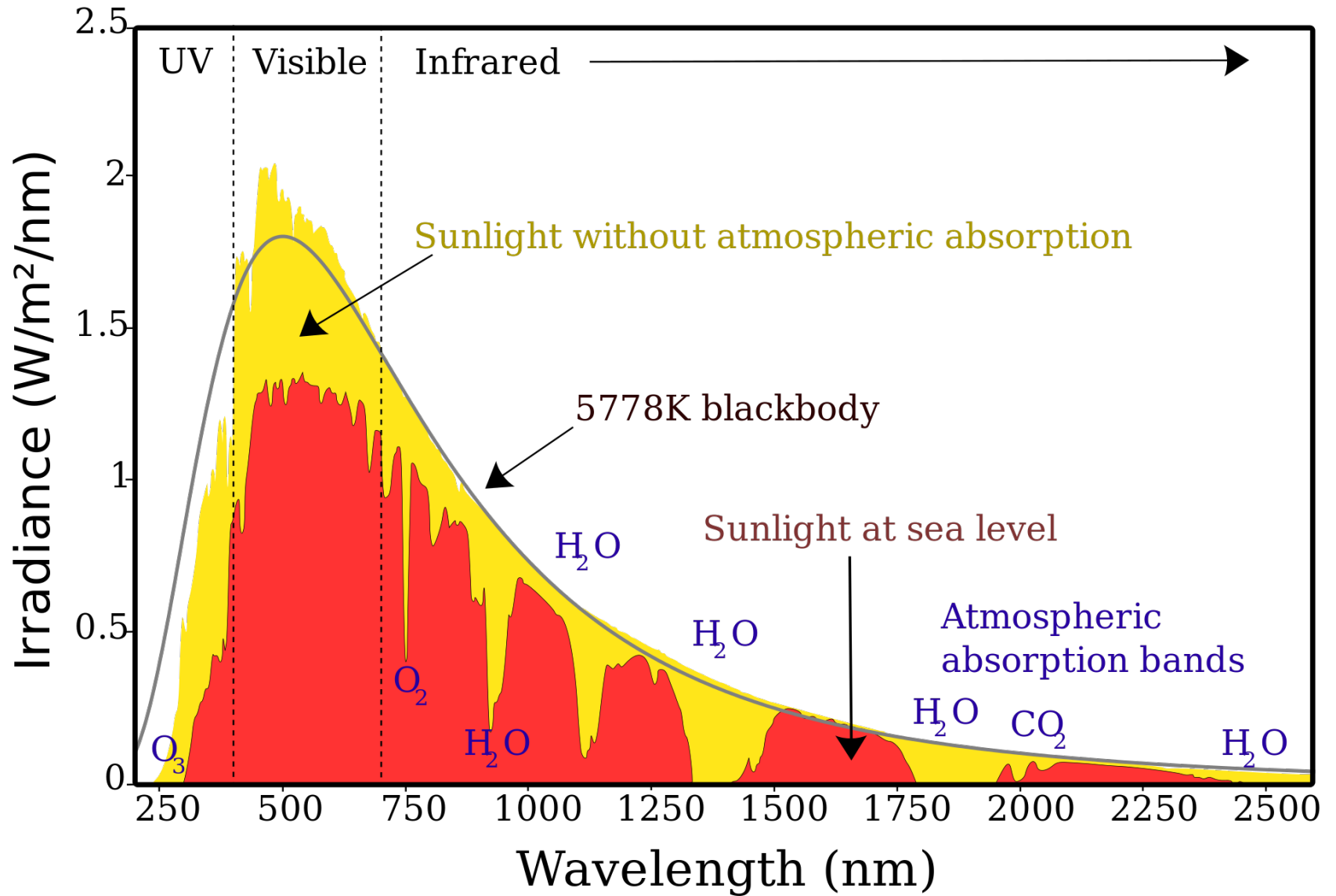
**Scattering** (life of photon) – change of direction of propagation



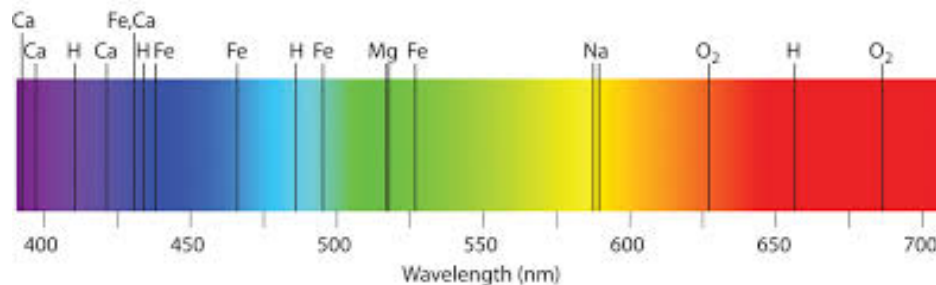
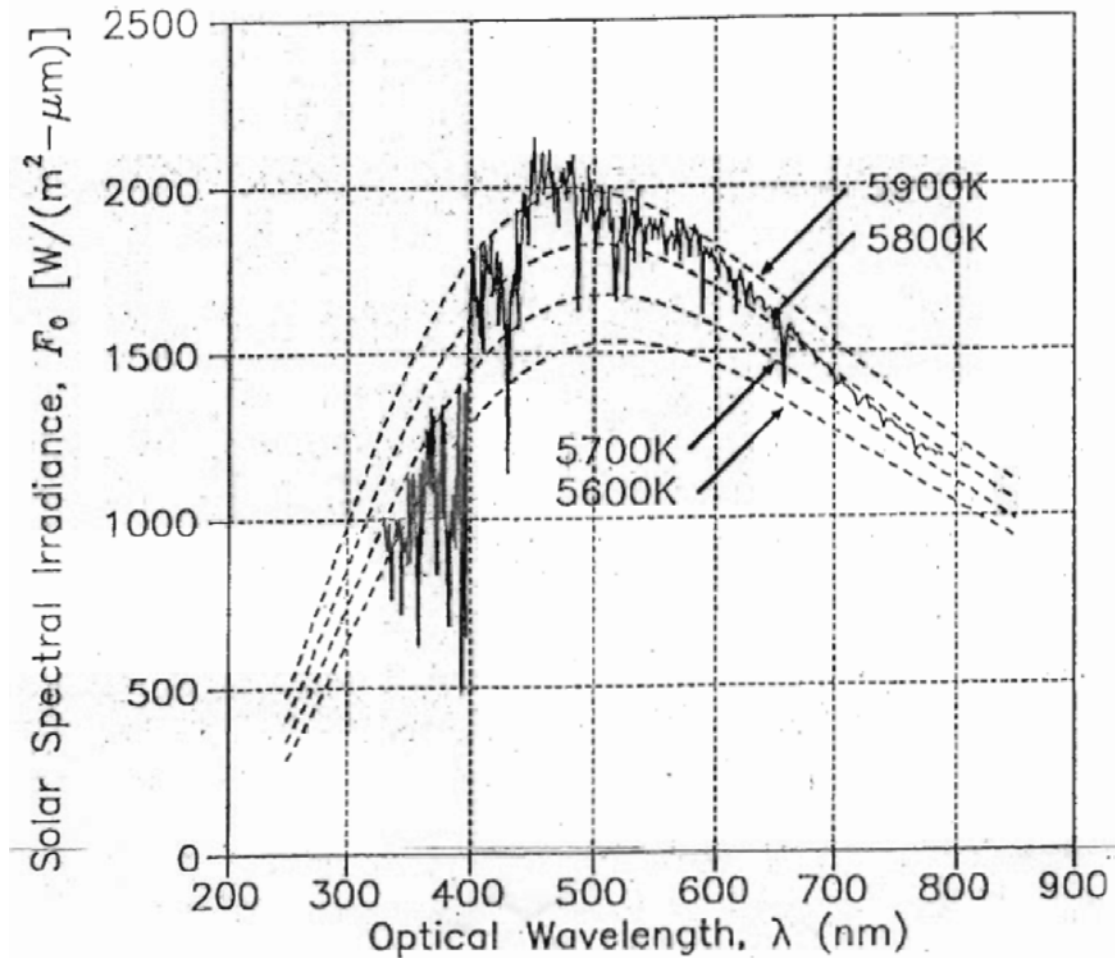
**Absorption** (death of photon) – transfer of energy to matter



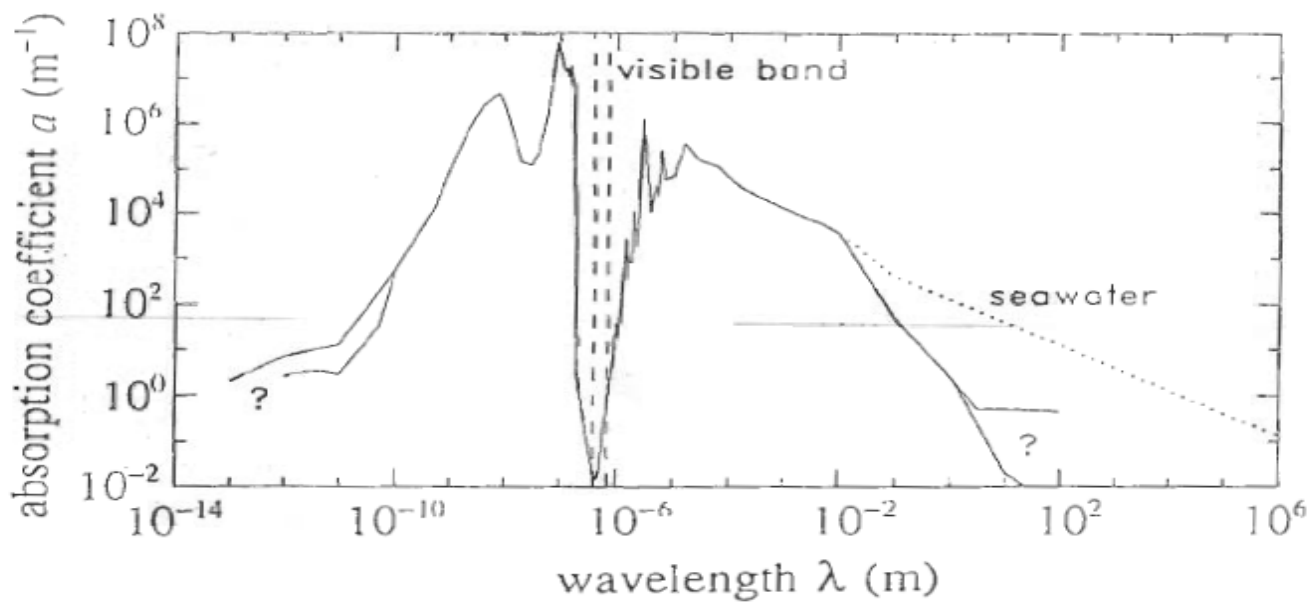
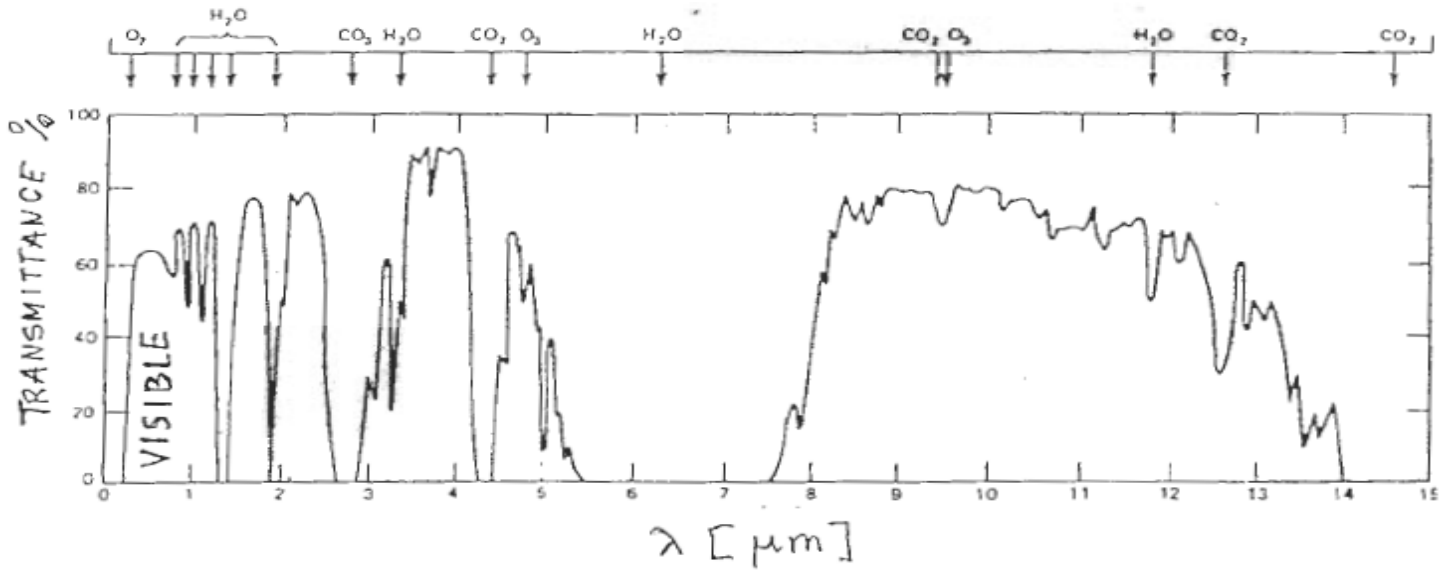
# Spectrum of Solar Radiation (Earth)



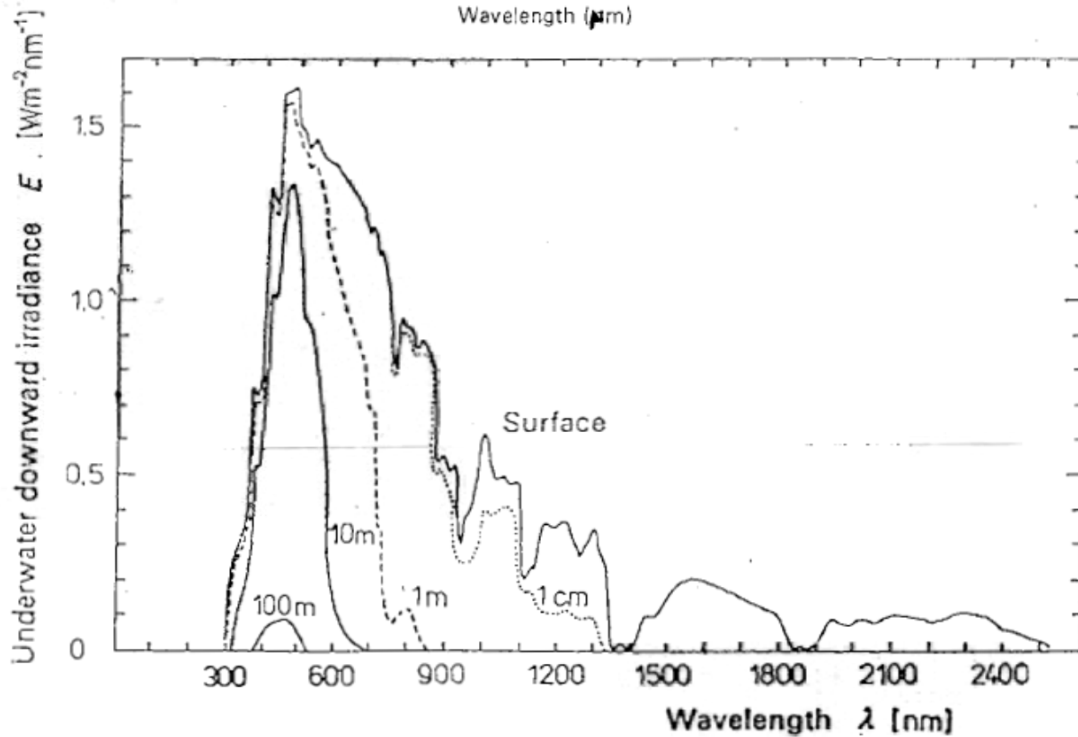
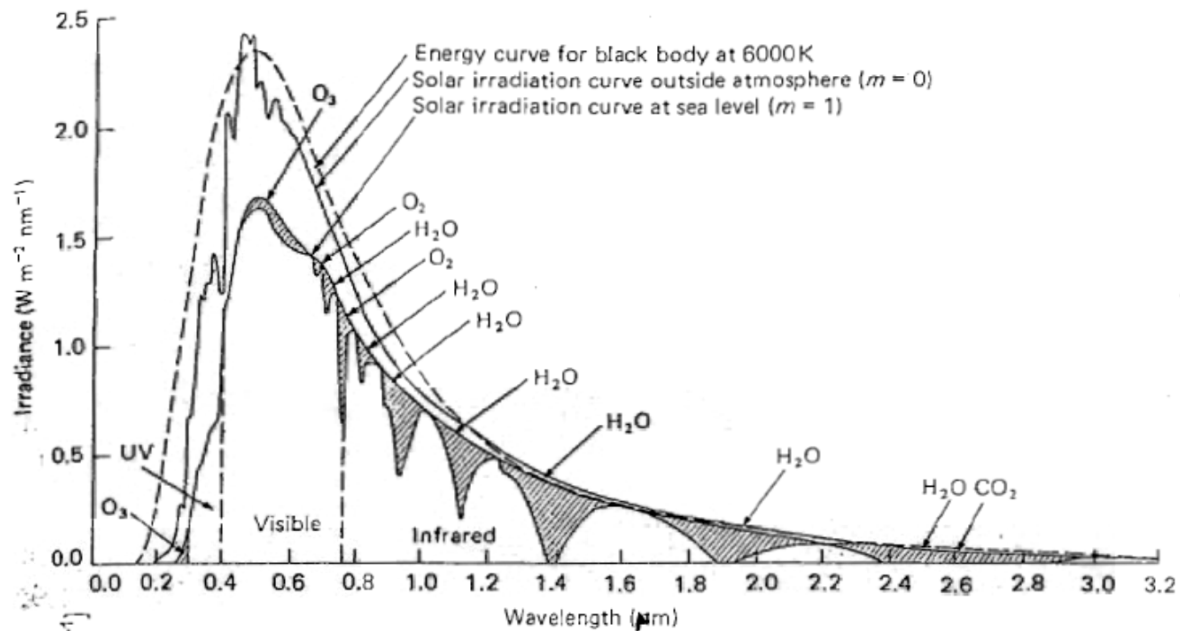
# Solar spectral irradiance outside the Earth's atmosphere



Overlap of “window” in atmospheric transmittance with minimum of water absorption in the visible band.

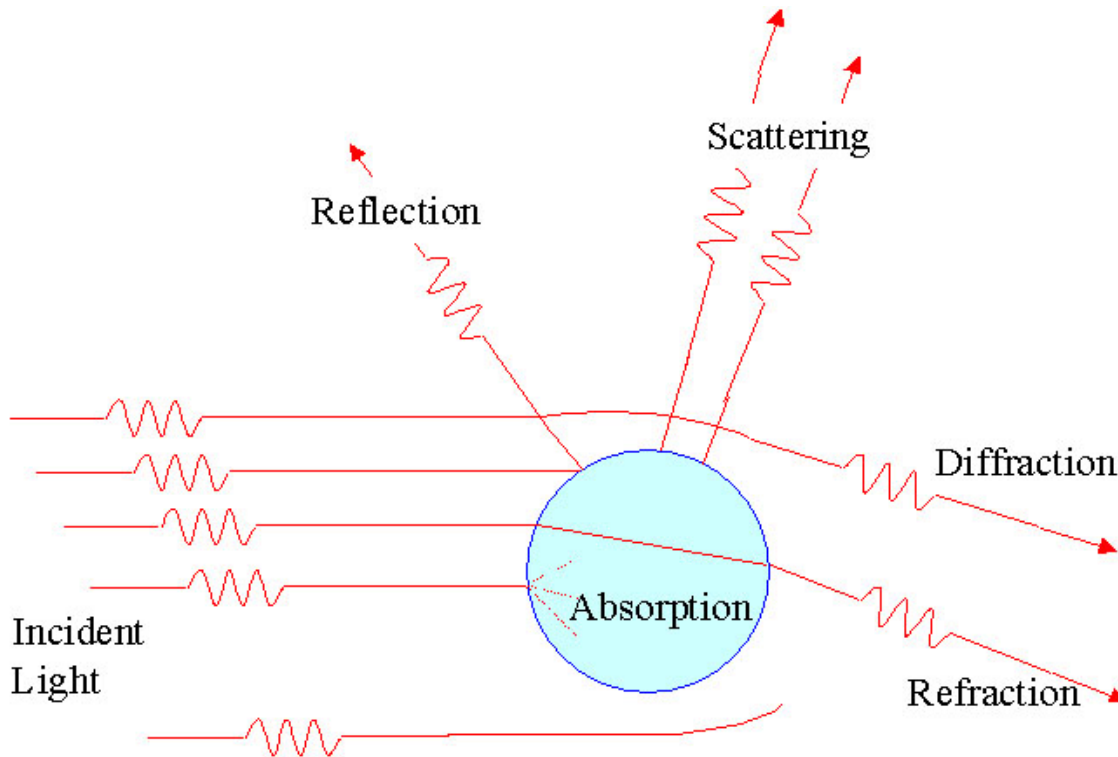


# Spectra of Solar Irradiance



# Interaction of light and matter

## Scattering - life of photon



## Absorption - death of photon

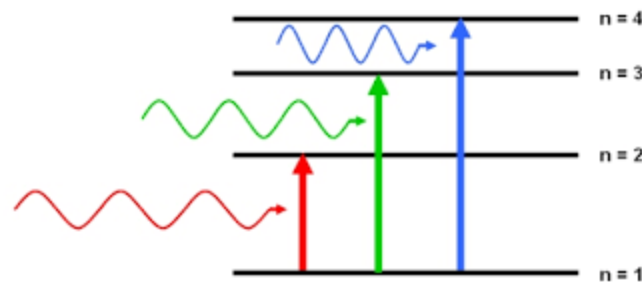
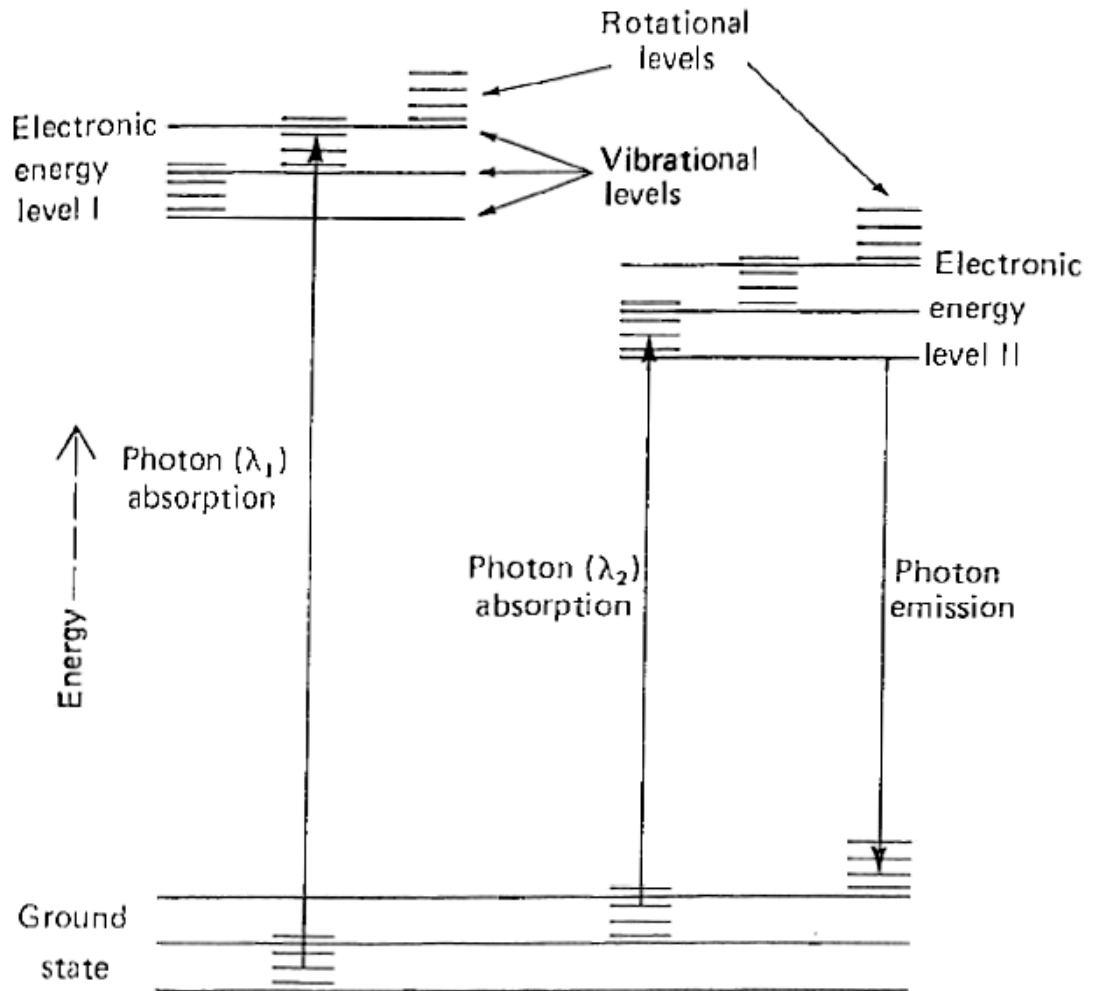


# Energy levels of molecule: Mechanism of light absorption

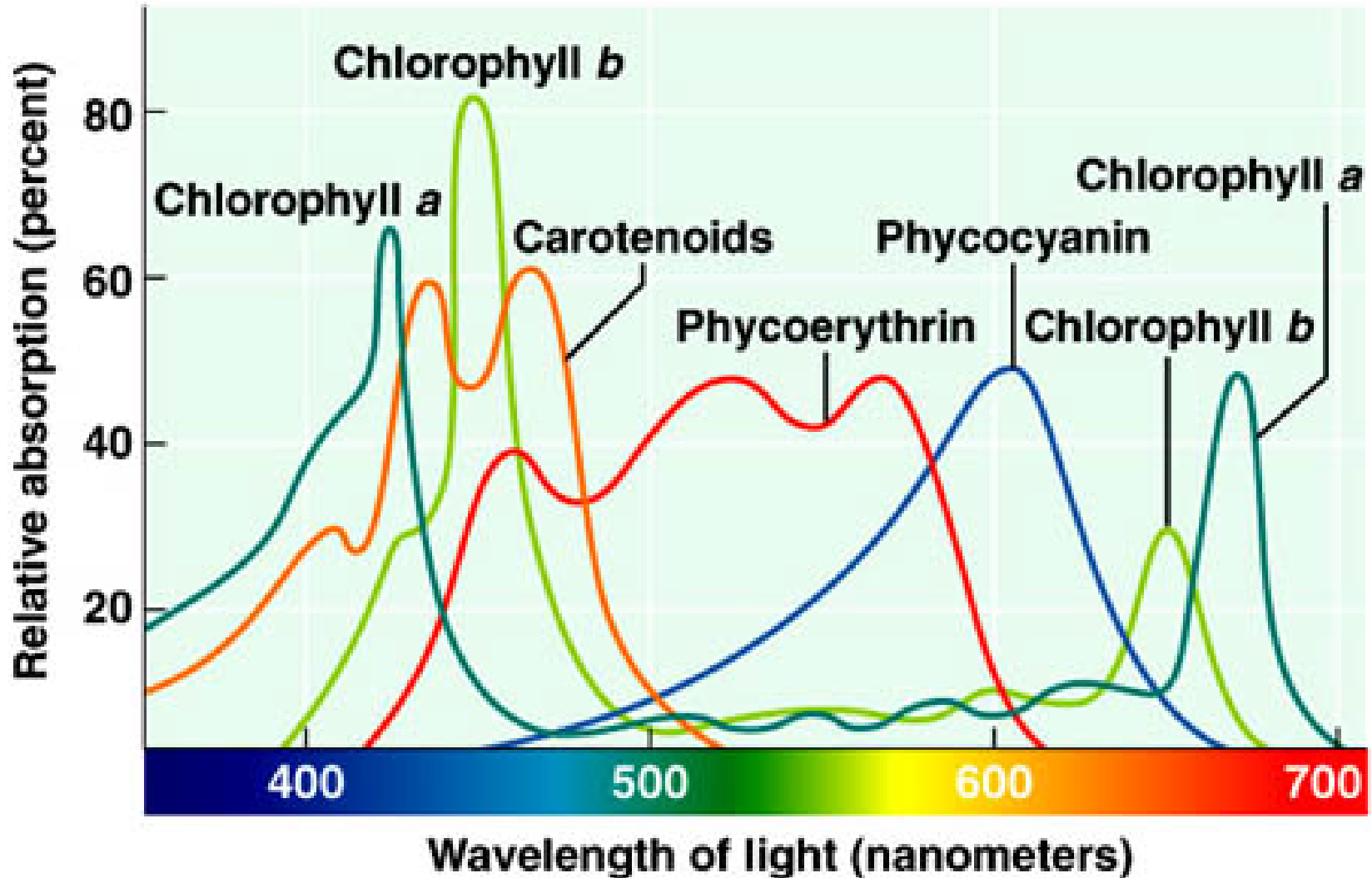
Electronic:  
energy  $\sim 400$  kJ/mol  
 $\lambda \sim 100 - 1000$  nm

Vibrational:  
energy  $\sim 4 - 40$  kJ/mol  
 $\lambda \sim 1 - 20$   $\mu\text{m}$

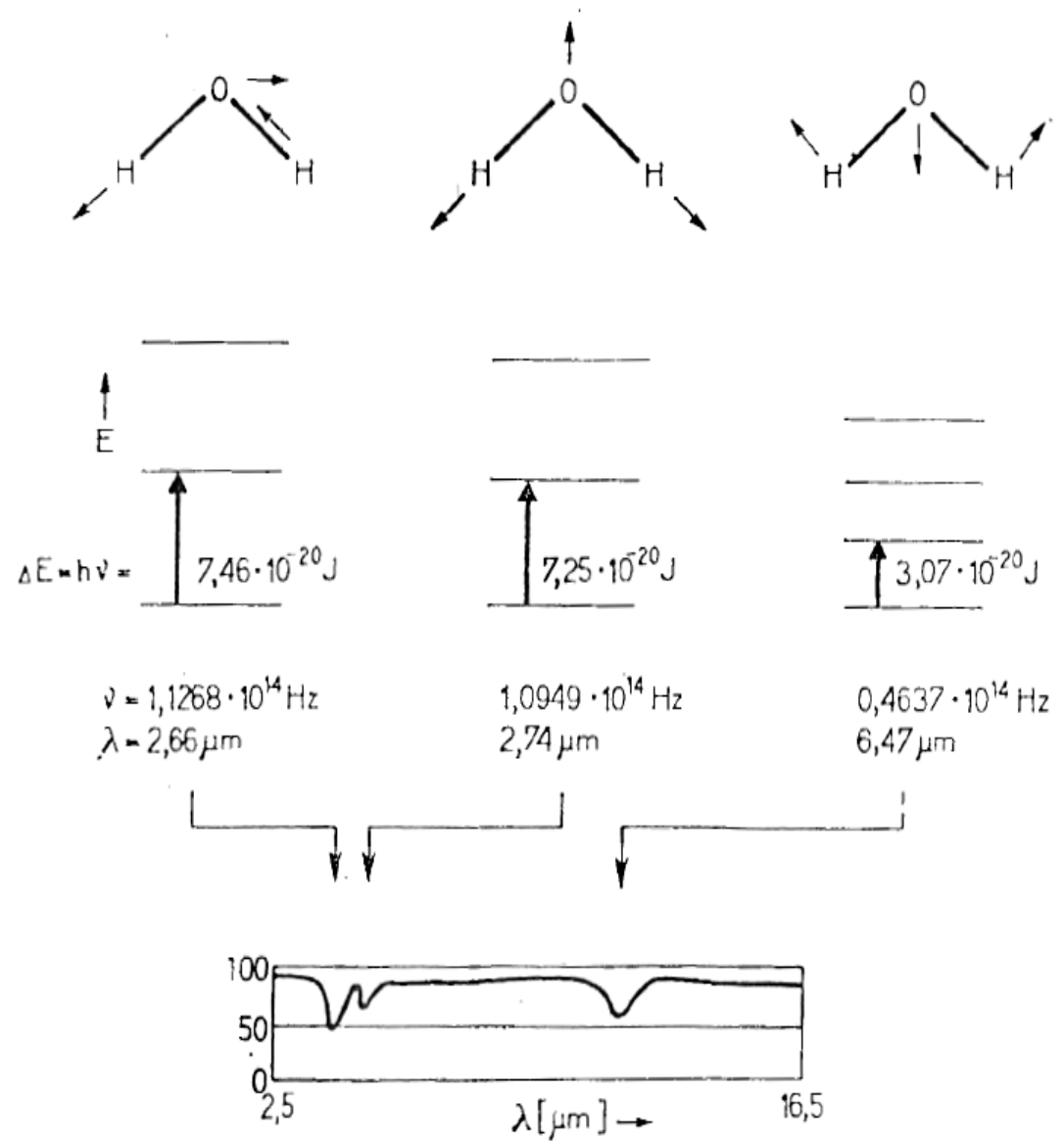
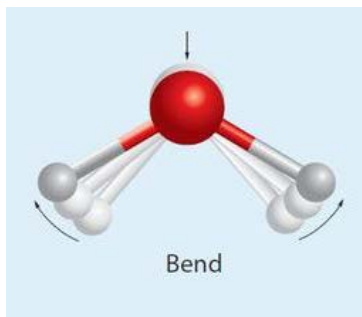
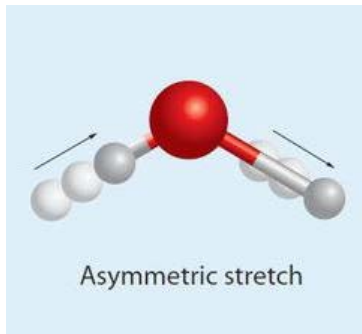
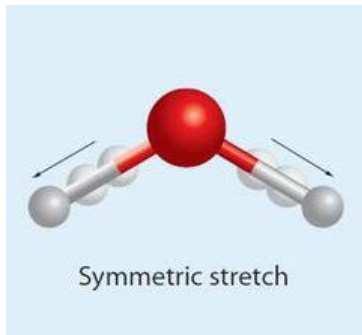
Rotational:  
energy  $\sim 10^{-2} - 10^{-3}$  kJ/mol  
 $\lambda > 20$   $\mu\text{m}$



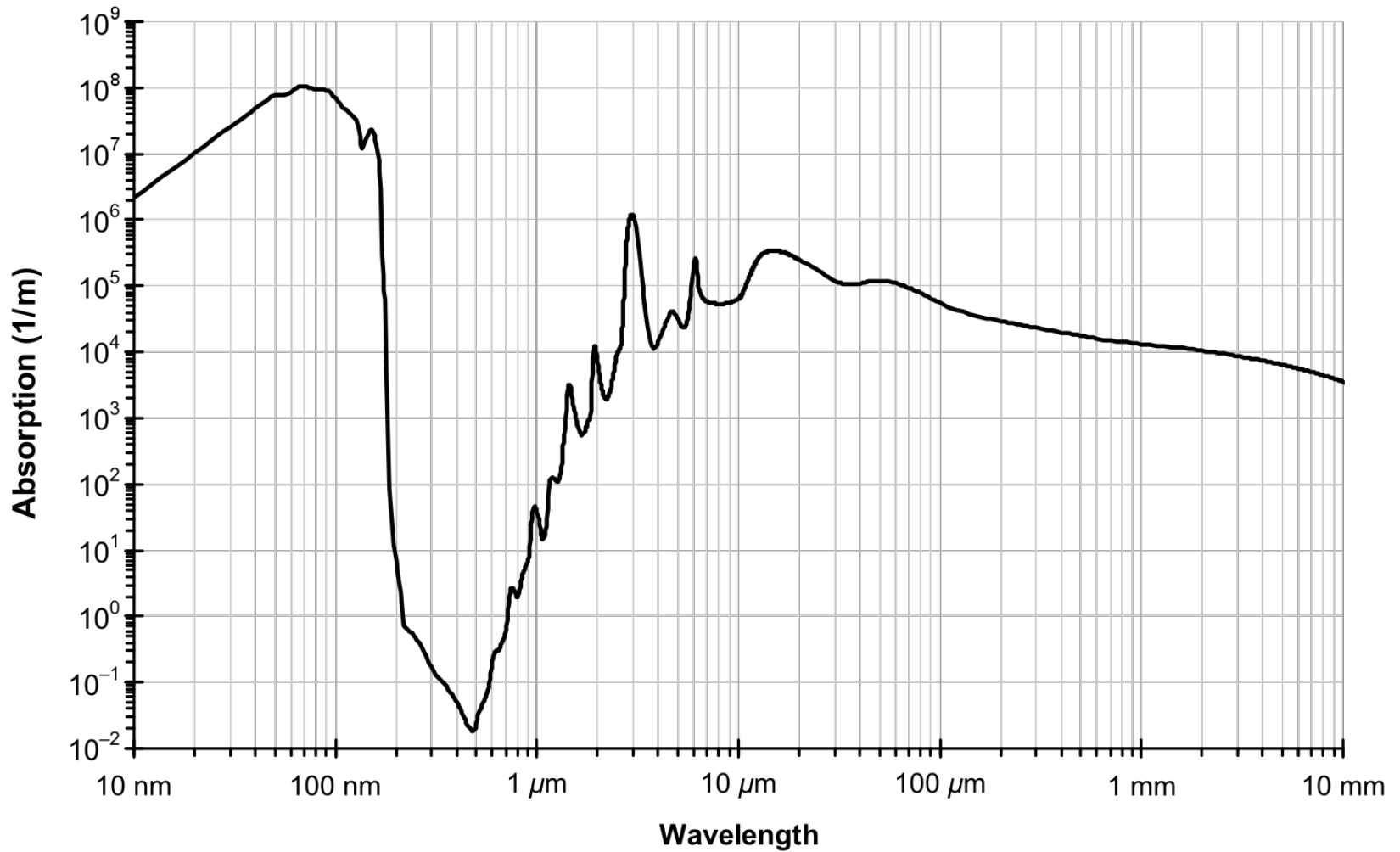
# Absorption spectra of plant pigments



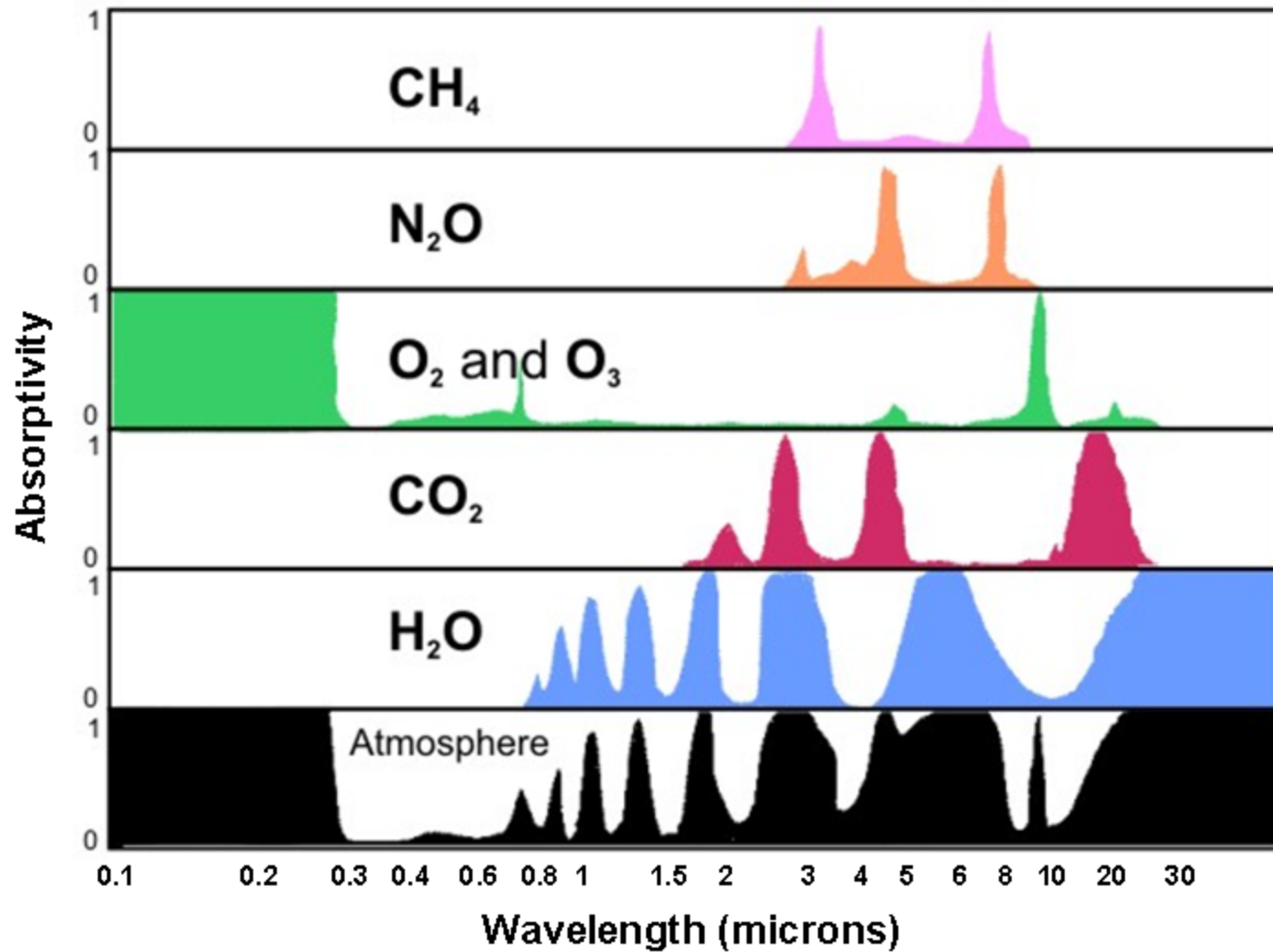
# Absorption mechanism associated with water molecule vibrations



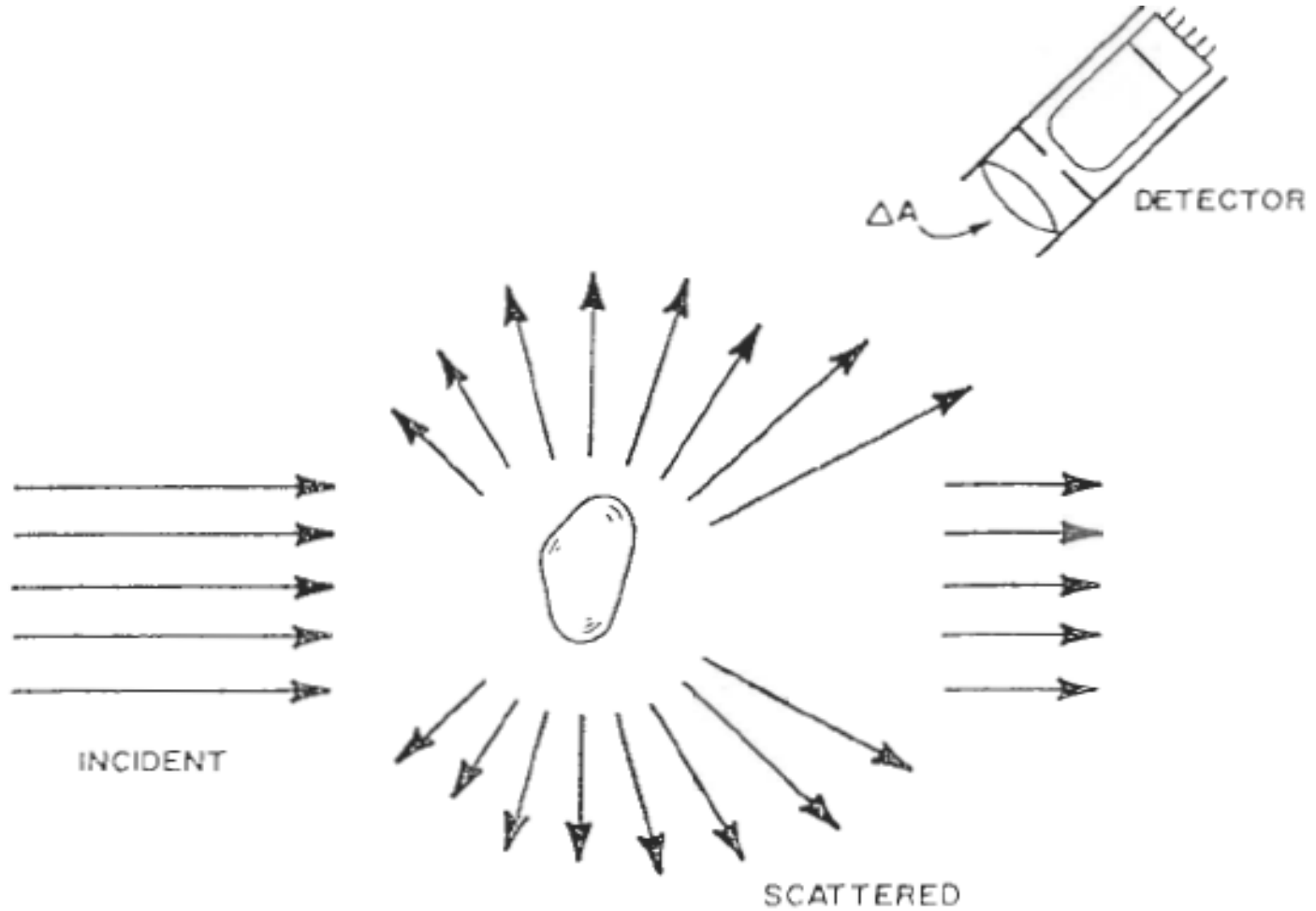
# Absorption spectrum of water molecules



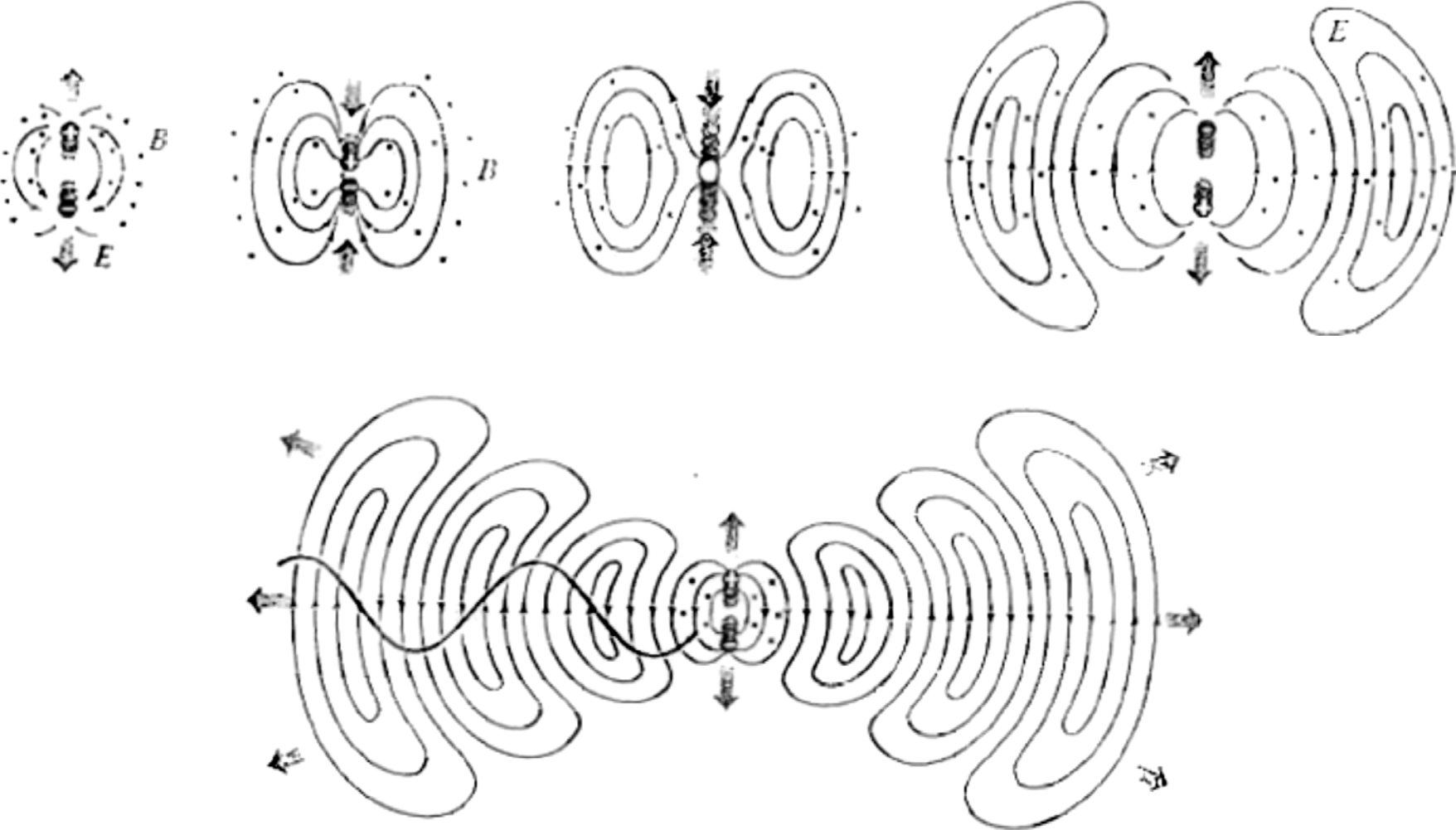
# Absorption spectra of atmospheric molecules



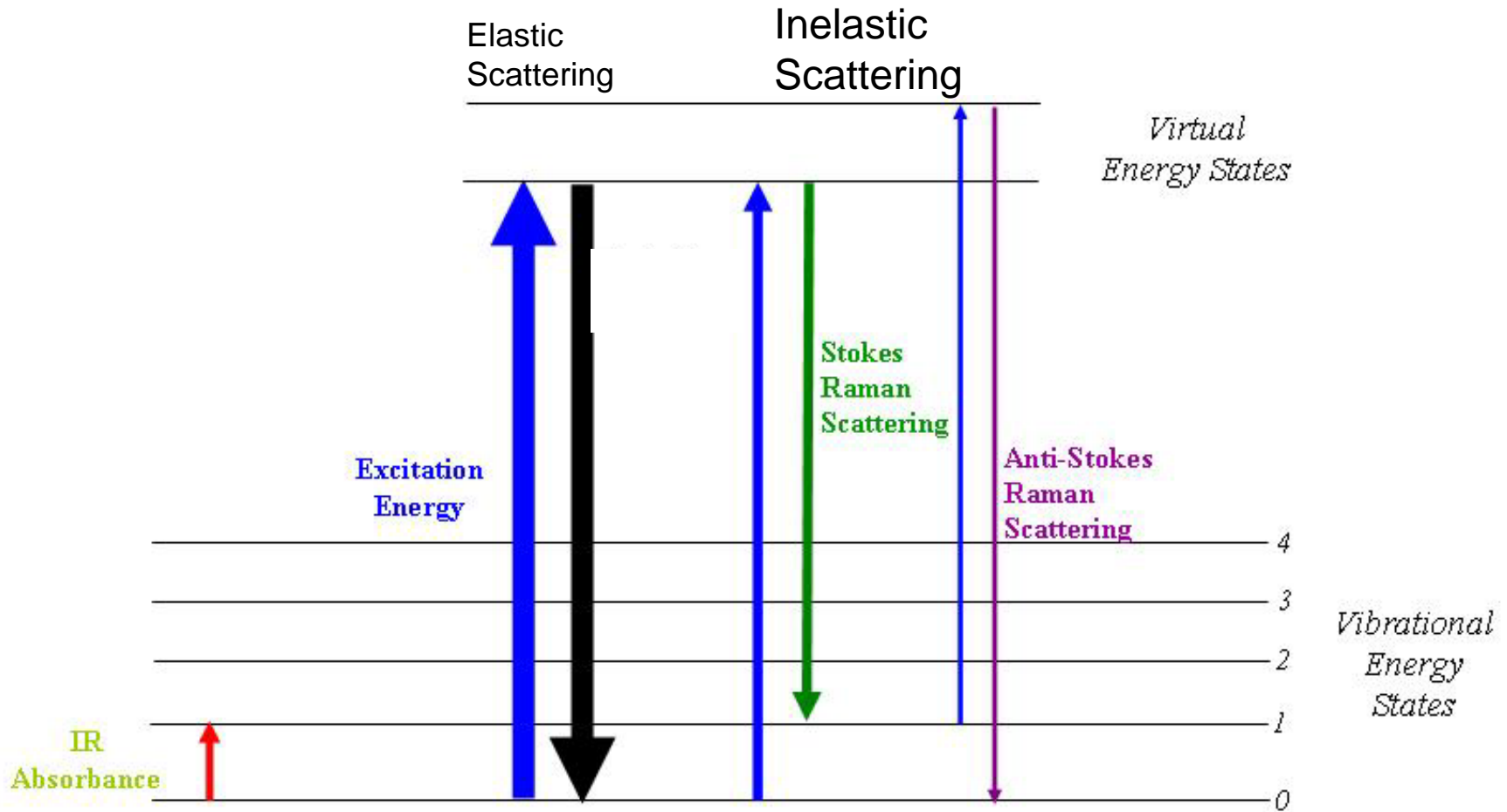
# Scattering of light by inhomogeneity of the medium



# Electromagnetic radiation of an oscillating dipole: Mechanism of light scattering

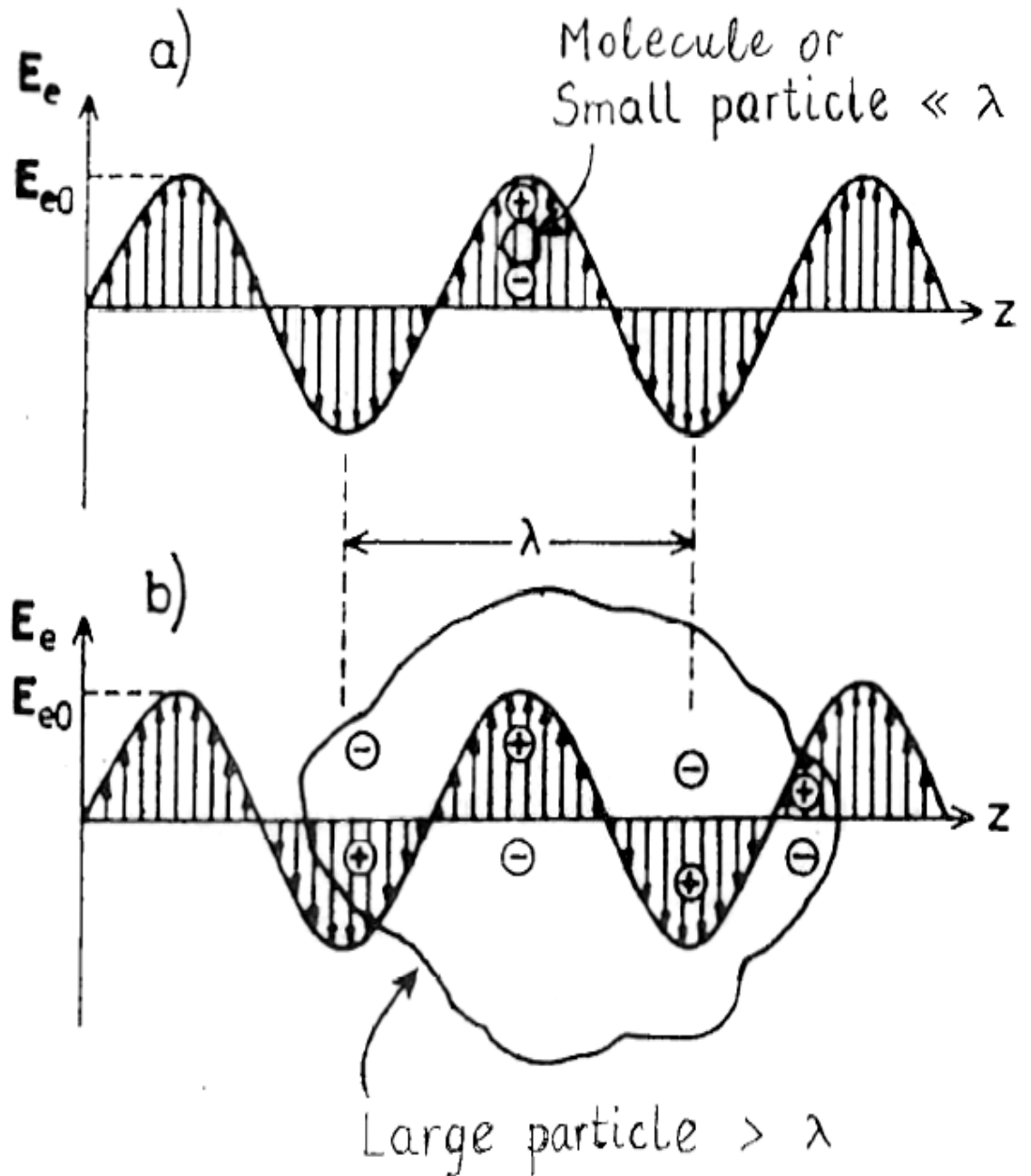


# Elastic and inelastic scattering

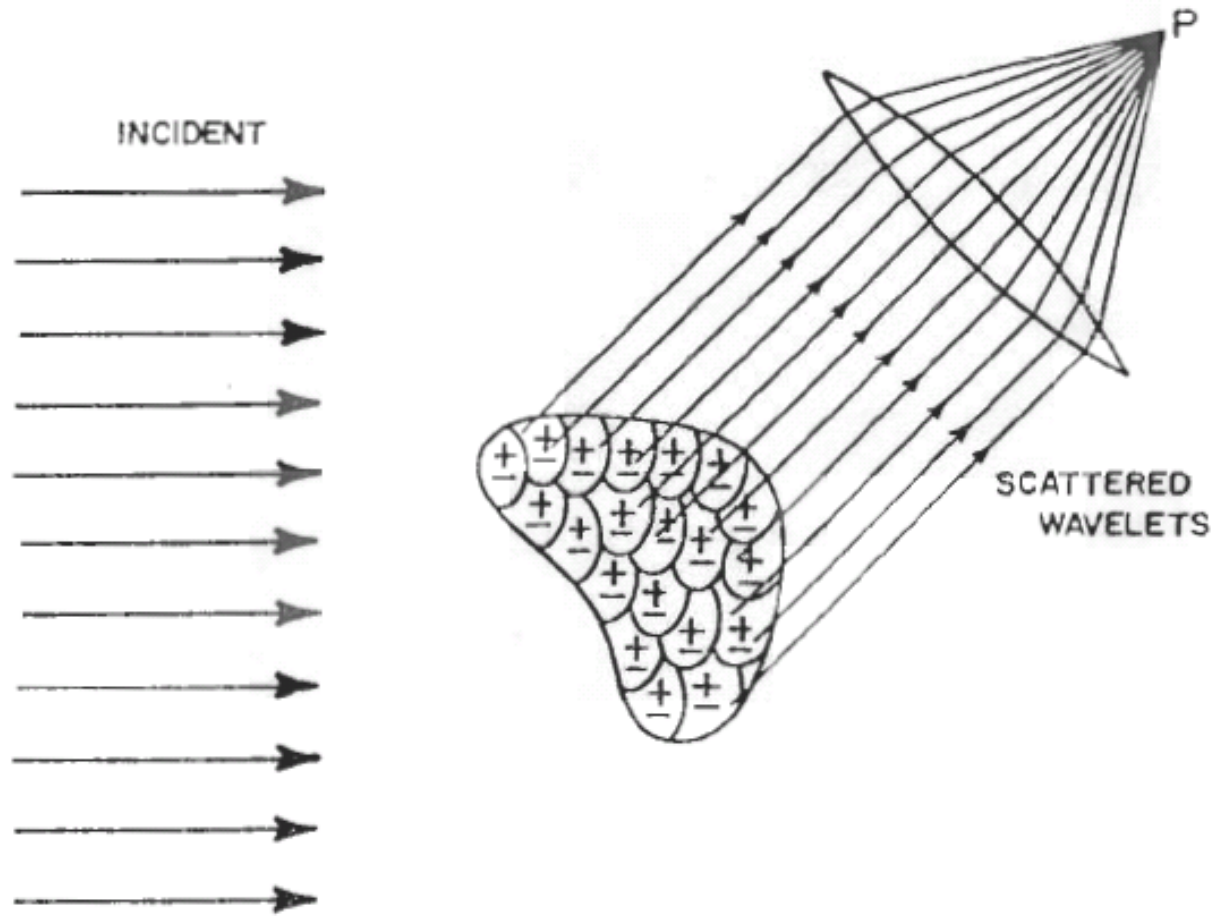




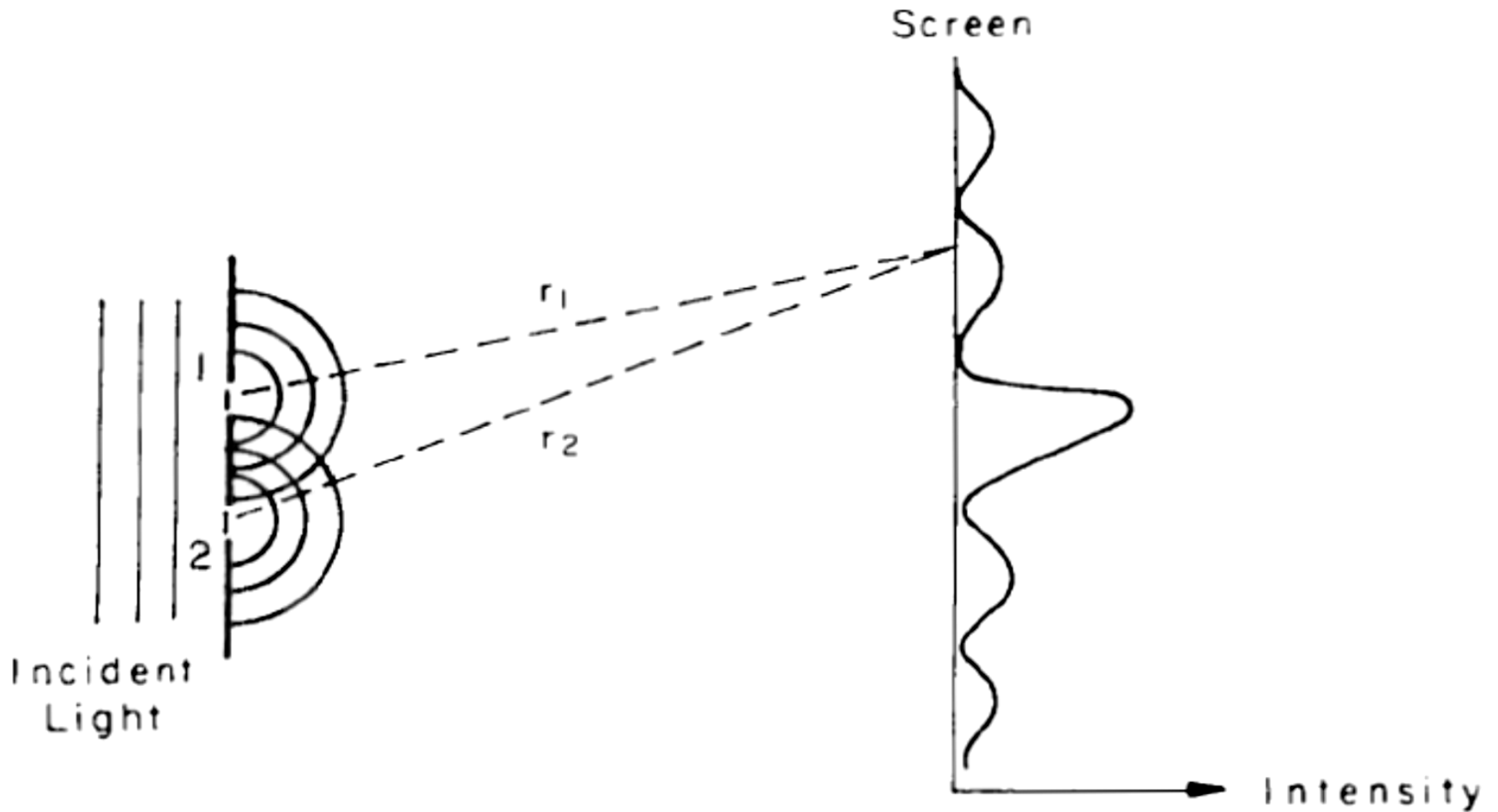
Small and large  
particle in the  
electric field of the  
electromagnetic  
wave



# A single particle subdivided into oscillating dipoles



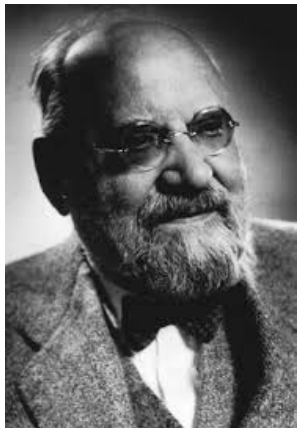
# The interference pattern produced by two slits



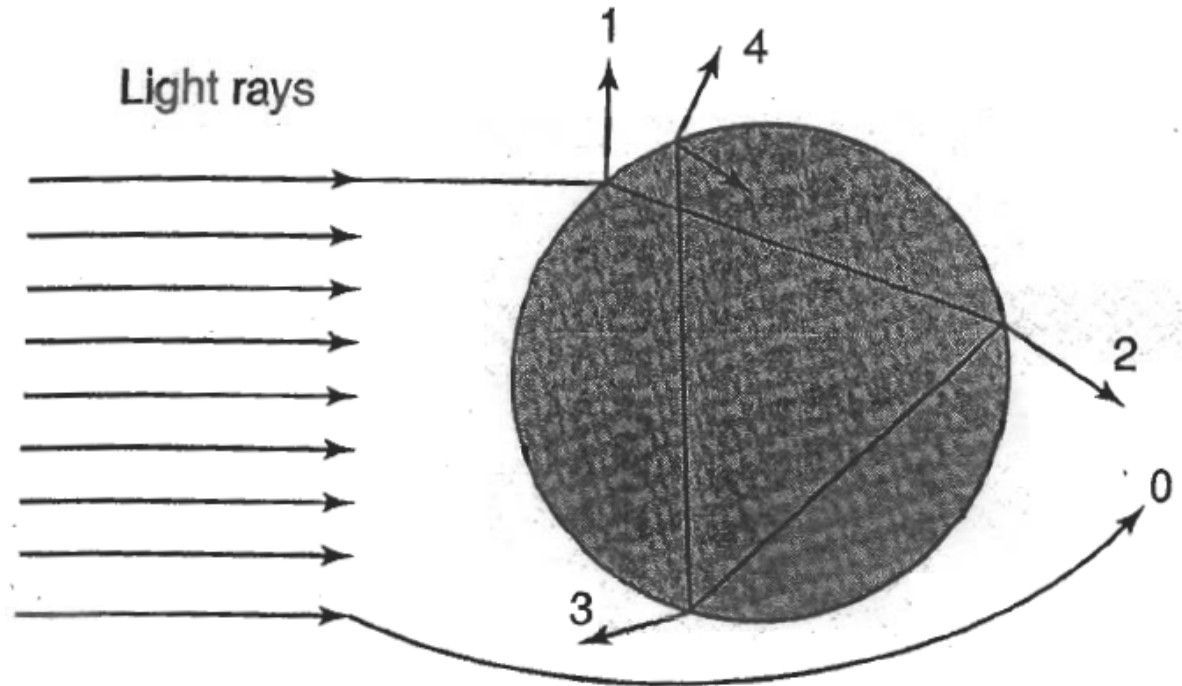
# Computations of light scattering: From Rayleigh and Mie theory to geometric ray tracing



John William Strutt  
Lord Rayleigh (1842 - 1919)  
Nobel Prize 1904



Gustav Mie (1868 - 1957)



- 0 Exterior Diffraction
- 1 External Reflection
- 2 Two Refractions
- 3 One Internal Reflection
- 4 Two Internal Reflections

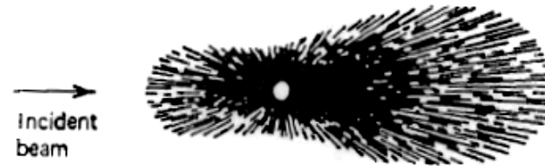
# Angular patterns of scattered intensity from particles of different sizes

Small Particles (a)



Size: smaller than one-tenth the wavelength of light  
Description: symmetric

Large Particles (b)



Size: approximately one-fourth the wavelength of light  
Description: scattering concentrated in forward direction

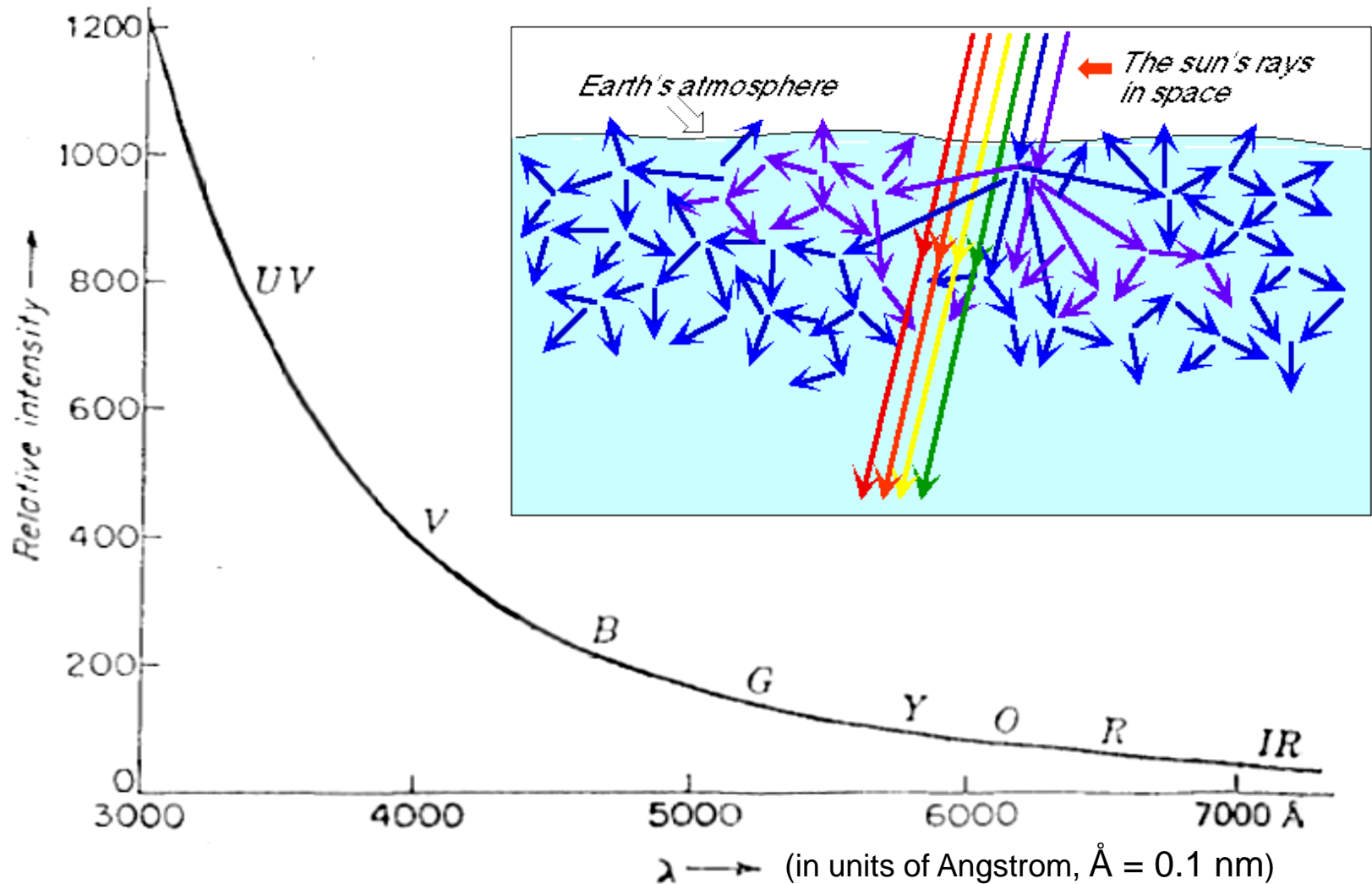
Larger Particles (c)



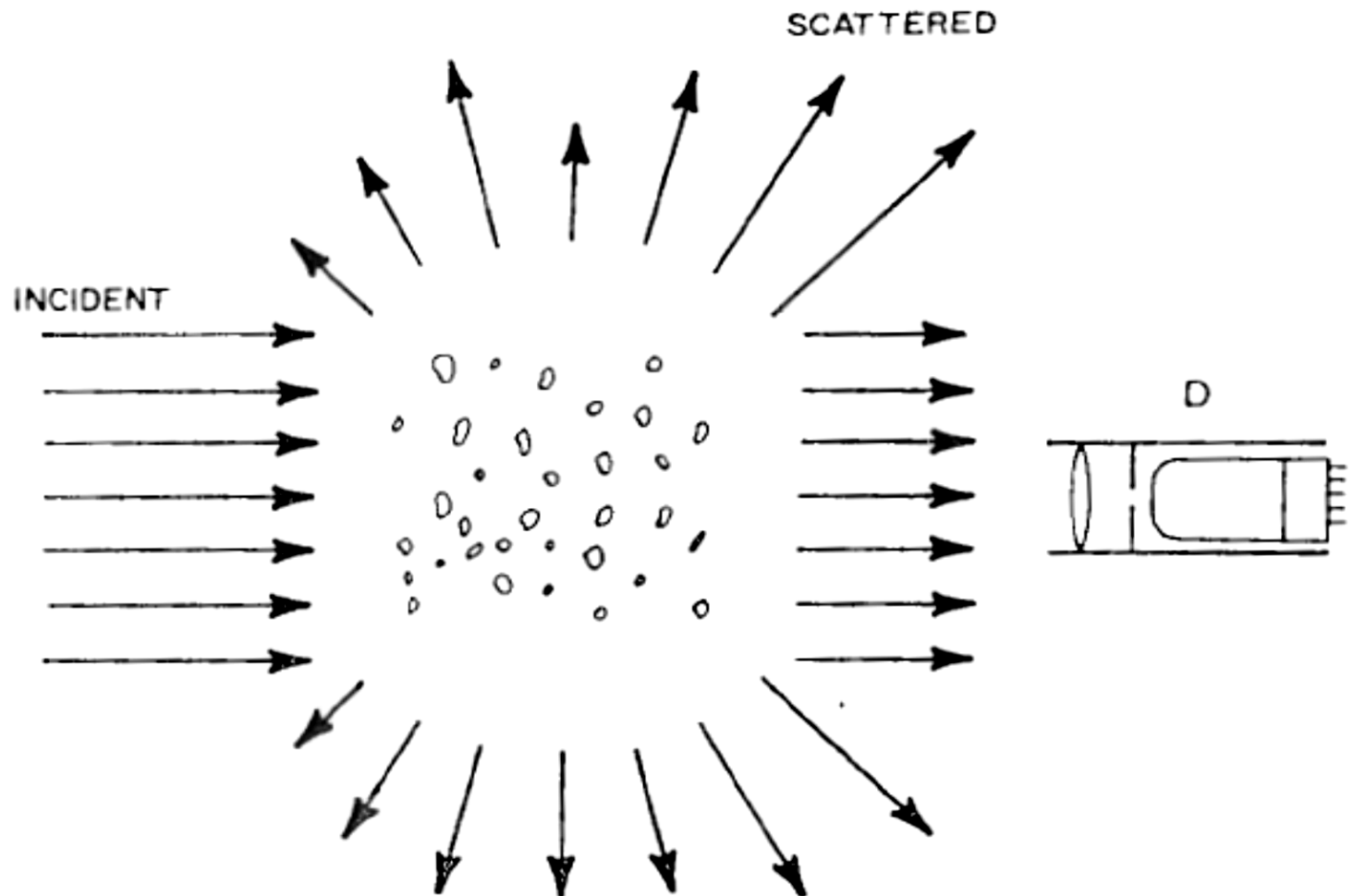
Size: larger than the wavelength of light  
Description: extreme concentration of scattering in forward direction; development of maxima and minima of scattering at wider angles

# Molecular scattering as a function of light wavelength

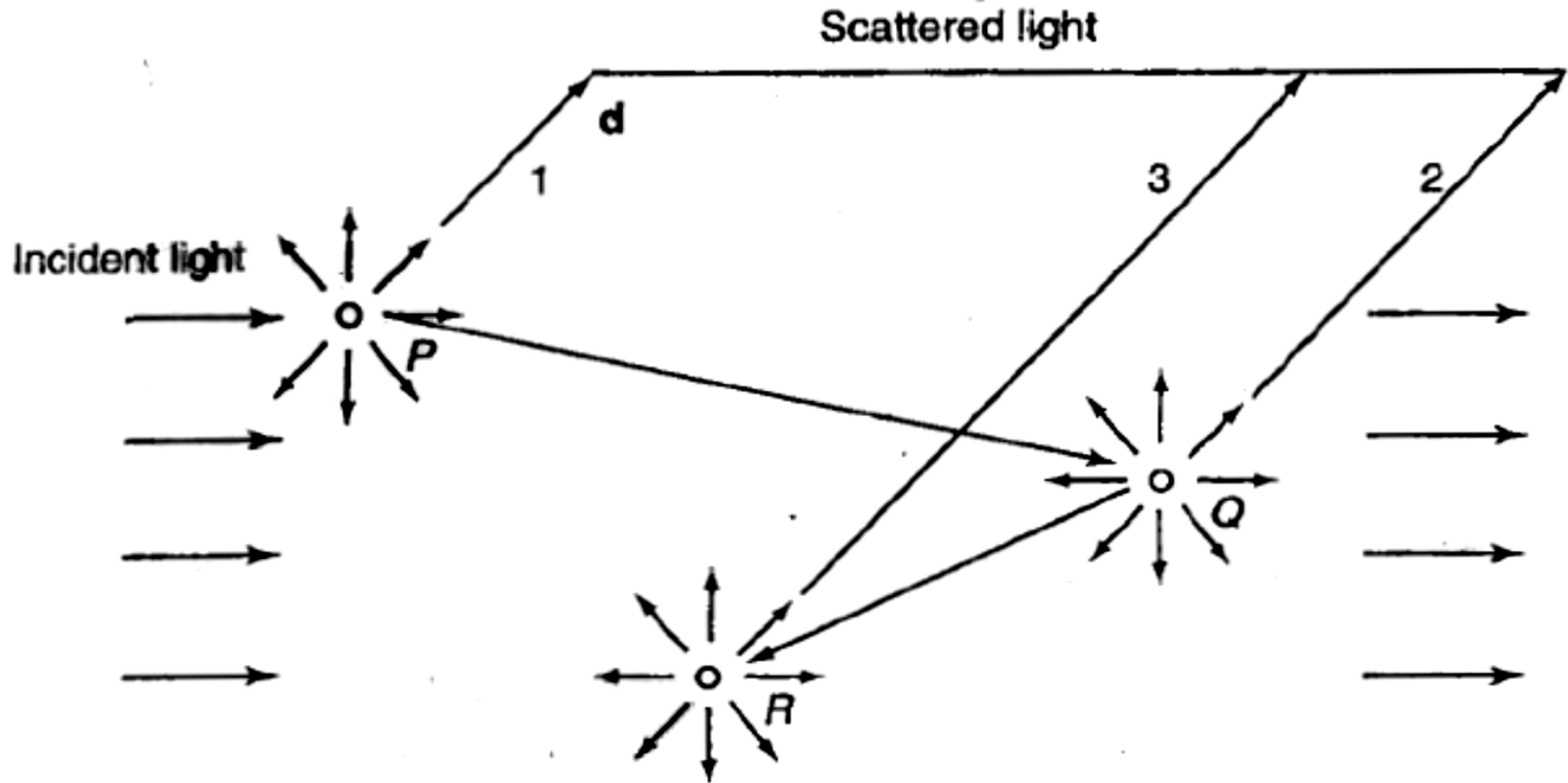
$$\text{Scattered Intensity} \sim \lambda^{-4}$$



# Scattering by a collection of particles



# Multiple light scattering by a collection of particles



**Figure 1.5** Multiple scattering process involving first ( $P$ ), second ( $Q$ ), and third ( $R$ ) order scattering in the direction denoted by  $d$ .